

# Funktionen in ' $\mathbb{R}^2$

## 9. Schulstufe

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Schwarzdruckkopiervorschläge mit großer Schrift  
und starken Linien

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Inhalt: Grafiken zu den Themen: einem x-Wert werden mehr als ein y-Wert zugeordnet, lineare Funktion, quadratische Funktion, Polynomfunktion 3. Grades, Polynomfunktion 4. Grades, gerade Funktion, ungerade Funktion, gebrochen rationale Funktion mit x im Nenner, gebrochen rationale Funktion mit  $x^2$  im Nenner, Sinusfunktion und Einheitskreis

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## Abkürzungen

f\_lin: lineare Funktion

f\_q: quadratische Funktion

f\_G3: Funktion 3. Grades

f\_G4: Funktion 4. Grades

f\_g: gerade Funktion

f\_u: ungerade Funktion

f\_gebr1: gebrochen

rationale Funktion Grad 1

f\_gebr2: gebrochen

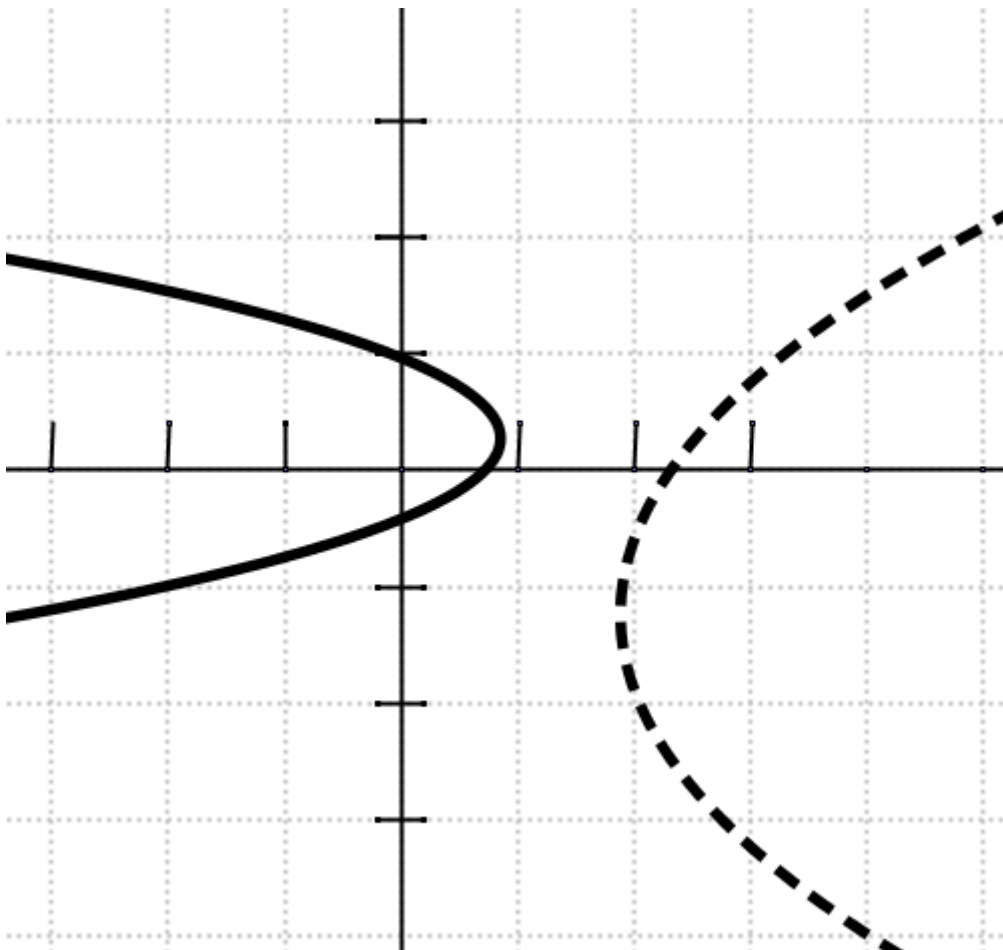
rationale Funktion Grad 2

f\_sin: Winkelfunktion

EK: Einheitskreis

## keine Funktionen

mehr y-Werte zu einem x



**f\_lin:  $f(x) = k * x + d$**

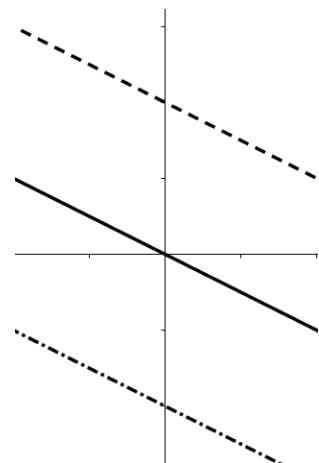
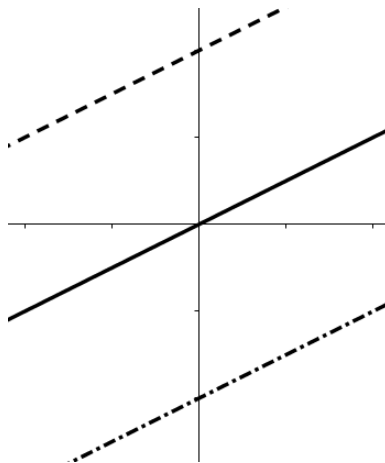
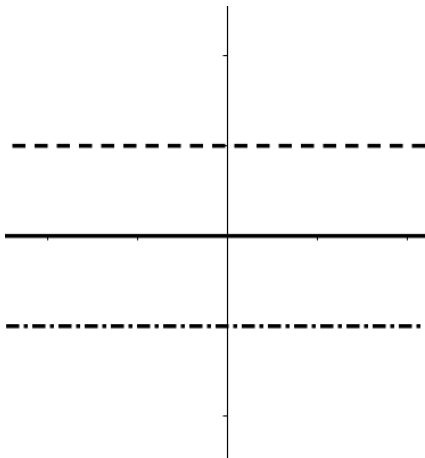
$$f(x) = k * x + d$$

$d = 0$ : 

$d > 0$ : 

$d < 0$ : 


$k = 0$     $\parallel$     $k > 0$     $\parallel$     $k < 0$



**f\_q .1:  $f(x) = a * x^2$**

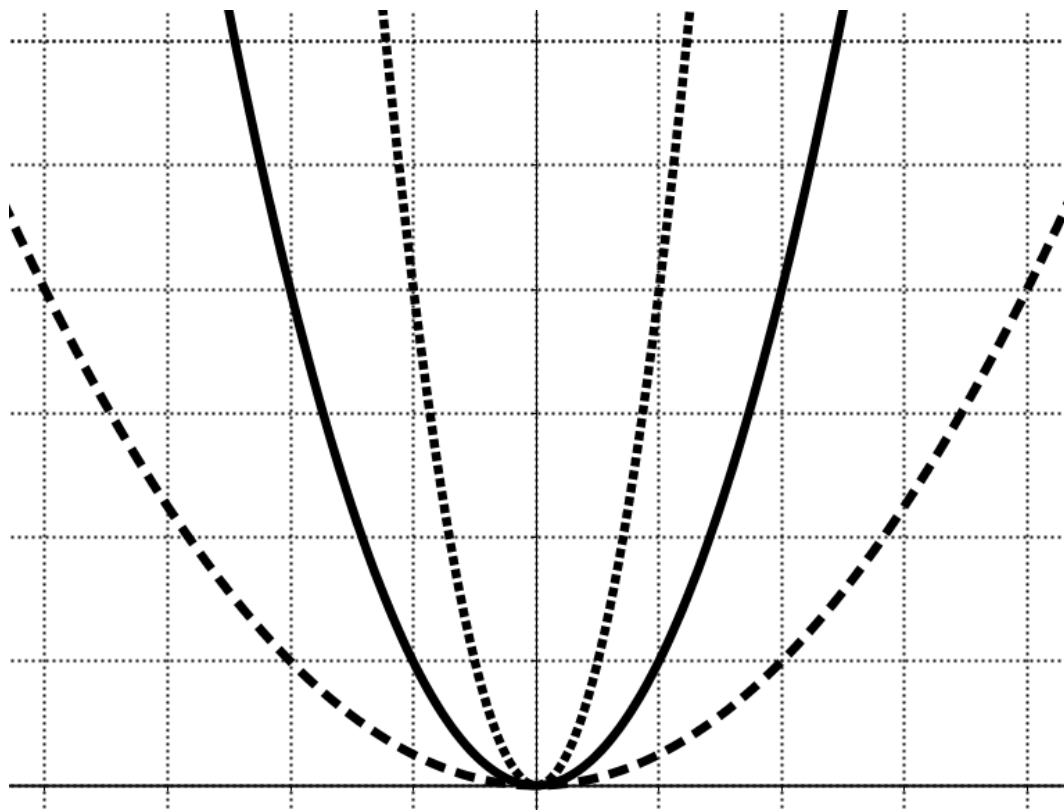
Parabel nach oben offen:

$a > 0$ : 

$f(x) = x^2$ ;  $a = +1$ : 

$f(x) = 1/4 * x^2$ ;  $a = 1/4$ : 

$f(x) = 4 * x^2$ ;  $a = 4$ : 





$f_{-q/2}: f(x) = a \cdot x^2$

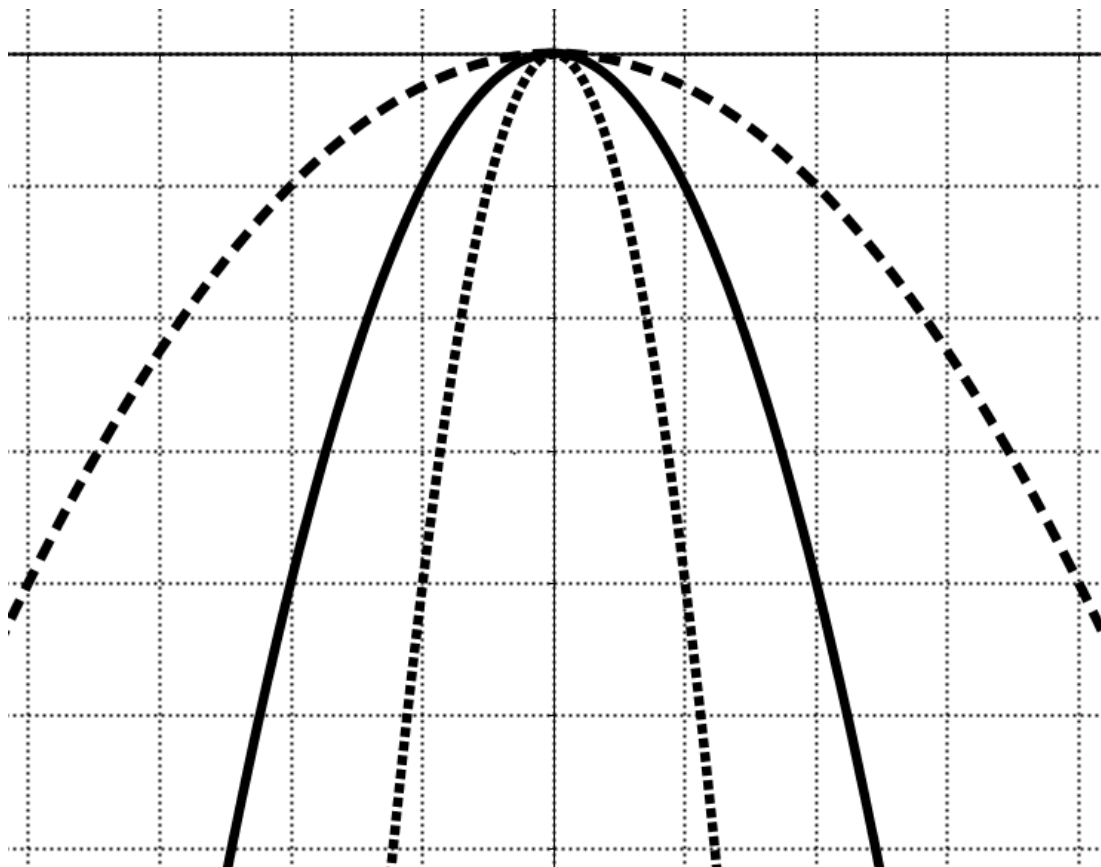
Parabel nach unten offen:

$a < 0$ : 

$f(x) = -x^2$ ;  $a = -1$ : 

$f(x) = -1/4 \cdot x^2$ ;  $a = -1/4$ : 

$f(x) = -4 \cdot x^2$ ;  $a = -4$ : 

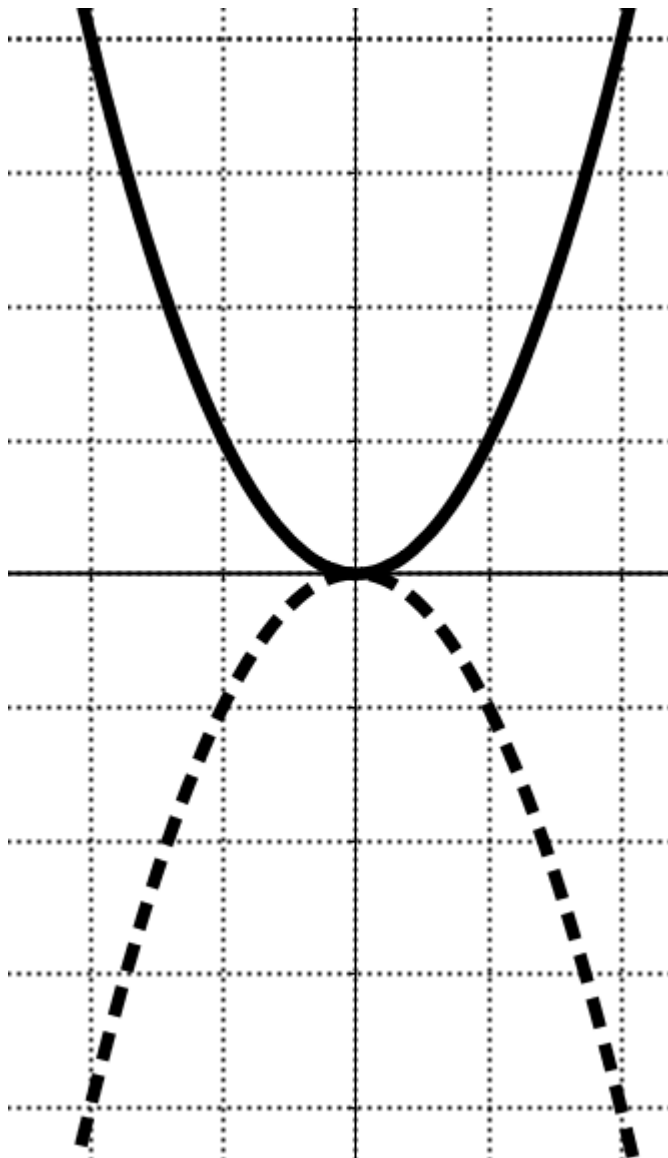




**f\_q.3:  $f(x) = a \cdot x^2$**

Parabel spiegeln

$a = 1$ : — ||  $a = -1$ : - - - - -



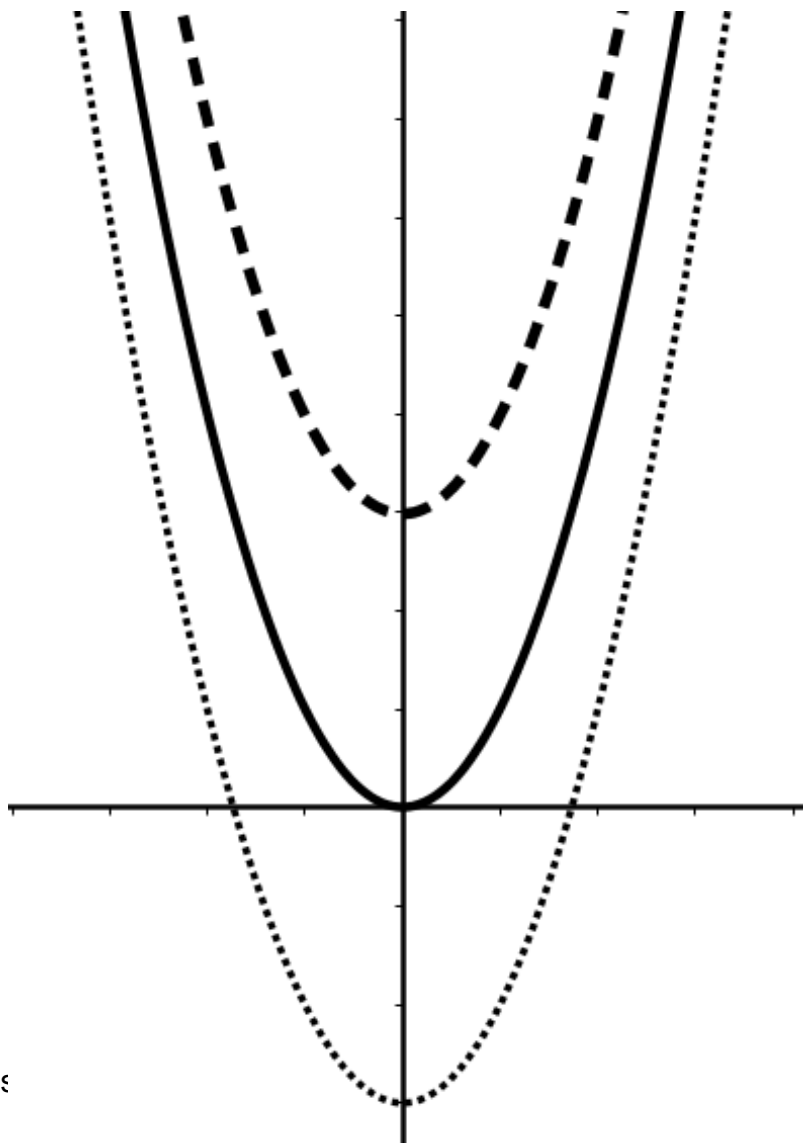
**f\_q.4:  $f(x) = x^2 + c$**

senkrecht verschieben

$c = 0$  ( $f(x) = x^2$ ): ———

$c > 0$  (hinauf): - - - - -

$c < 0$  (hinunter): .....  
.....



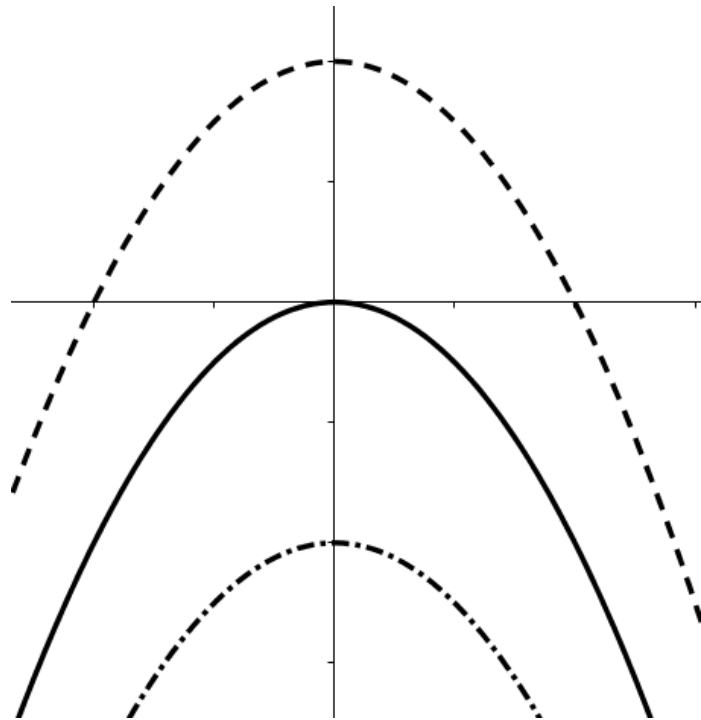
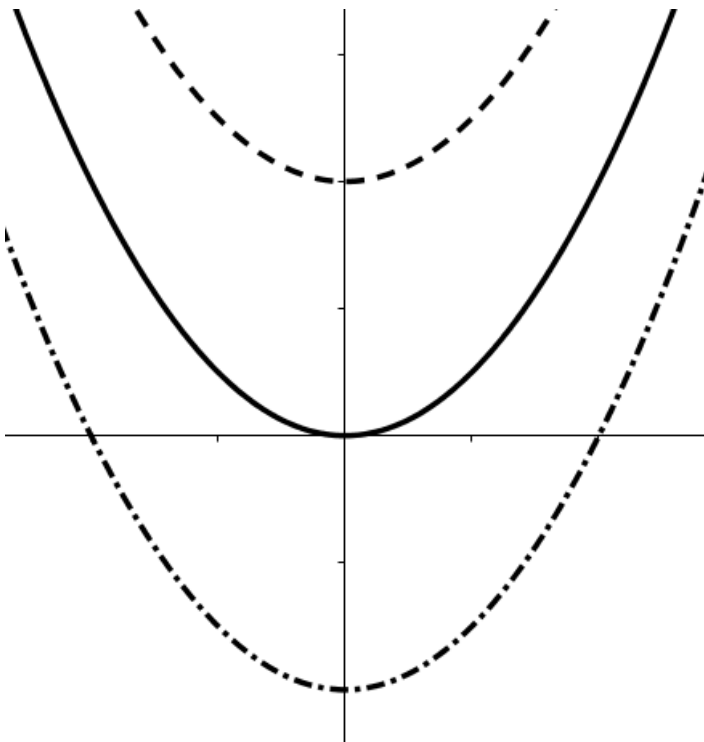
**f\_q.5:  $f(x) = a \cdot x^2 + c$**

$c = 0$ : ———

$c > 0$ : - - - -

$c < 0$ : — . —

$a > 0$                       ||                       $a < 0$



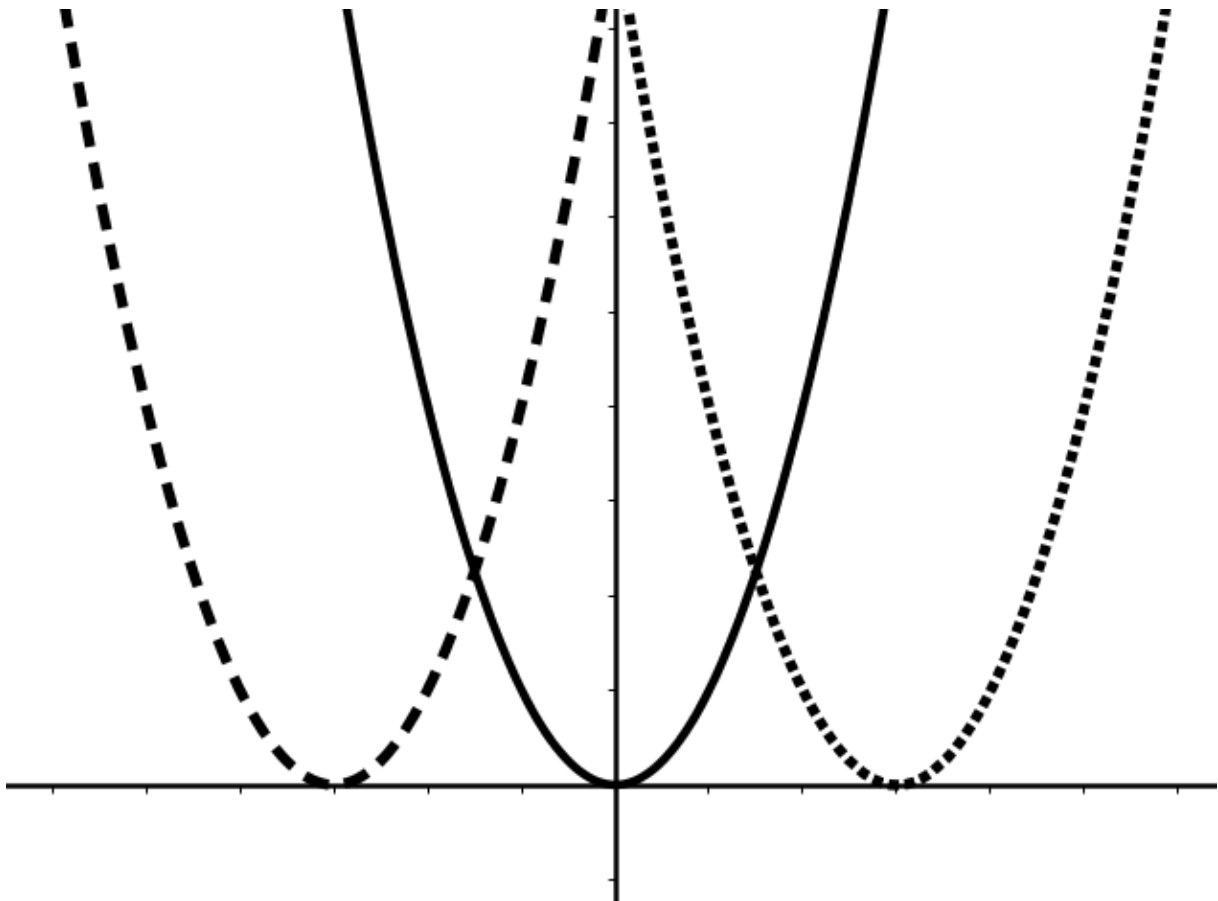
**f\_q.6:  $f(x) = (x + b)^2$**

waagrecht verschieben

$b = 0$  ( $f(x) = x^2$ ): ———

$b > 0$  (nach links): - - - -

$b < 0$  (nach rechts): .....

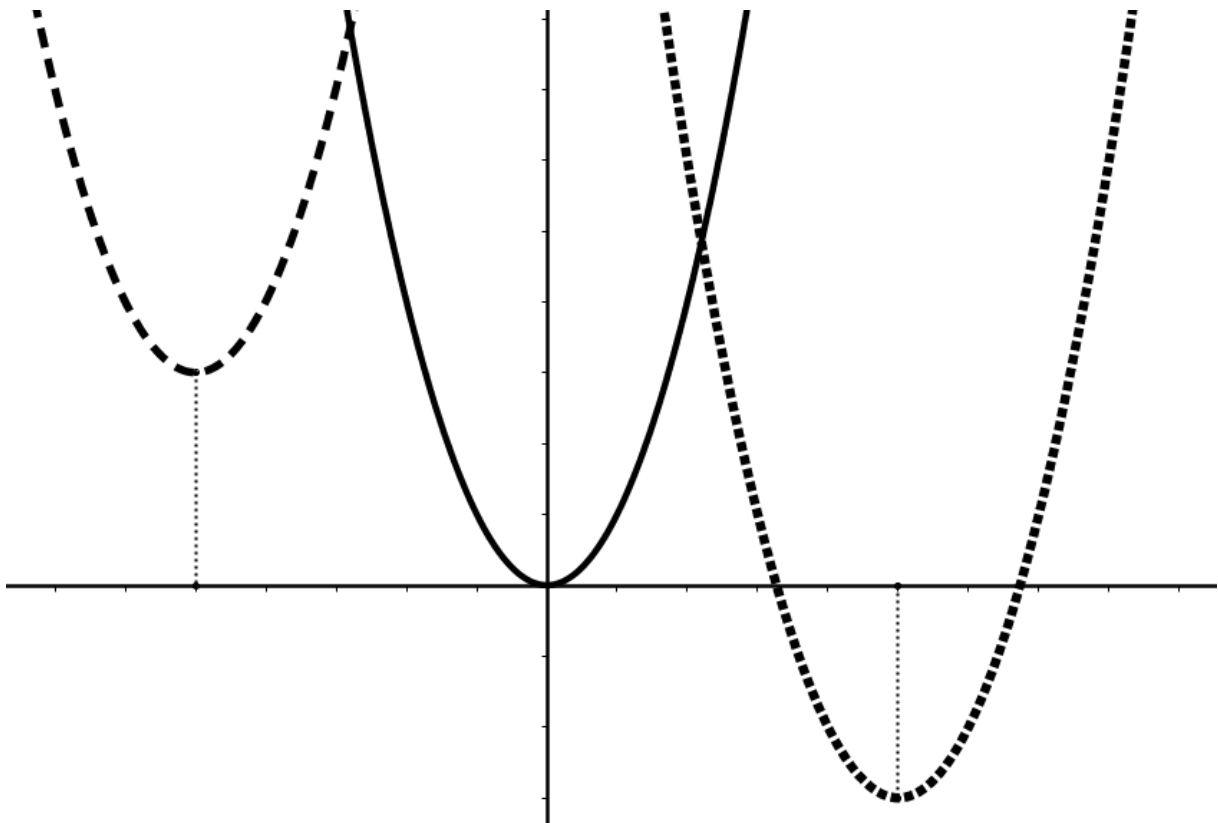


**f\_q.7:  $f(x) = (x + b)^2 + c$**

$b = 0, c = 0$  ( $f(x) = x^2$ ): ———

$b > 0, c > 0$  (li, hinauf): - - - -

$b < 0, c < 0$  (re, hinunter): .....

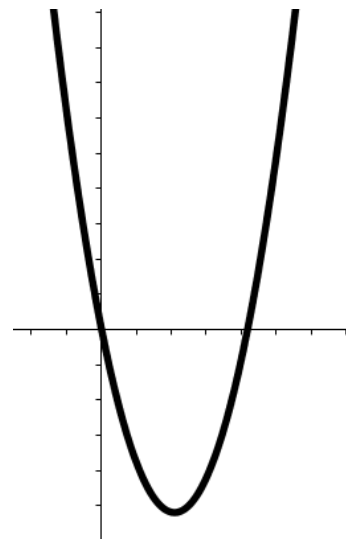
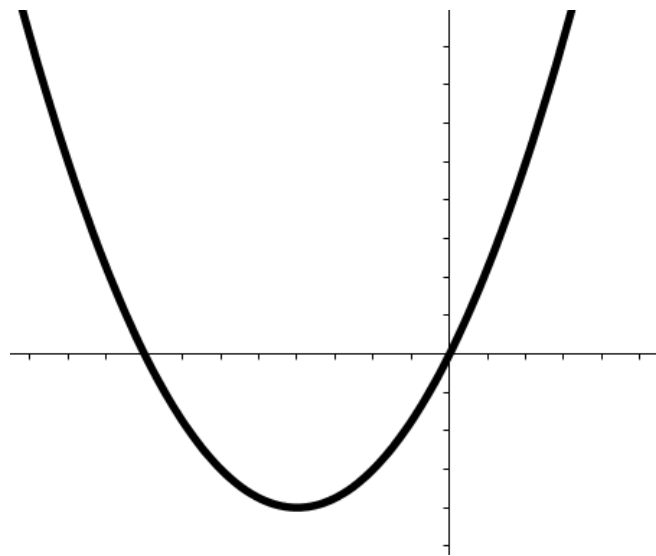


**f\_q.8:  $f(x) = a \cdot x^2 + b \cdot x$**

enthält Ursprung (0|0)

$a > 0, b > 0$

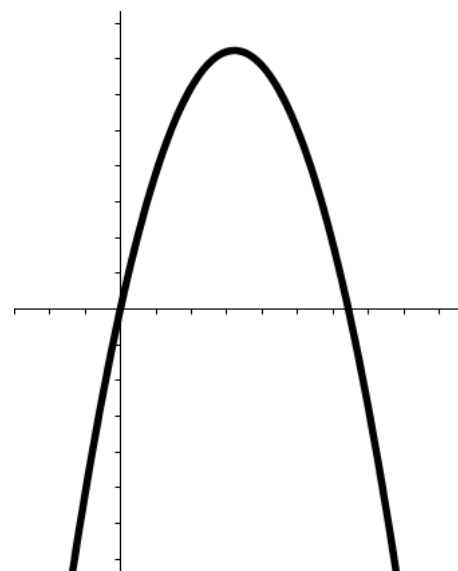
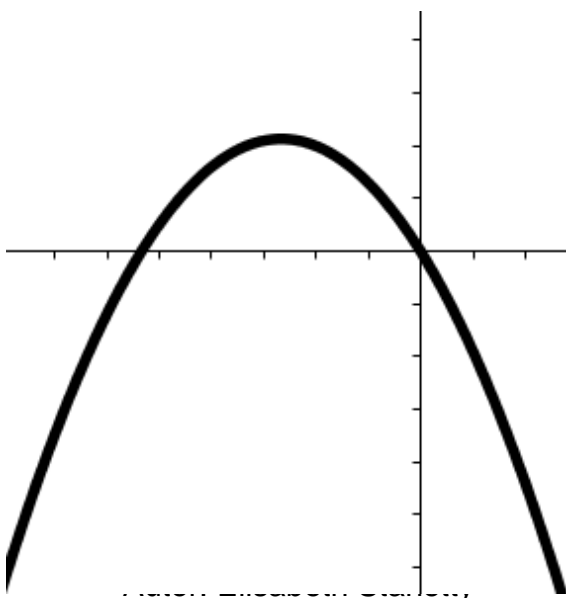
$a > 0, b < 0$



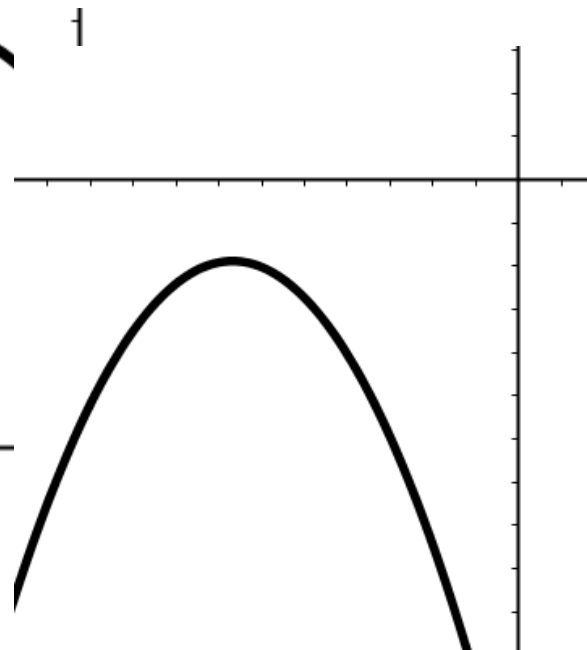
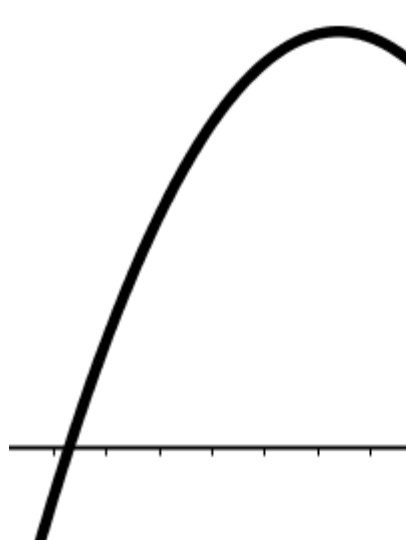
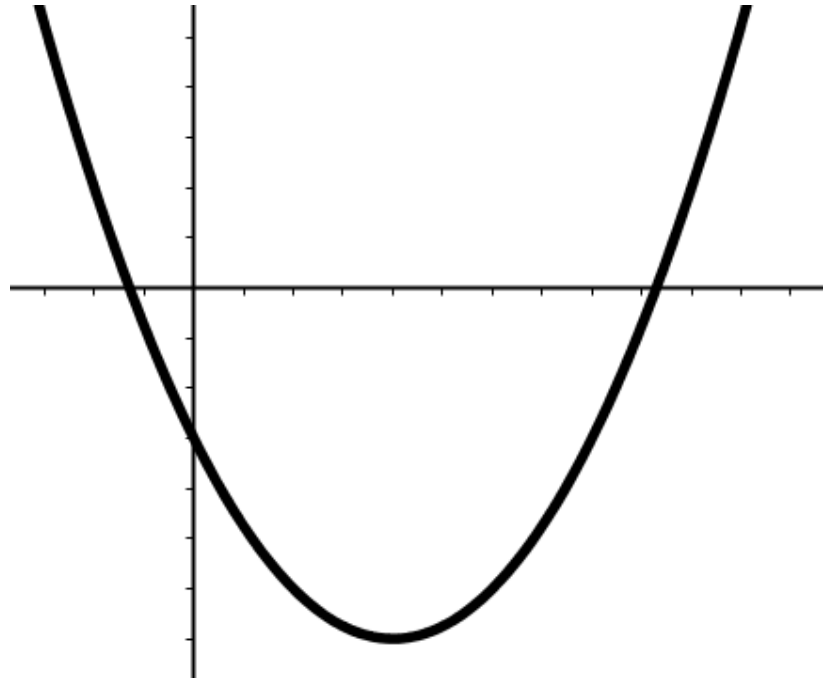
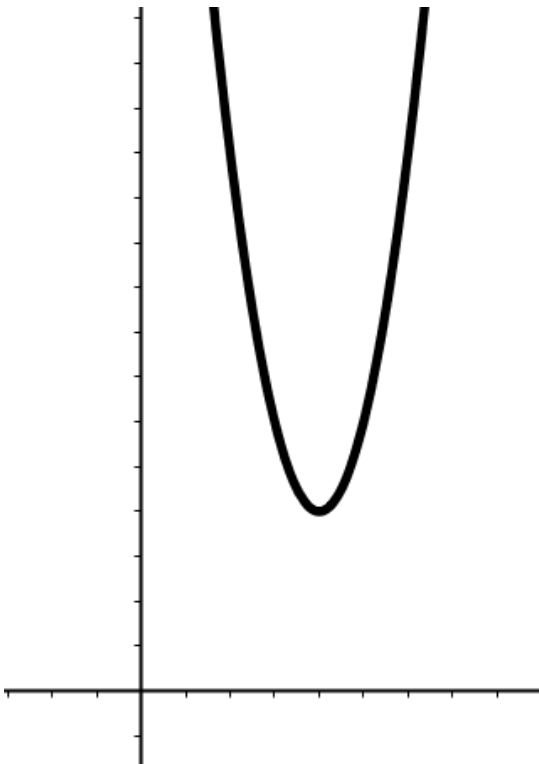
a

$a < 0, b > 0$

$a < 0, b < 0$



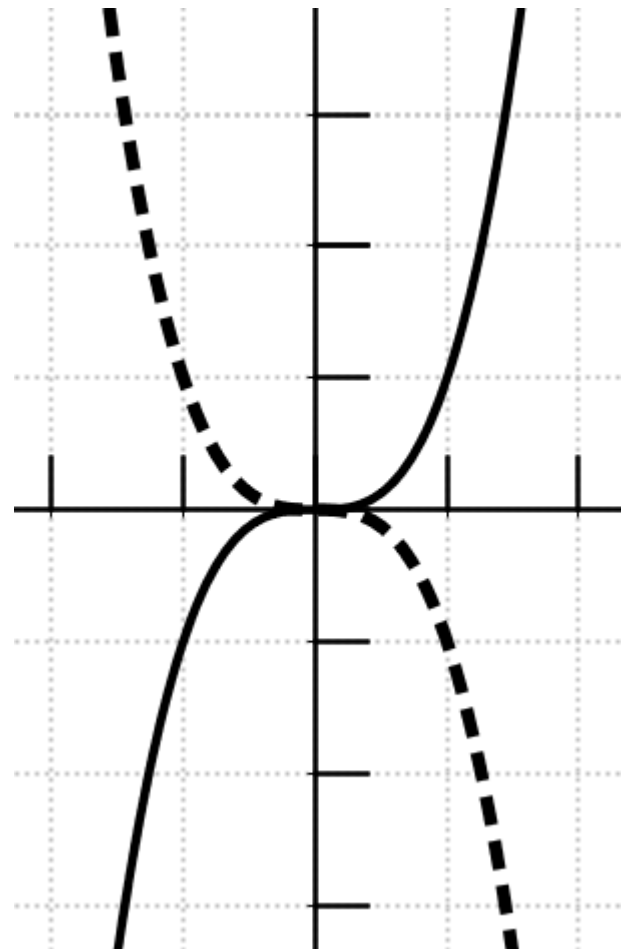
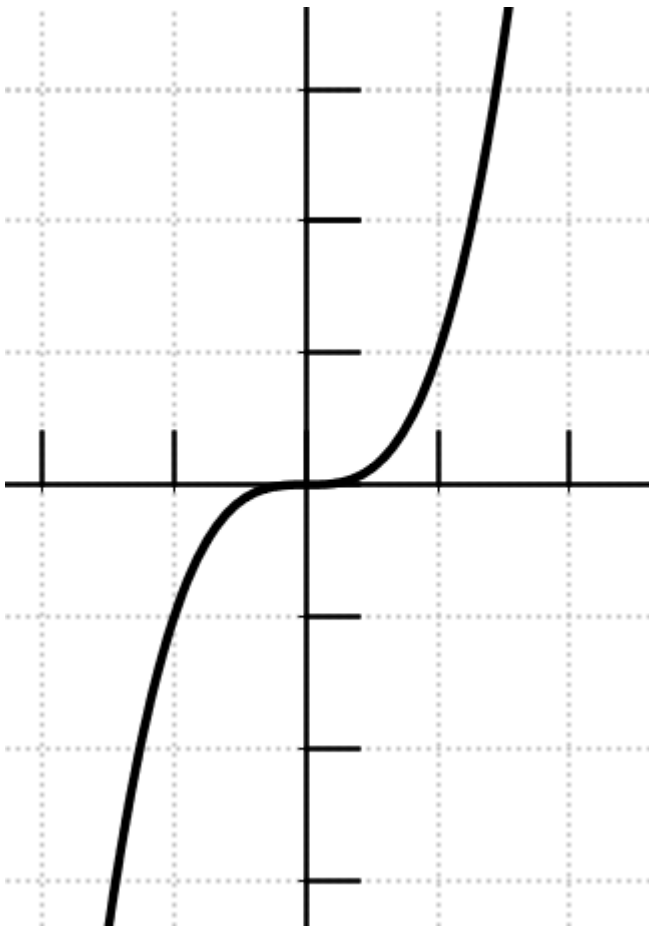
**f\_q.9: f:  $a * x^2 + b * x + c$**



**f\_G3.1:  $f(x) = a * x^3$**

$a = 1$  ( $f(x) = x^3$ ): ———

$a = -1$  ( $f(x) = -x^3$ ): - - - -





$$f\_G3.2: f(x) = a * x^3 + c$$

senkrecht verschieben

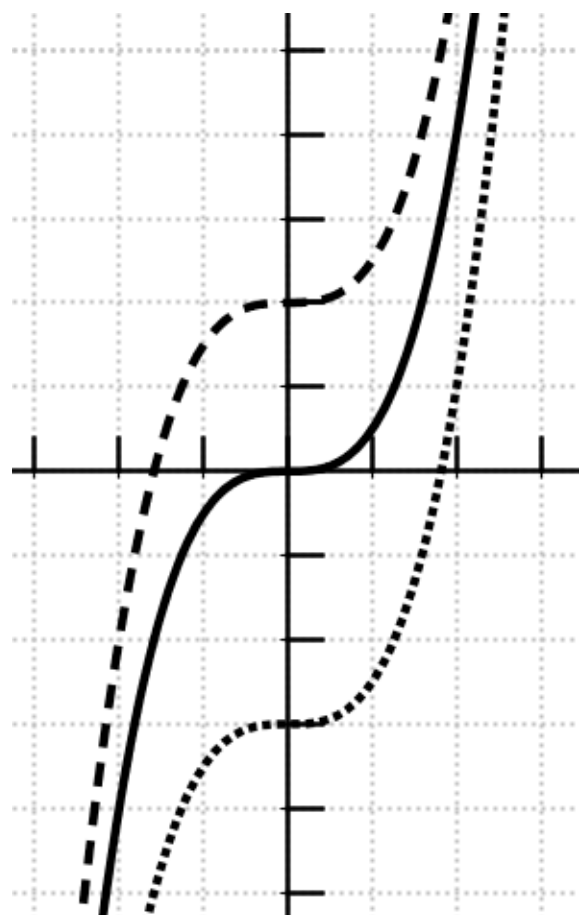
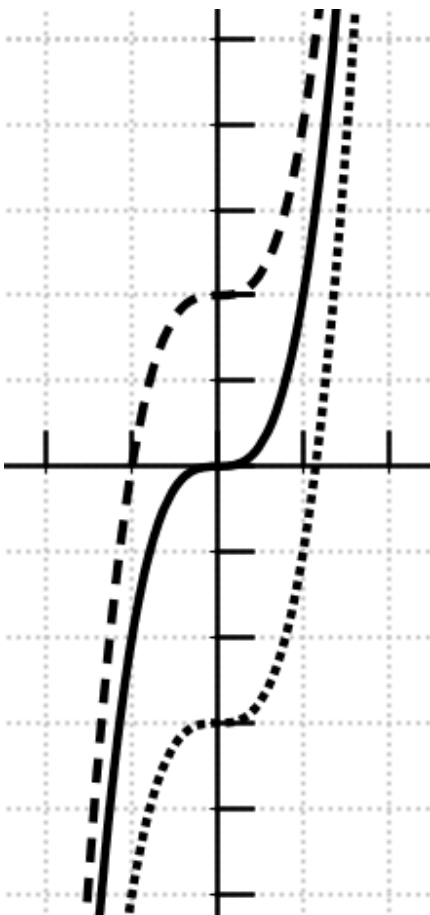
$a > 0, c = 0$ : ———

$a > 0, c > 0$  (hinauf): - - - -

$a > 0, c < 0$  (hinunter): .....

$a=2$

$a = 0,5$



$$f_{\text{G3.3}}: f(x) = a \cdot x^3 + c$$

senkrecht verschieben

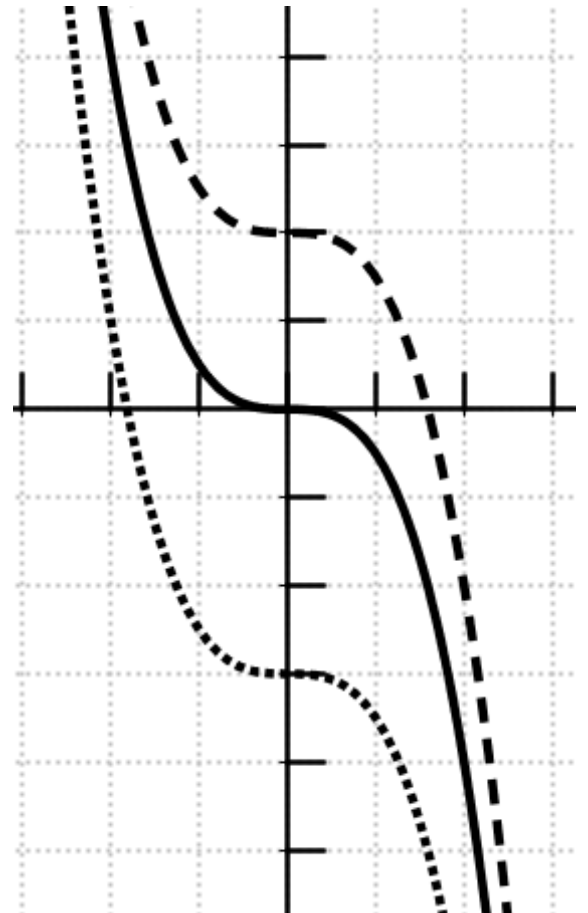
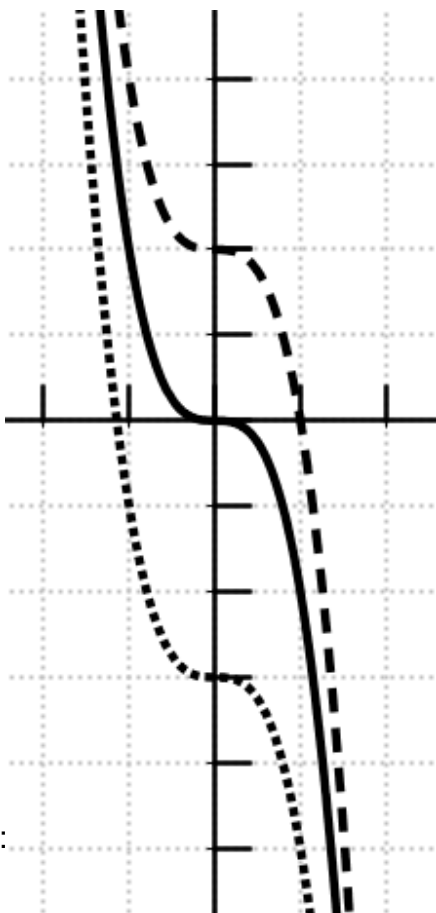
$a < 0, c = 0$ : ———

$a < 0, c > 0$  (hinauf): - - - -

$a < 0, c < 0$  (hinunter): .....

$a = -2$

$a = -0,5$



$$f\_G3.4: f(x) = (x + b)^3$$

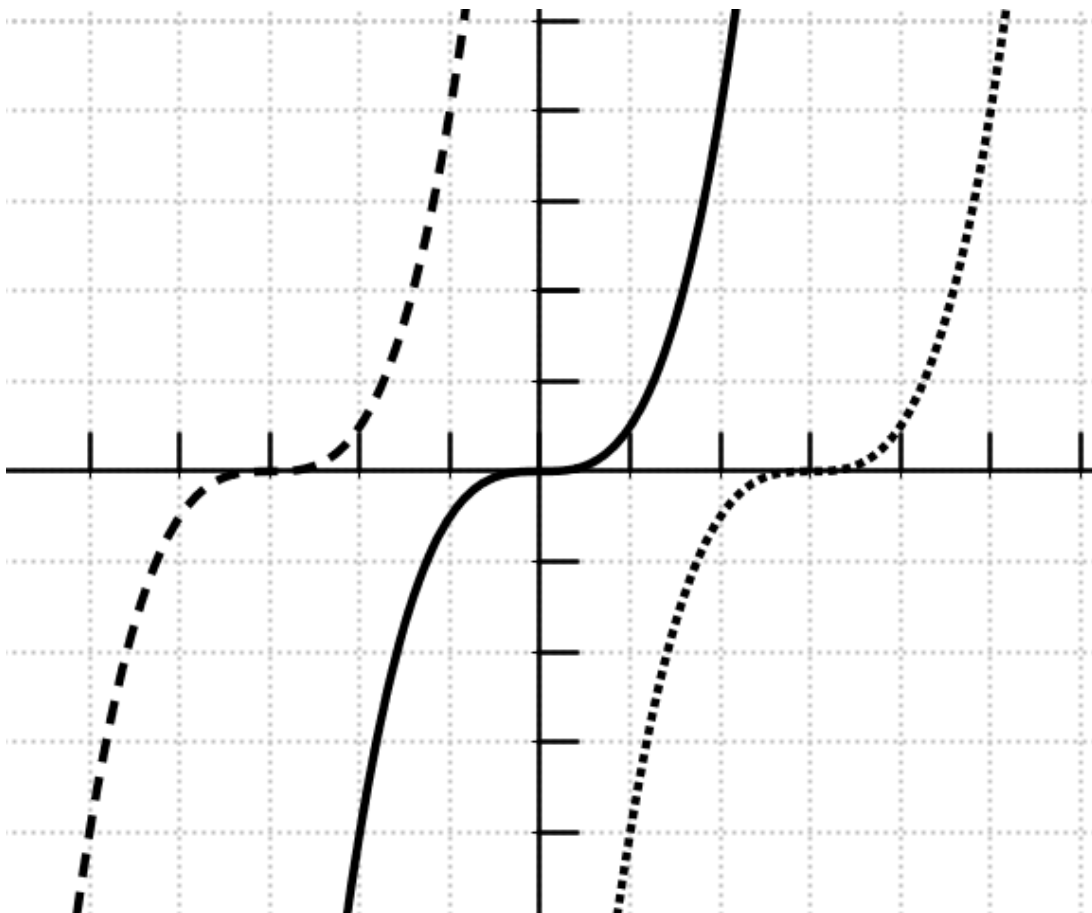
waagrecht verschieben

$a > 0, b = 0$ : ———

$a > 0, b > 0$  (nach links: - - - -

$a > 0, b < 0$  (n. rechts): .....

$$a = 0,5$$



$$f\_G3.5: f(x) = (x + b)^3$$

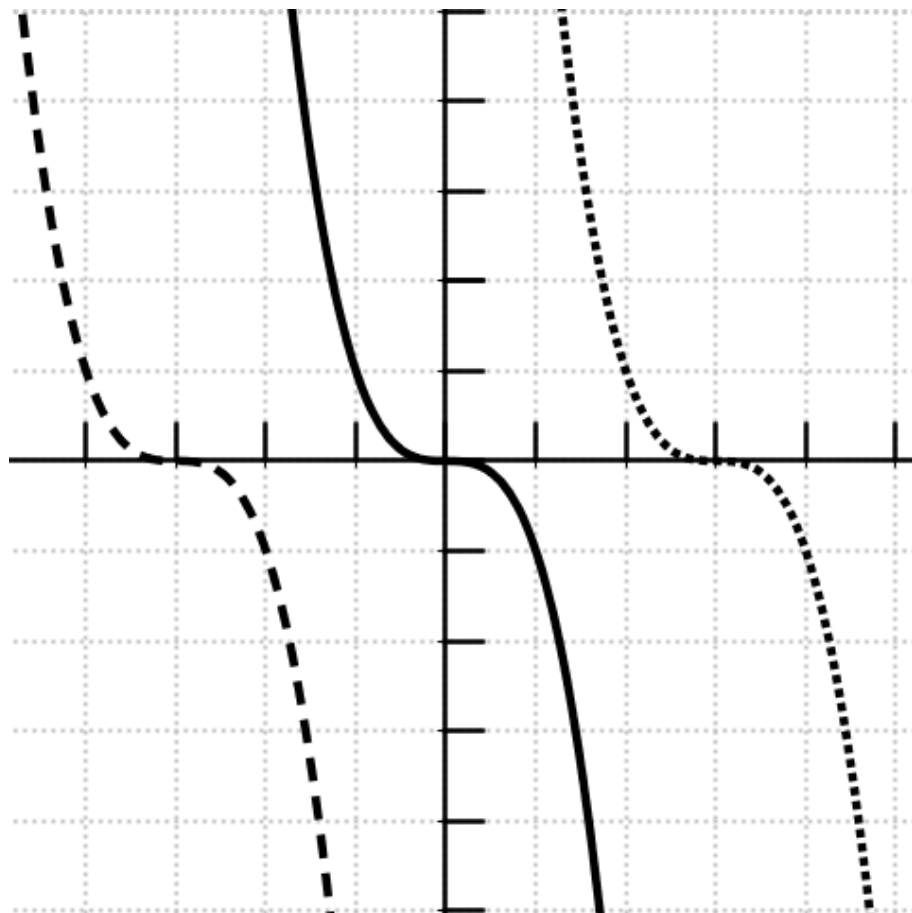
waagrecht verschieben

$a < 0, b = 0$ : ———

$a < 0, b > 0$  (nach links: - - - -

$a < 0, b < 0$  (n. rechts): .....

$$a = -1$$

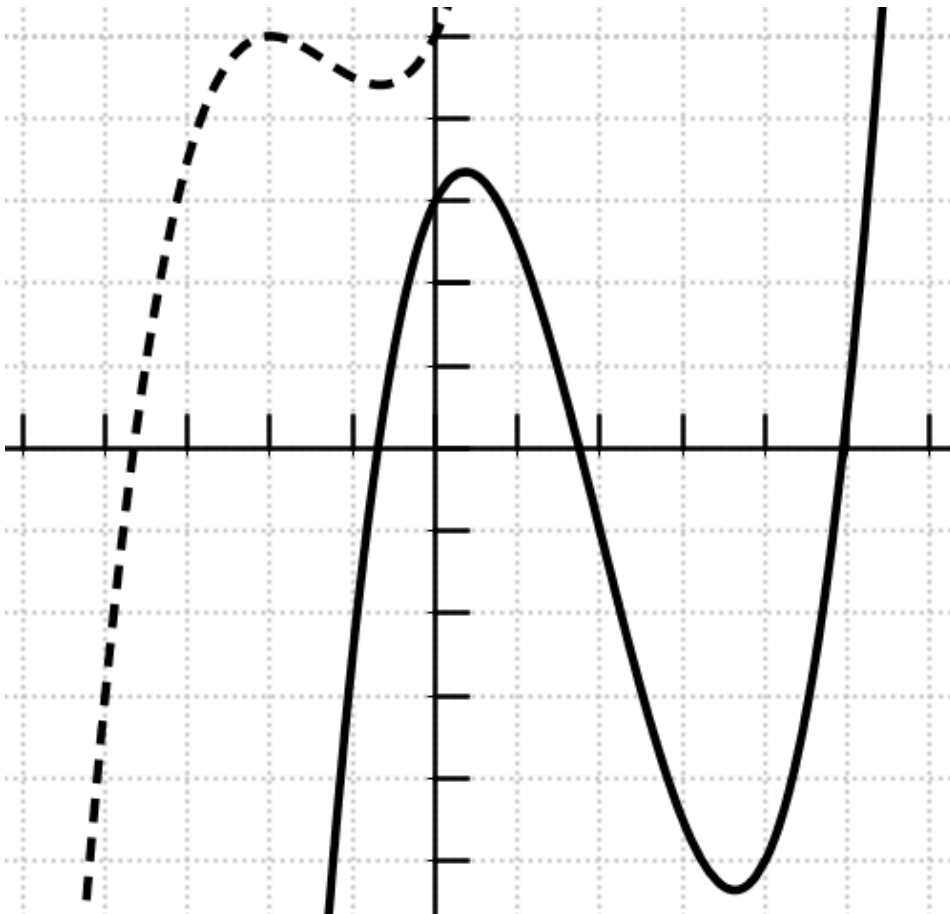


$$f_{G3.6}: a \cdot x^3 + b \cdot x^2 + c \cdot x + d$$

enthält Punkt  $(0|d)$

1 bis 3 Nullstellen

$a > 0$ : beginnt steigend

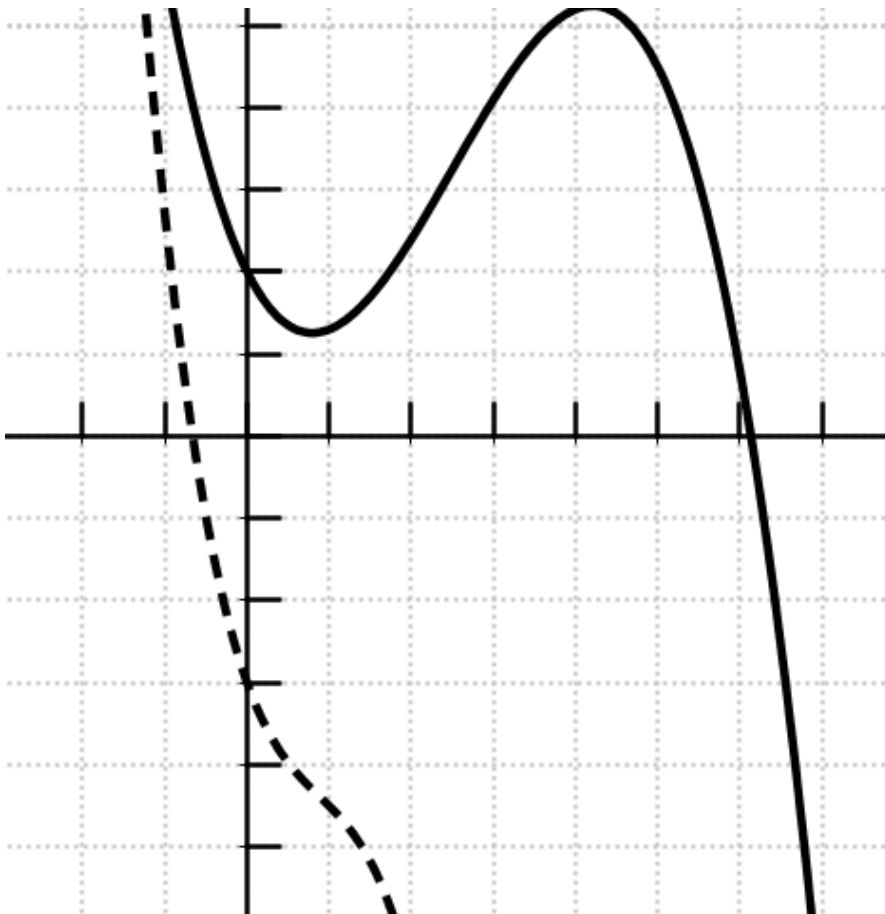


$$f_{G3.7}: a \cdot x^3 + b \cdot x^2 + c \cdot x + d$$

enthält Punkt  $(0|d)$

1 bis 3 Nullstellen

$a < 0$ : beginnt fallend



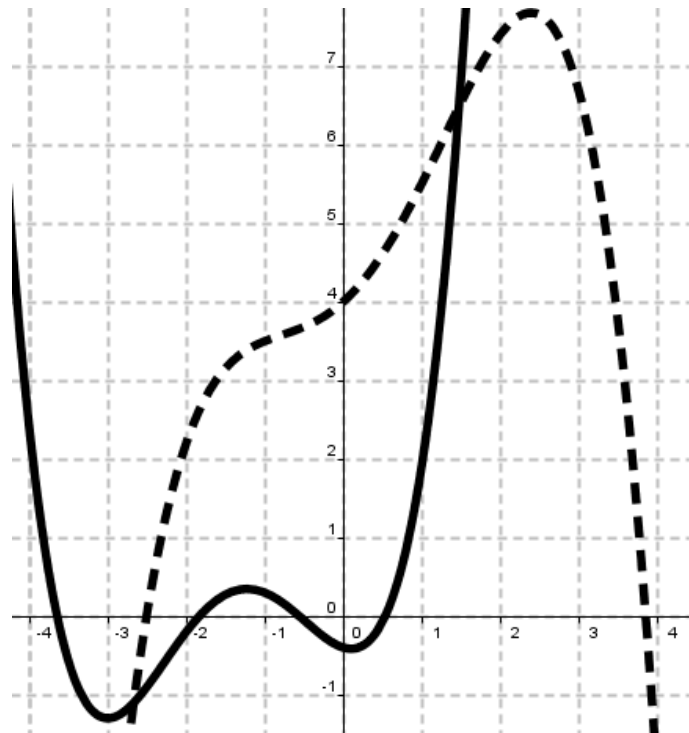
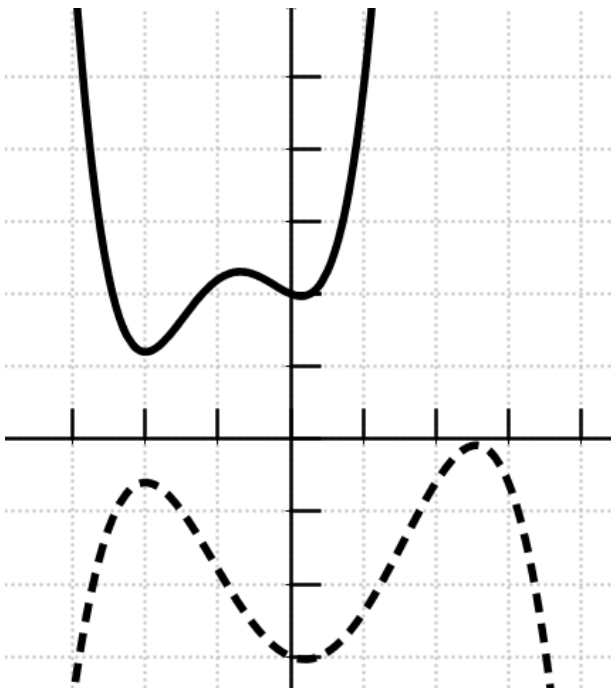
$$f\_G4.1: f(x) = a \cdot x^4 + b \cdot x^3 + c \cdot x^2 + d \cdot x + e$$

enthält Punkt  $(0|e)$ ,

0 bis 4 Nullstellen

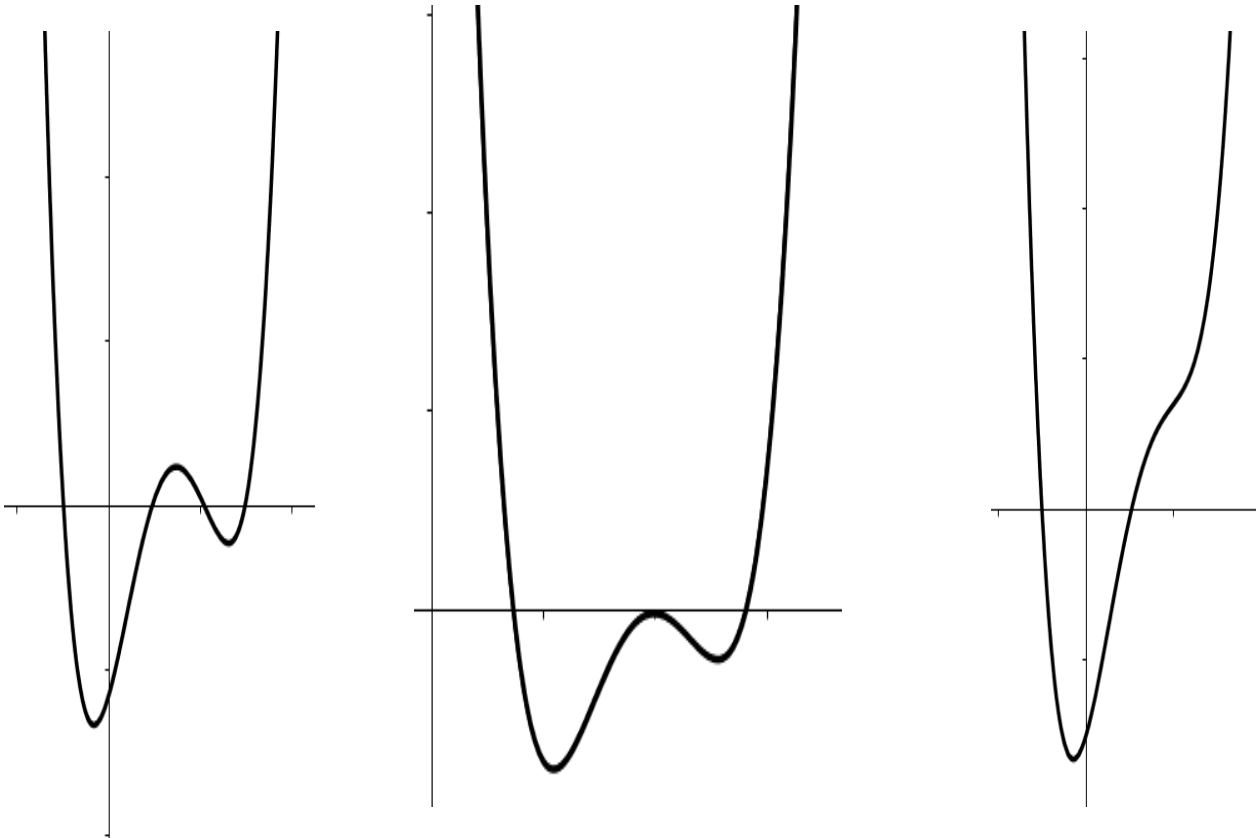
$a > 0$ : beginnt fallend

$a < 0$ : beginnt steigend



$$f\_G4.2: f(x) = a * x^4 + b * x^3 + c * x^2 + d * x + e$$

Doppel-S-Kurve  
verschiedenste  
Ausprägungen





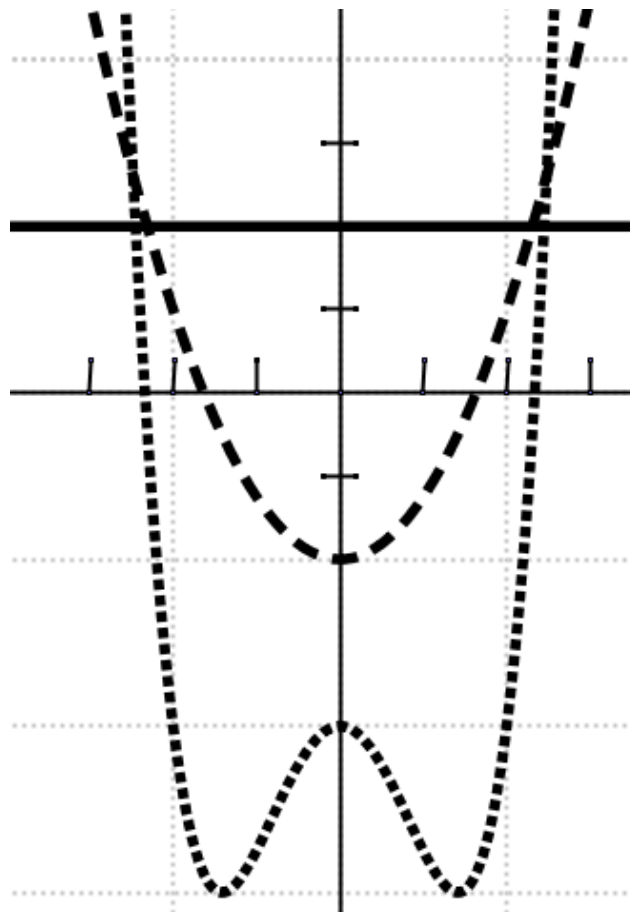
## **f\_g: Hochzahl gerade**

Symmetrisch zur  
senkrechten Achse,  $a \neq 0$

$$f(x) = a \cdot x^0 = a \quad \text{—————}$$

$$f(x) = a \cdot x^2 + b \quad \text{-----}$$

$$f(x) = a \cdot x^4 + b \cdot x^2 + c \quad \text{.....}$$



**f\_u: Hochz. ungerade**

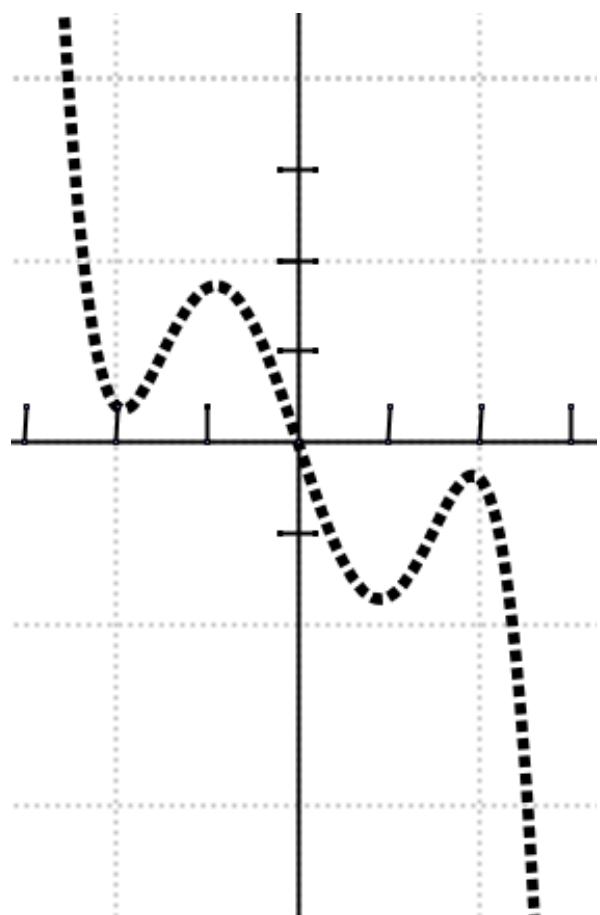
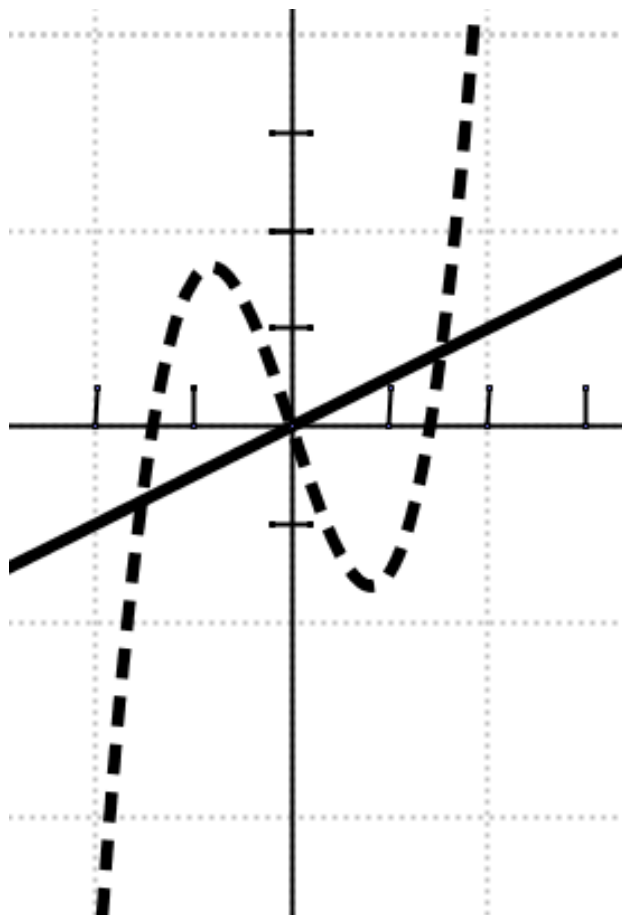
Symmetrisch zum

Ursprung,  $a \neq 0$ 

$$f(x) = a \cdot x \quad \text{—————}$$

$$f(x) = a \cdot x^3 + b \cdot x \quad \text{-----}$$

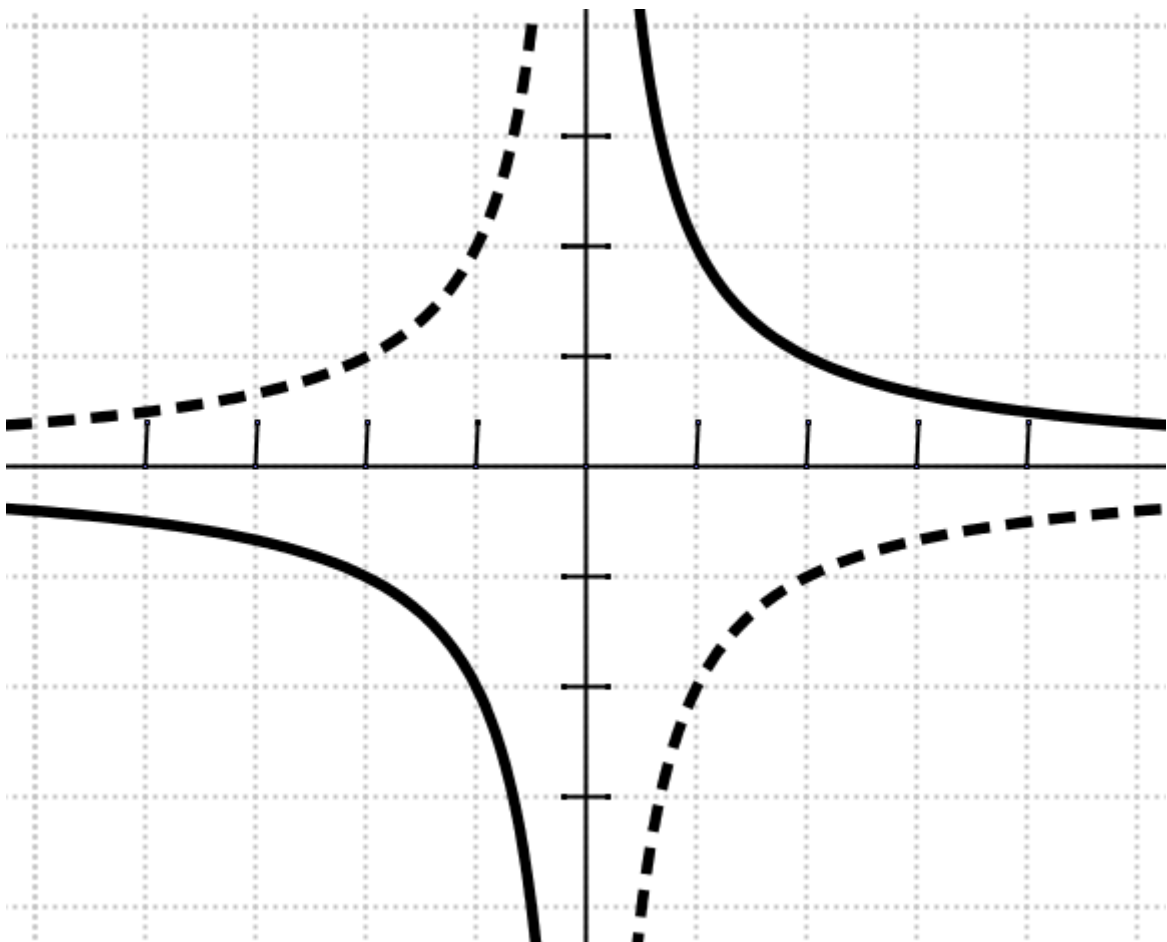
$$f(x) = a \cdot x^5 + b \cdot x^3 + c \cdot x \quad \text{.....}$$



## $f_{\text{gebr1.1}}: f(x) = a/x$

$a > 0$  mit  $(1|a)$  —————

$a < 0$  mit  $(-1|a)$  - - - - -



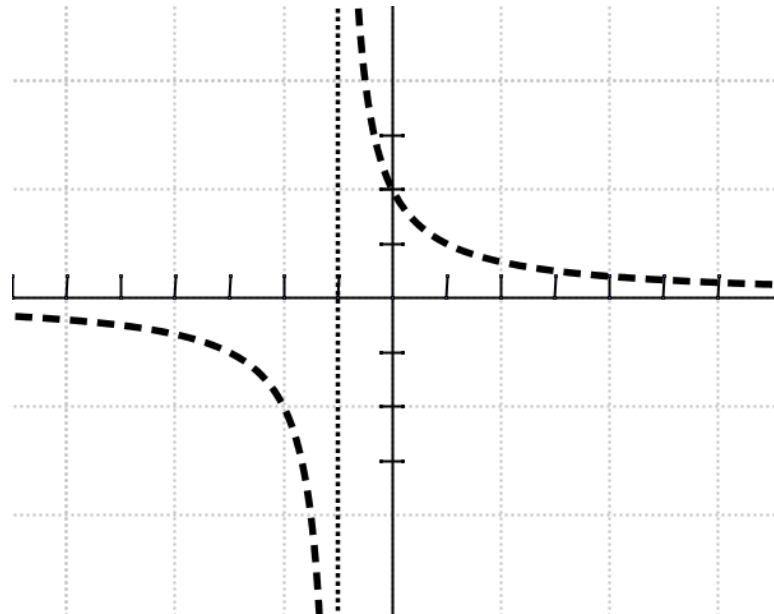
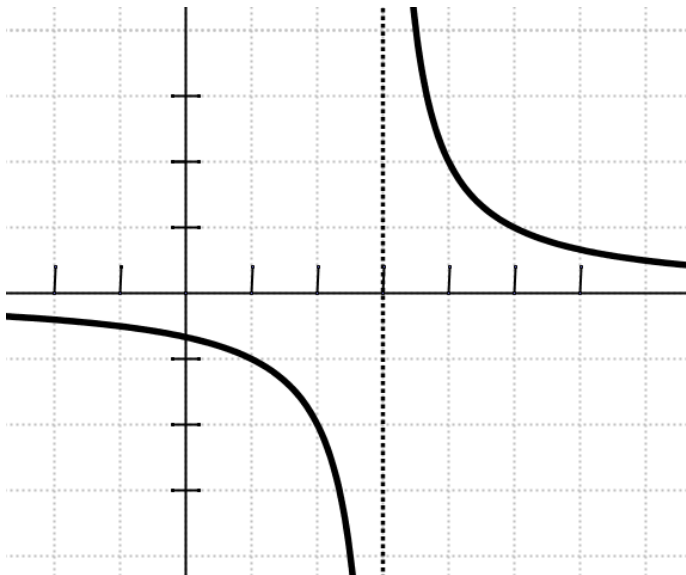
## f\_gebr1.2: $f(x) = a/(x + b)$

$a > 0, b < 0$

————

$a > 0, b > 0$

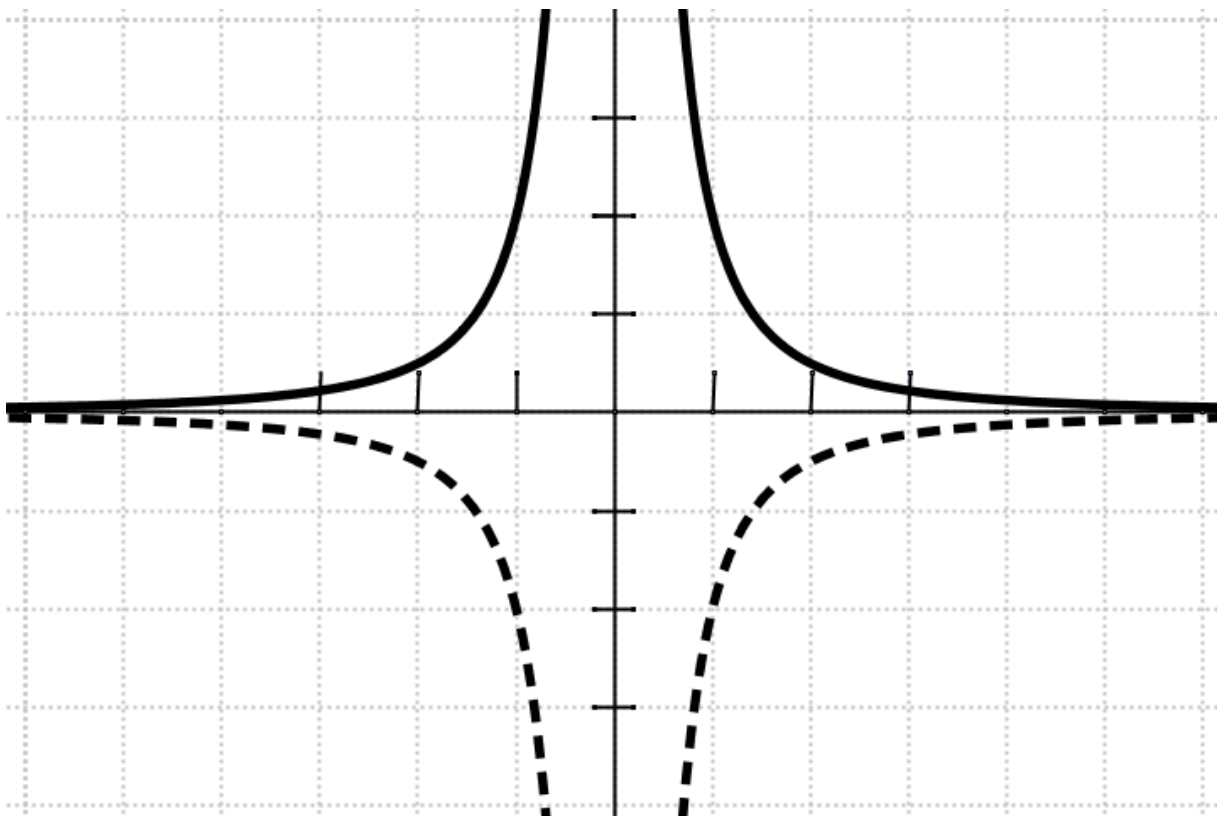
- - - - .



## f\_gebr2.1: $f(x) = a/x^2$

$a > 0$ : 

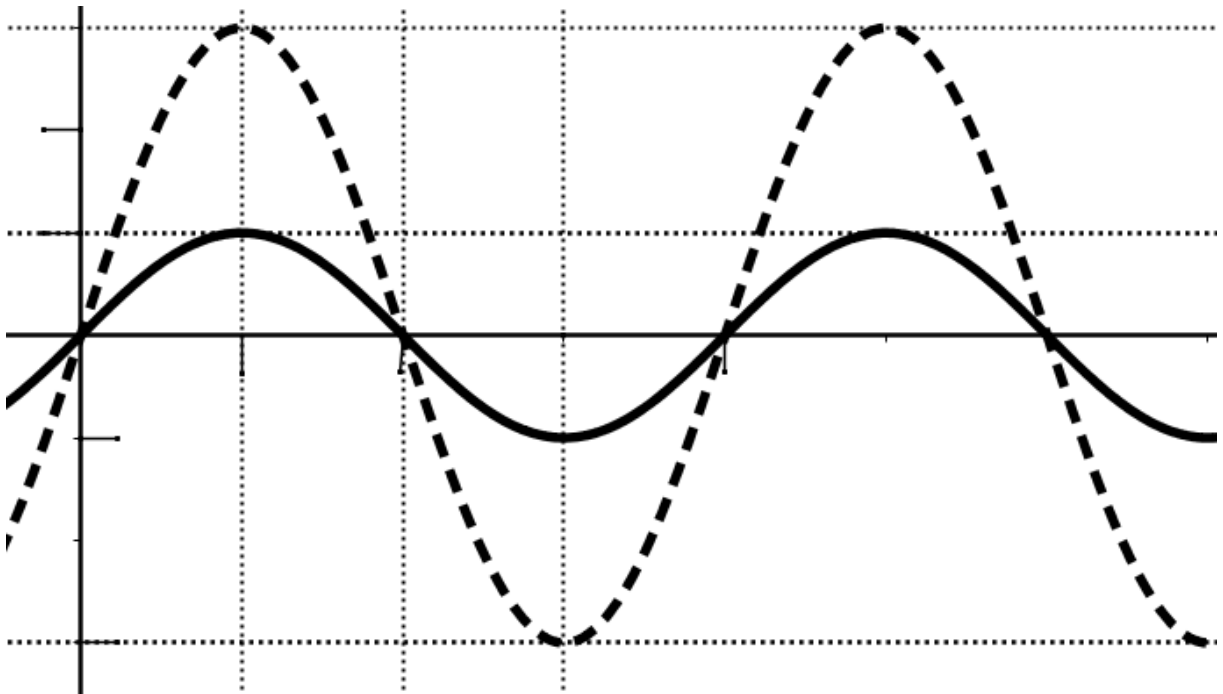
$a < 0$ : 



**f\_sin.1:  $f(x) = a \cdot \sin(x)$**

$a = 1$ : 

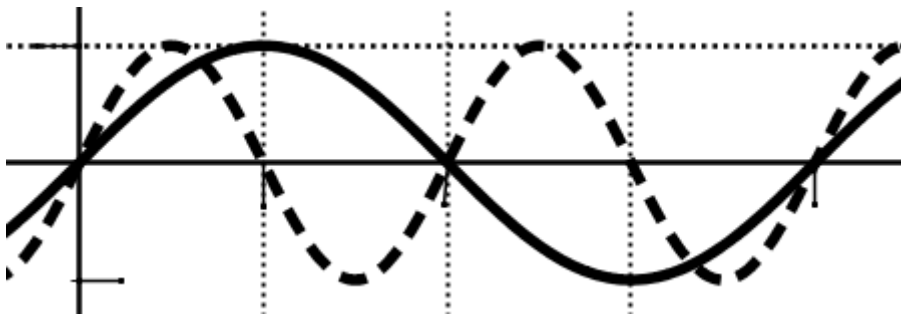
$a = 3$ : 



## f\_sin.2: $f(x) = \sin(b \cdot x)$

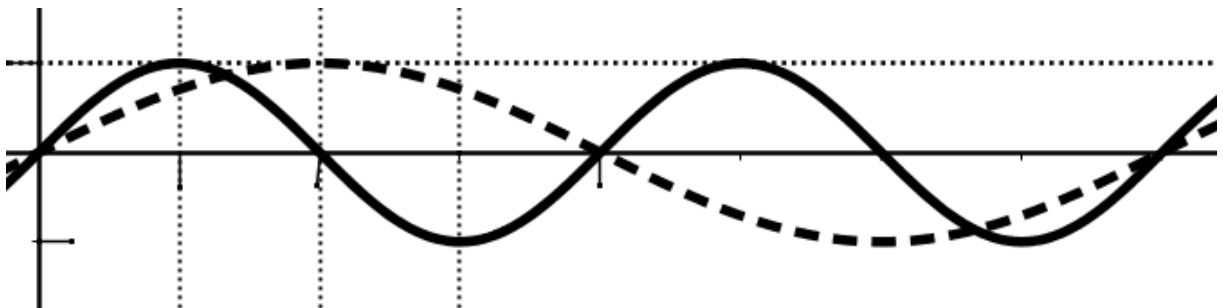
$b = 1$ : \_\_\_\_\_

$b = 2$ : - - - - -



$b = 1$ : \_\_\_\_\_

$b = 1/2$ : - - - - -



EK

$P(\cos(\alpha) | \sin(\alpha))$  •

