

Funktionen in 'R²

9. Schulstufe

Schwarzdruckkopiervorschläge mit großer Schrift
und starken Linien

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19.09.2019

Inhalt: Grafiken zu den Themen: einem x-Wert werden mehr als ein y-Wert zugeordnet, lineare Funktion, quadratische Funktion, Polynomfunktion 3. Grades, Polynomfunktion 4. Grades, gerade Funktion, ungerade Funktion, gebrochen rationale Funktion mit x im Nenner, gebrochen rationale Funktion mit x^2 im Nenner, Sinusfunktion und Einheitskreis

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31 EK

Abkürzungen

f_lin: lineare Funktion

f_q: quadratische Funktion

f_G3: Funktion 3. Grades

f_G4: Funktion 4. Grades

f_g: gerade Funktion

f_u: ungerade Funktion

f_gebr1: gebrochen

rationale Funktion Grad 1

f_gebr2: gebrochen

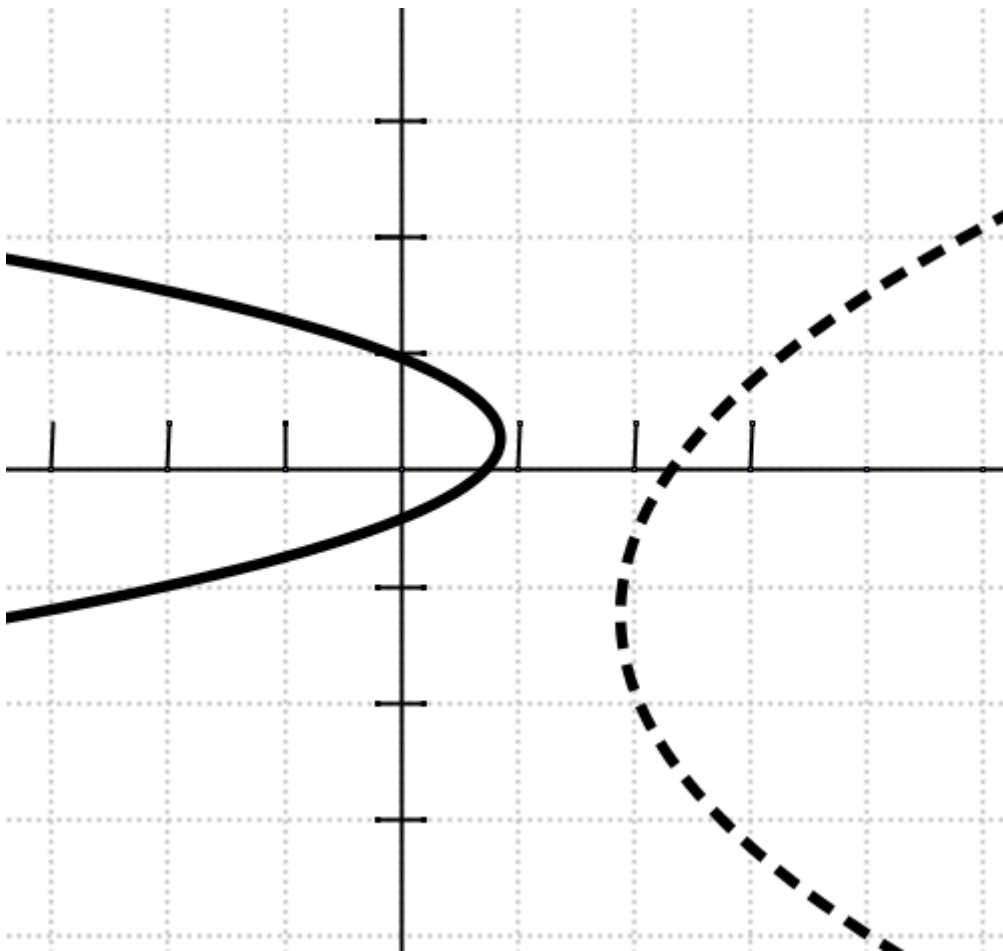
rationale Funktion Grad 2

f_sin: Winkelfunktion

EK: Einheitskreis

keine Funktionen

mehrere y-Werte zu einem
x-Wert



f_lin: $f(x) = k * x + d$

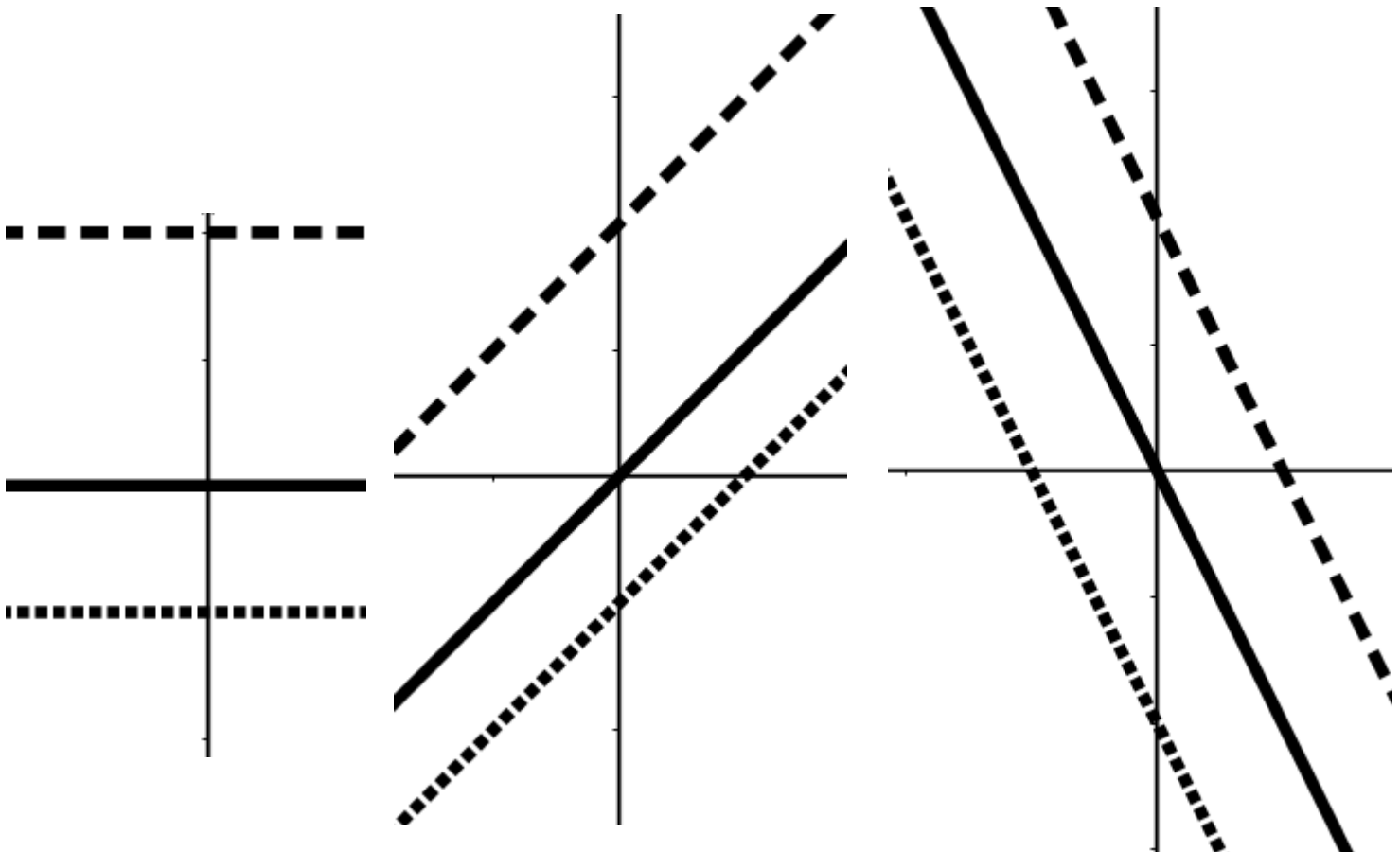
$$f(x) = k * x + d$$

$d = 0$: —————

$d > 0$: - - - - -

$d < 0$:
.....


$k = 0$ \parallel $k > 0$ \parallel $k < 0$




f_q .1: $f(x) = a * x^2$

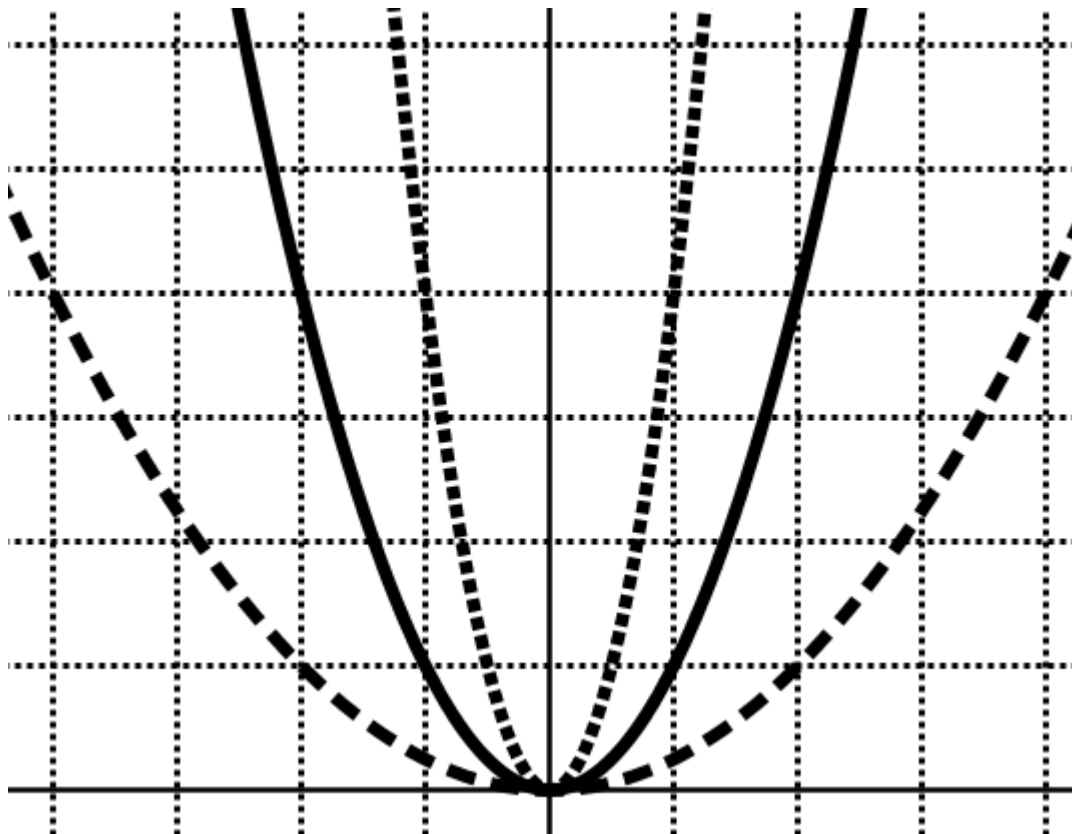
Parabel nach oben offen:

$a > 0$: 

$f(x) = x^2$; $a = +1$: 


$f(x) = 1/4 * x^2$; $a = 1/4$: 

$f(x) = 4 * x^2$; $a = 4$: 





f_q.2: $f(x) = a \cdot x^2$

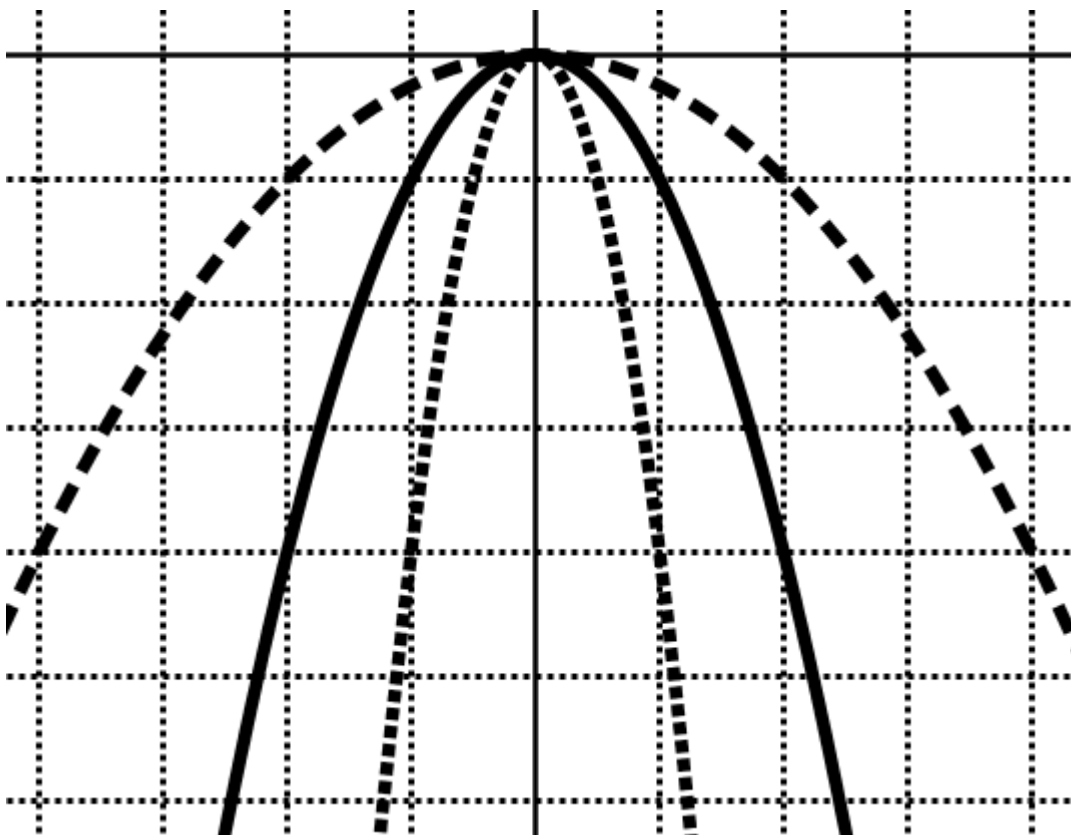
Parabel nach unten offen:

$a < 0$: 

$f(x) = -x^2$; $a = -1$: 

$f(x) = -1/4 \cdot x^2$; $a = -1/4$: 

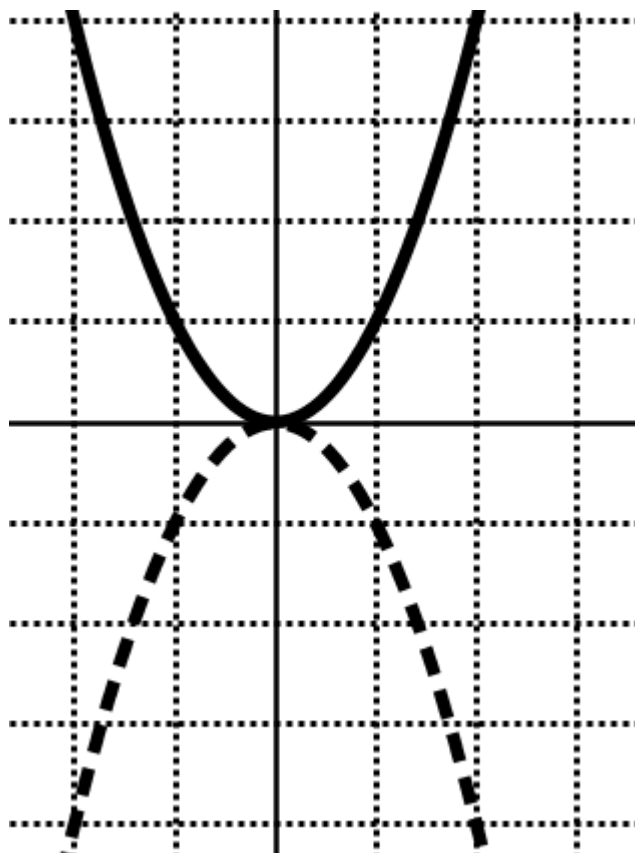
$f(x) = -4 \cdot x^2$; $a = -4$: 



f_q.3: $f(x) = a \cdot x^2$

Parabel spiegeln

$a = 1$: — || $a = -1$: - - - - -



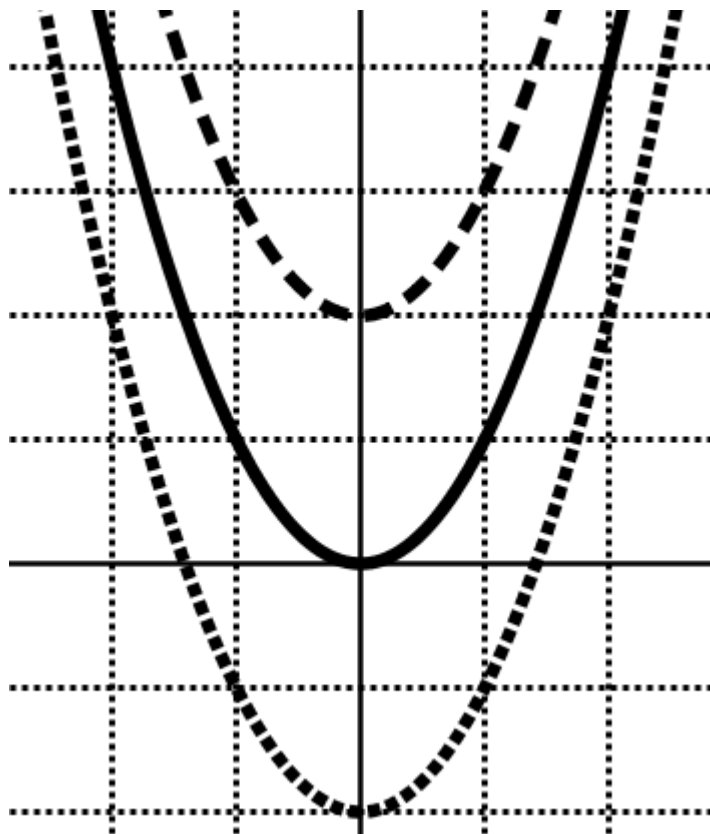
f_q.4: $f(x) = x^2 + c$

senkrecht verschieben

$c = 0$ ($f(x) = x^2$): —————

$c > 0$ (hinauf): - - - - -

$c < 0$ (hinunter):
.....



f_q.5: $f(x) = a \cdot x^2 + c$

$c = 0$: 

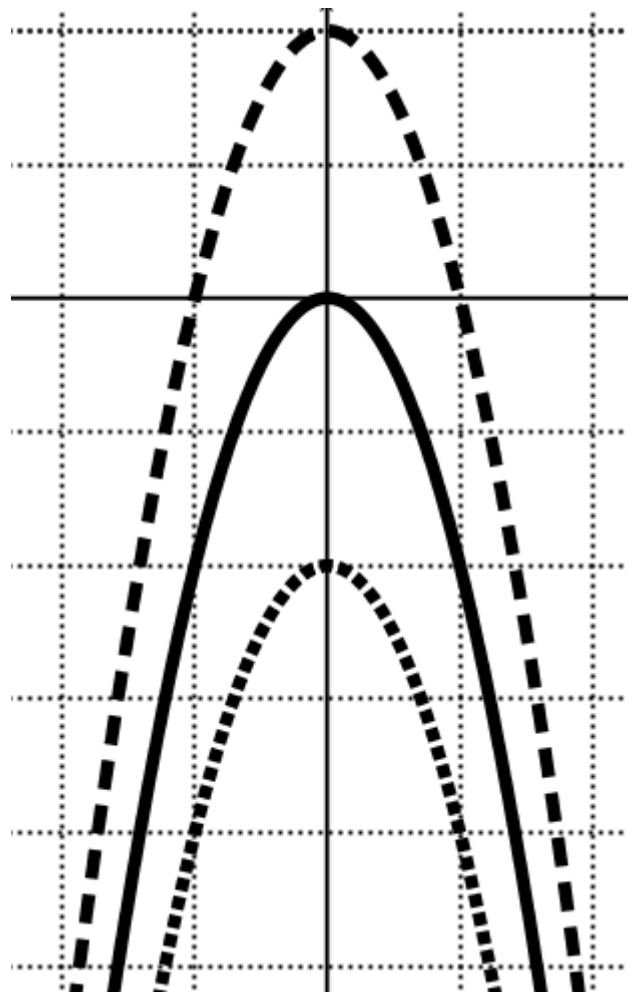
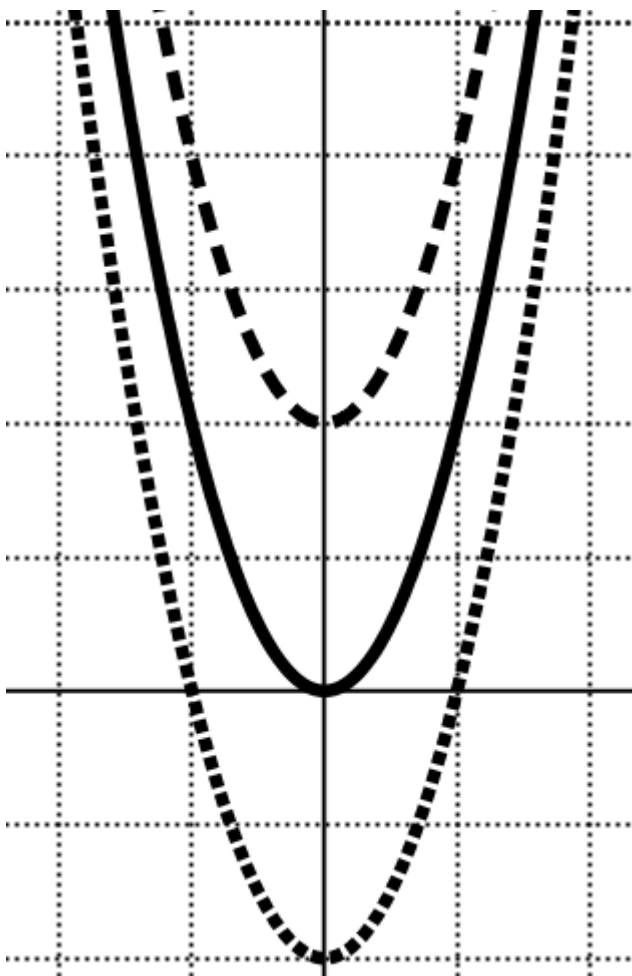
$c > 0$: 

$c < 0$: 

$a > 0$

||

$a < 0$



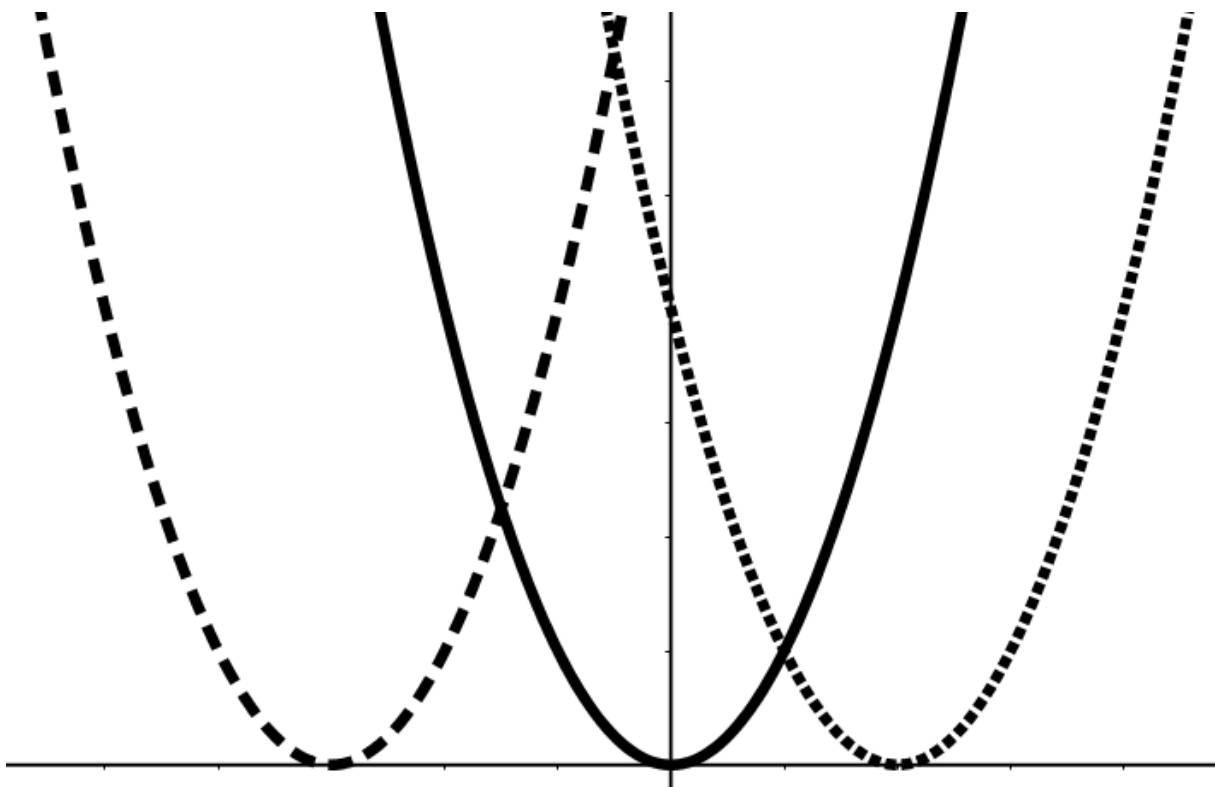
f_q.6: $f(x) = (x + b)^2$

waagrecht verschieben

$b = 0$ ($f(x) = x^2$): —————

$b > 0$ (nach links): - - - - -

$b < 0$ (nach rechts):

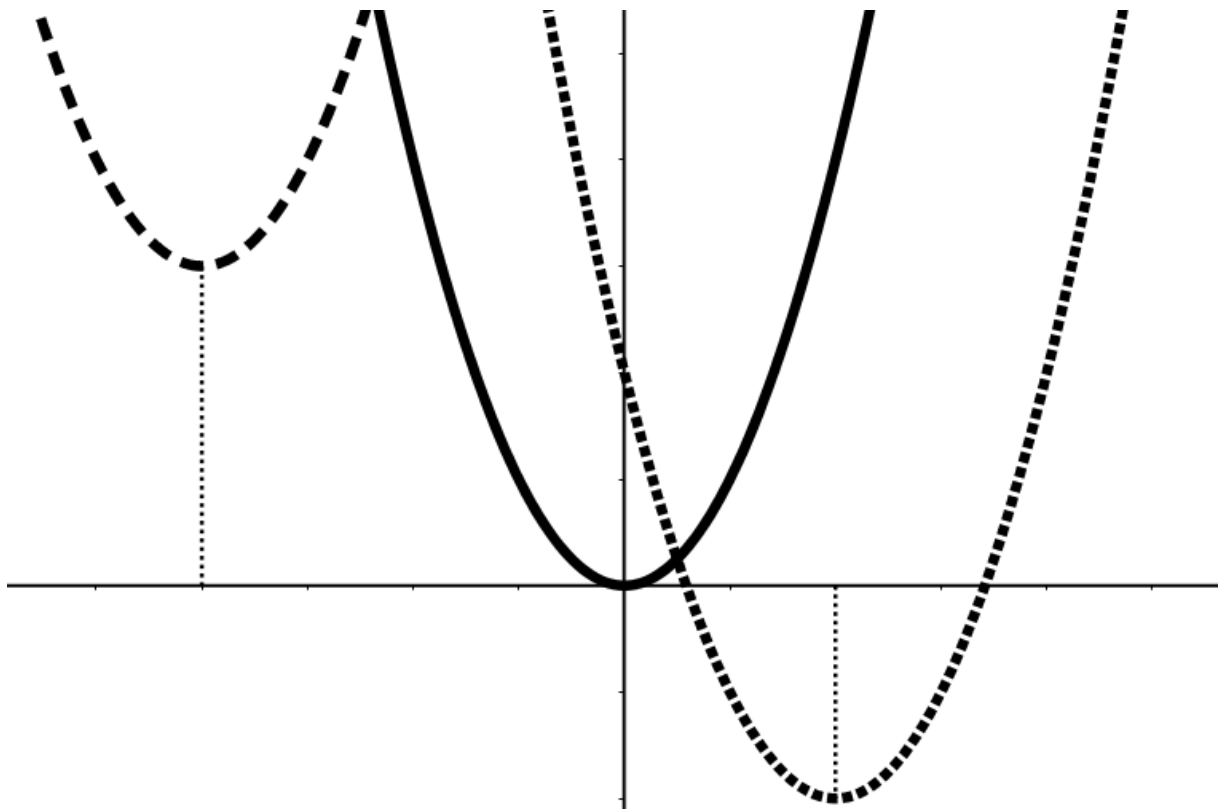


f_q.7: $f(x) = (x + b)^2 + c$

$b = 0, c = 0$ ($f(x) = x^2$): ———

$b > 0, c > 0$ (li, hinauf): - - - -

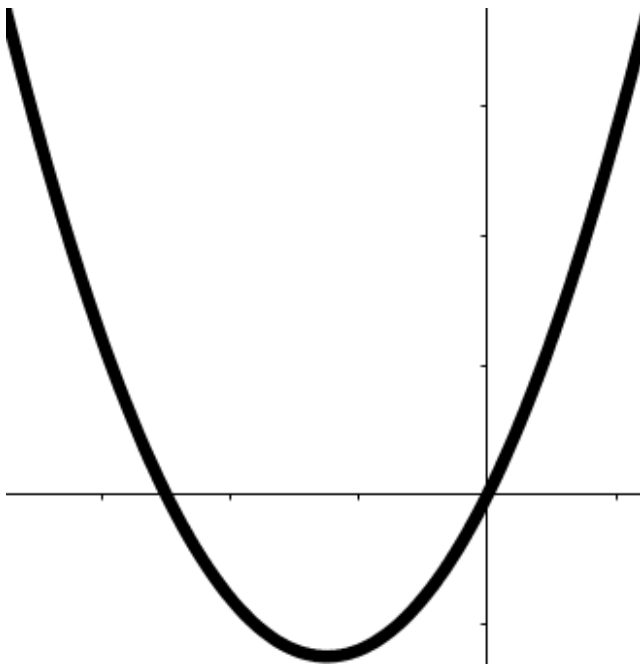
$b < 0, c < 0$ (re, hinunter): ······



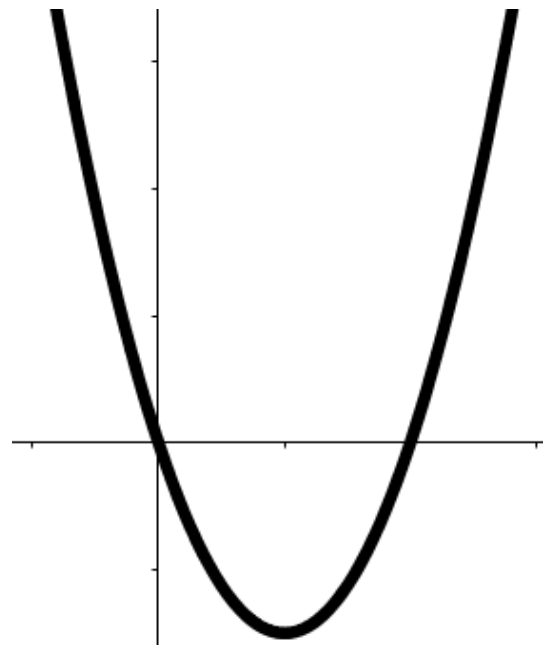
f_q.8: $f(x) = a \cdot x^2 + b \cdot x$

enthält Ursprung (0|0)

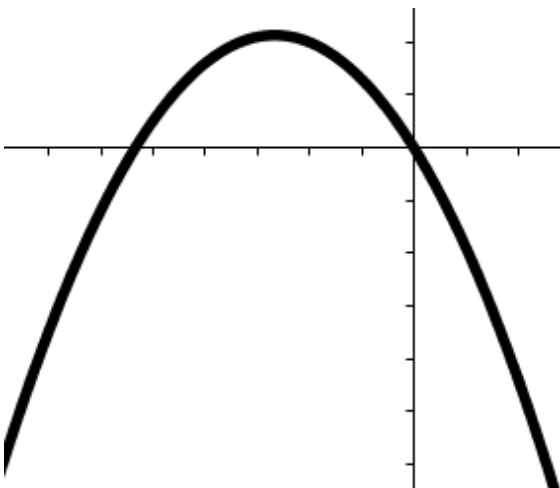
$a > 0, b > 0$



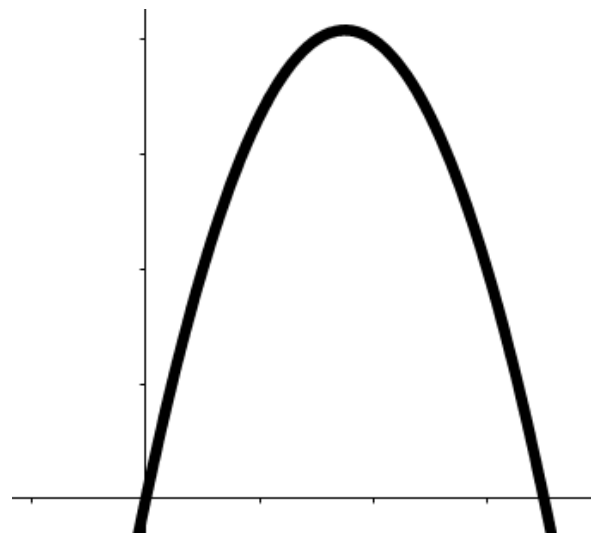
$a > 0, b < 0$



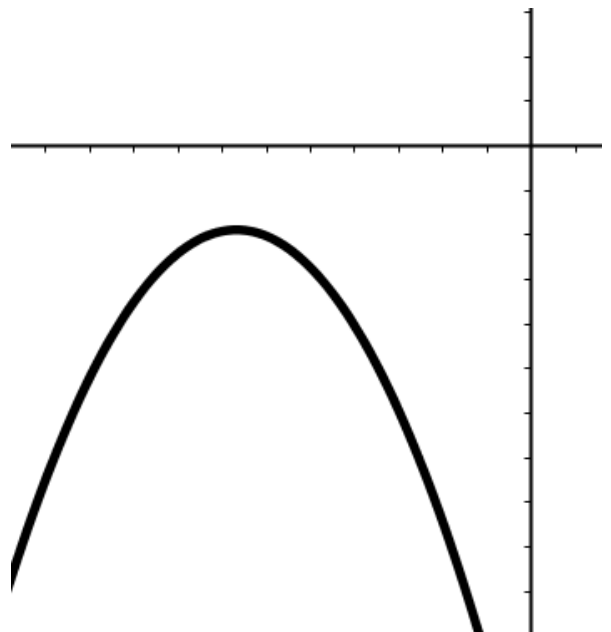
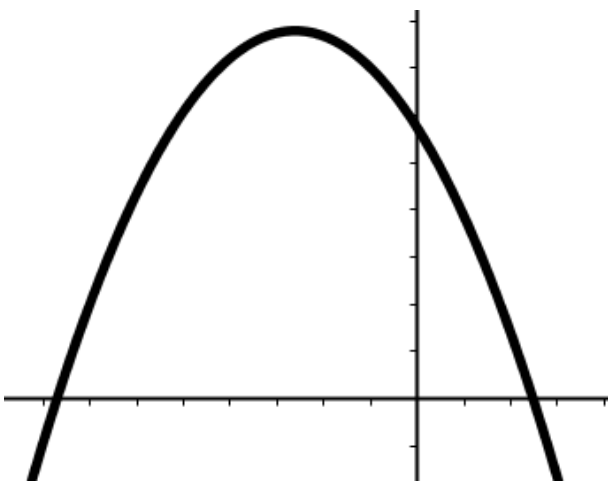
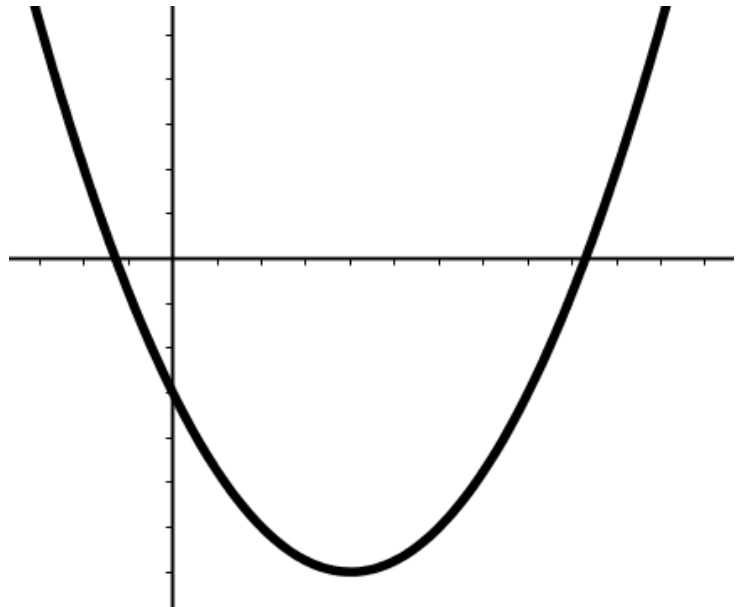
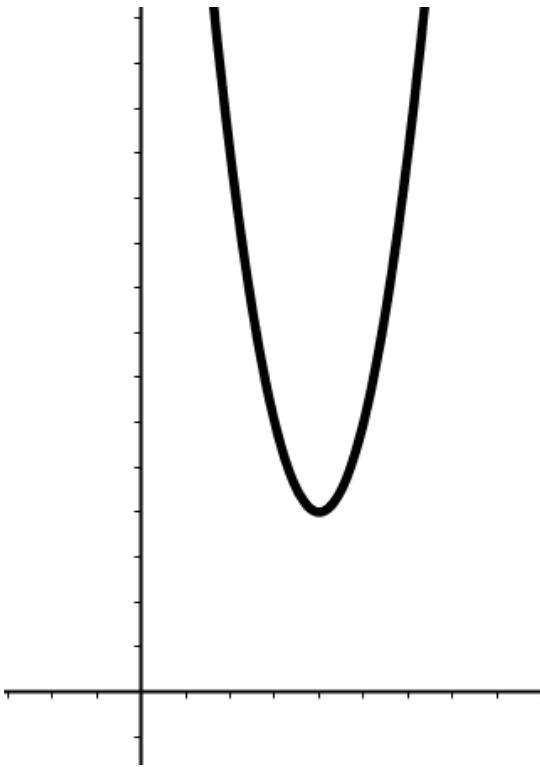
$a < 0, b > 0$



$a < 0, b < 0$



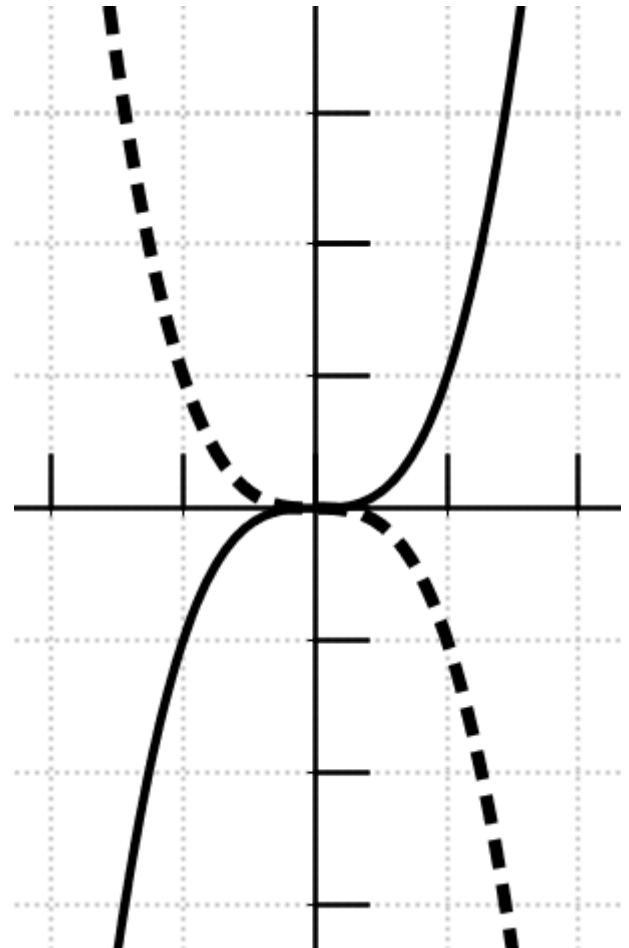
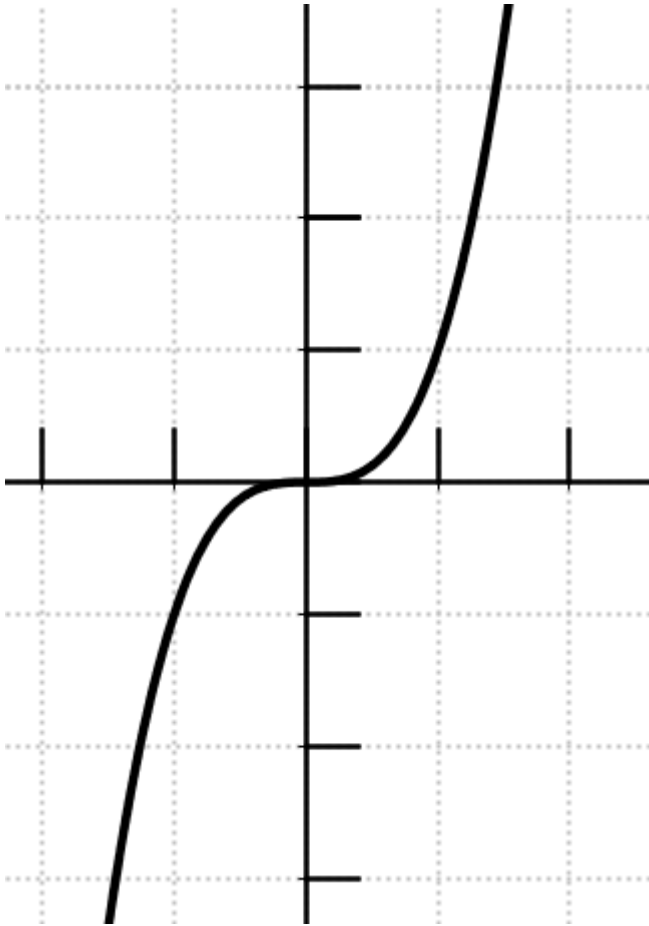
f_q.9: $f: a \cdot x^2 + b \cdot x + c$



f_G3.1: $f(x) = a * x^3$

$a = 1$ ($f(x) = x^3$): ———

$a = -1$ ($f(x) = -x^3$): - - - -



$$f_{G3.2}: f(x) = a \cdot x^3 + c$$

senkrecht verschieben

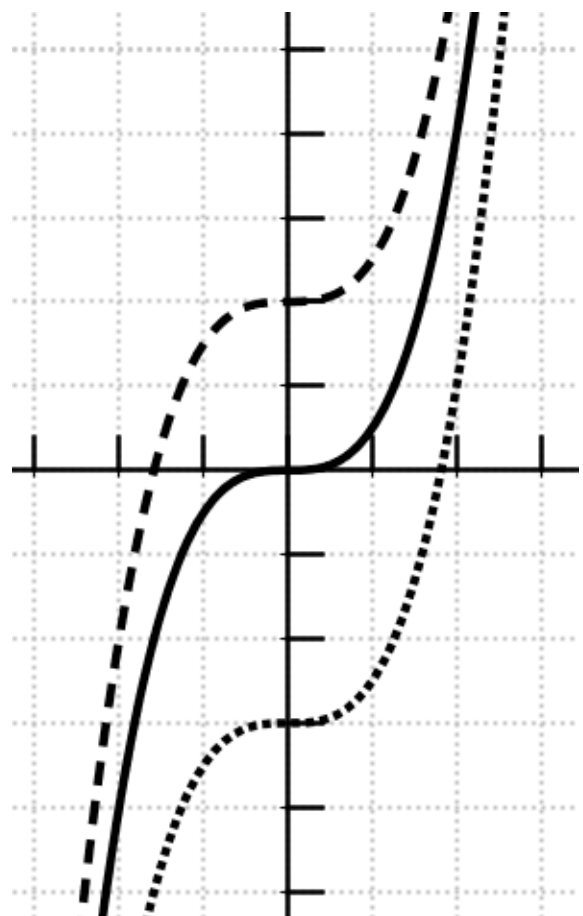
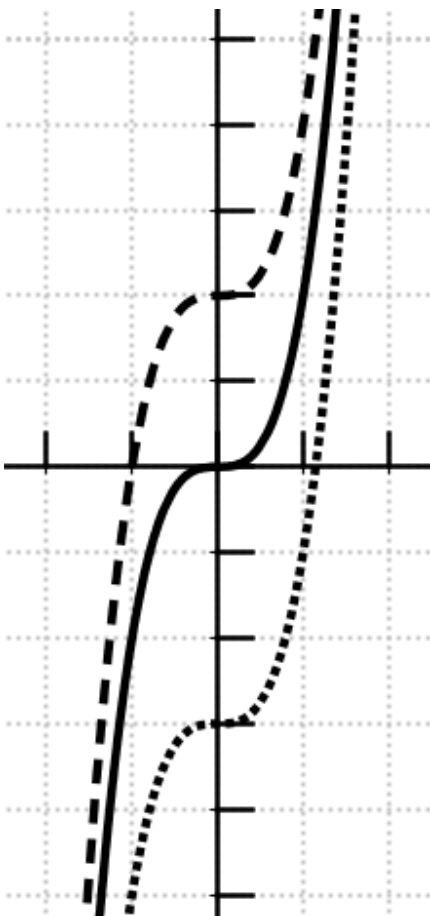
$a > 0, c = 0$: ———

$a > 0, c > 0$ (hinauf): - - - -

$a > 0, c < 0$ (hinunter):

$a=2$

$a = 0,5$



f_G3.3: $f(x) = a \cdot x^3 + c$

senkrecht verschieben

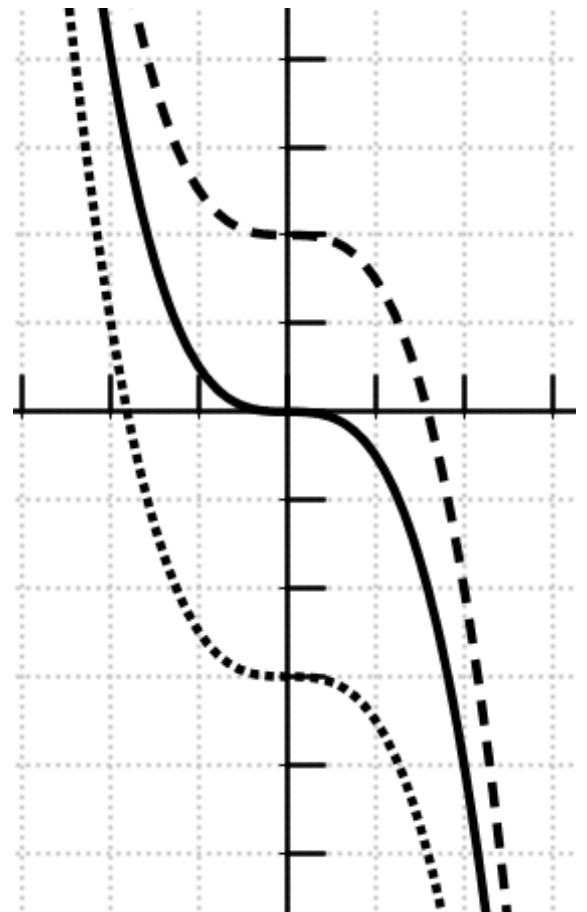
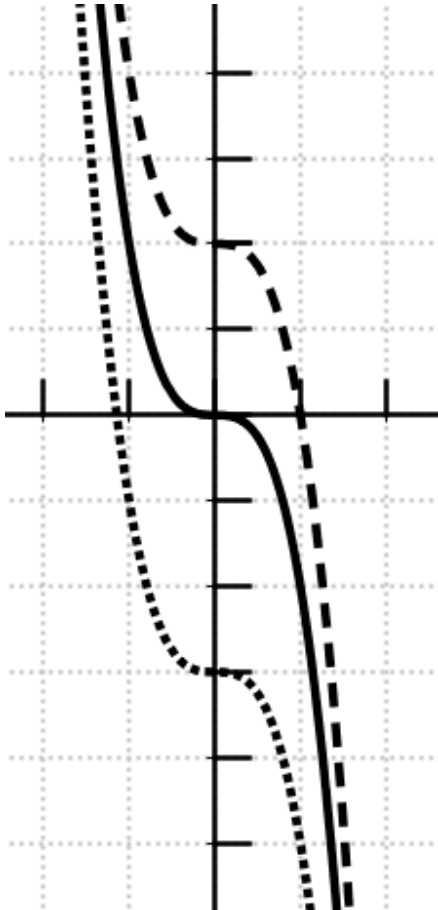
$a < 0, c = 0$: ———

$a < 0, c > 0$ (hinauf): - - - -

$a < 0, c < 0$ (hinunter):

$a = -2$

$a = -0,5$



$$f_G3.4: f(x) = (x + b)^3$$

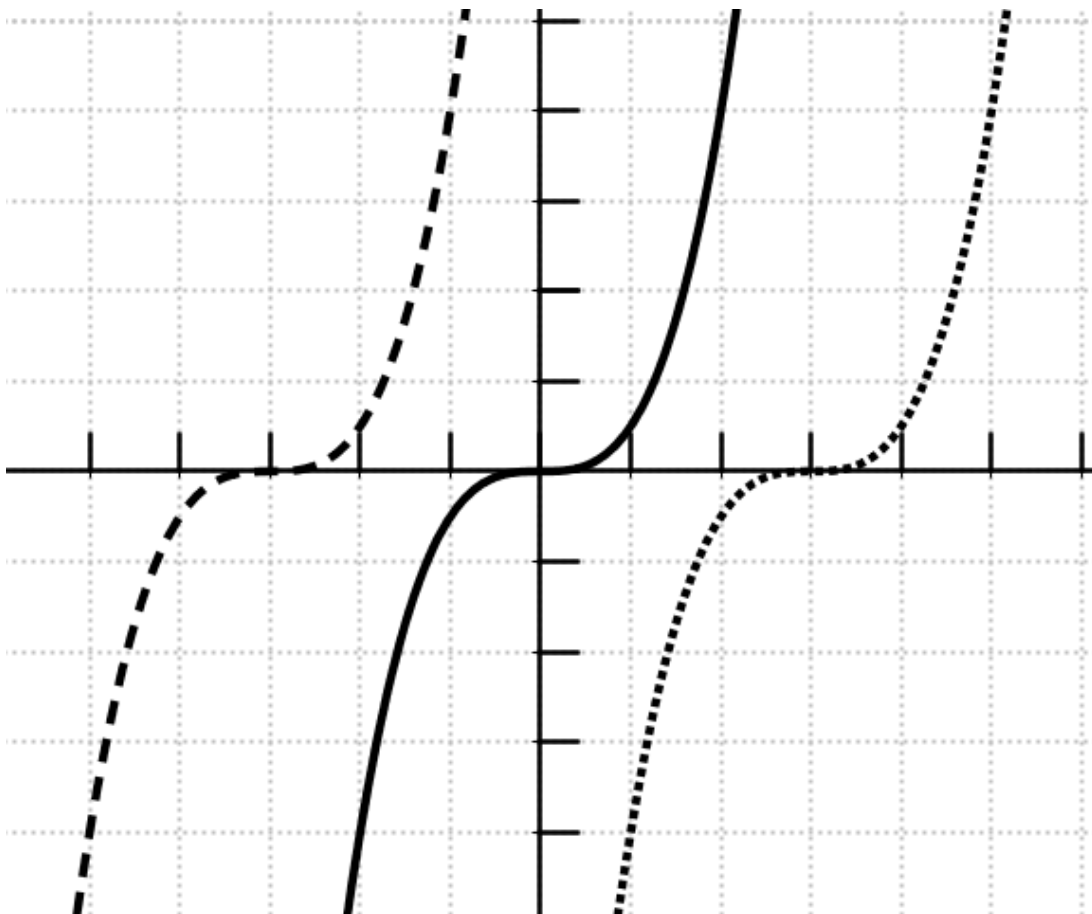
waagrecht verschieben

$a > 0, b = 0$: ———

$a > 0, b > 0$ (nach links): - - - -

$a > 0, b < 0$ (n. rechts):

$a = 0,5$



f_G3.5: $f(x) = (x + b)^3$

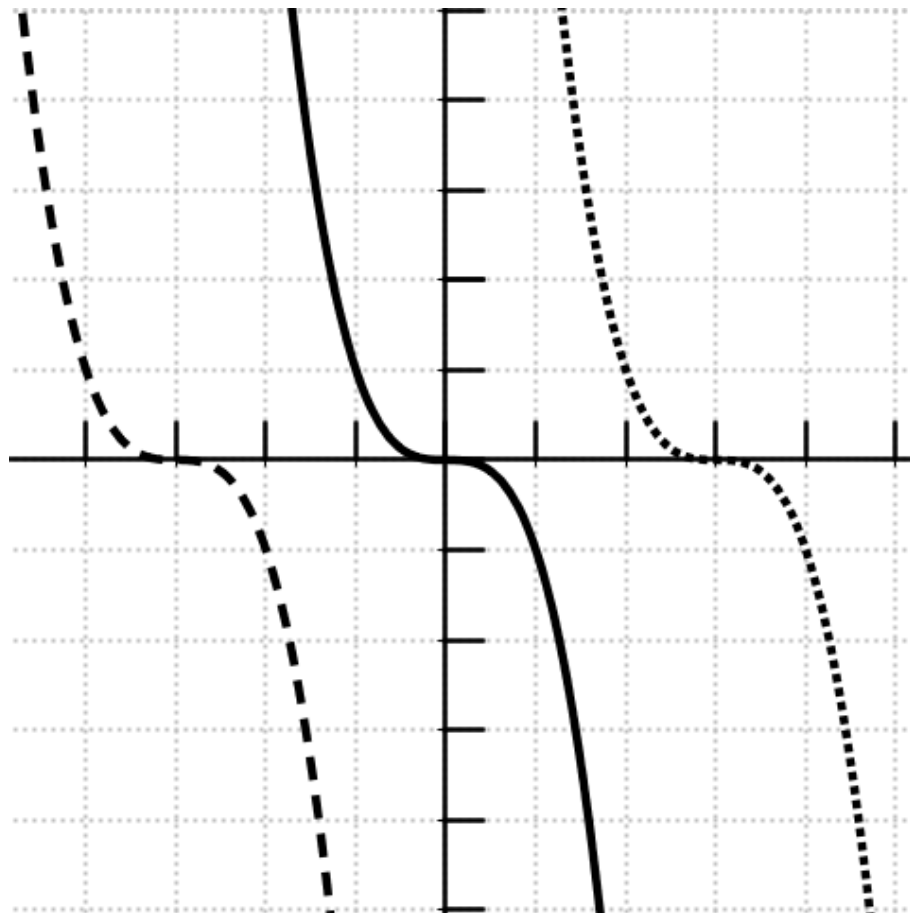
waagrecht verschieben

$a < 0, b = 0$: ———

$a < 0, b > 0$ (nach links): - - - -

$a < 0, b < 0$ (n. rechts):

$a = -1$

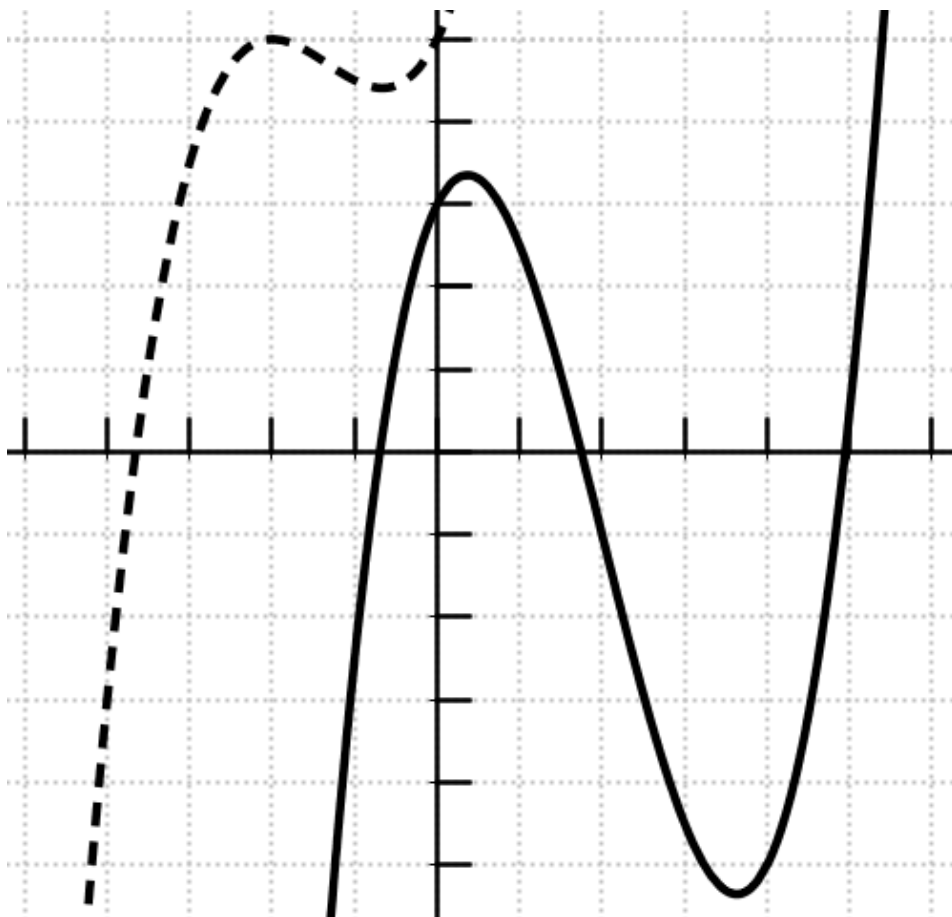


$$f_{\text{G3.6}}: a \cdot x^3 + b \cdot x^2 + c \cdot x + d$$

enthält Punkt $(0|d)$

1 bis 3 Nullstellen

$a > 0$: beginnt steigend

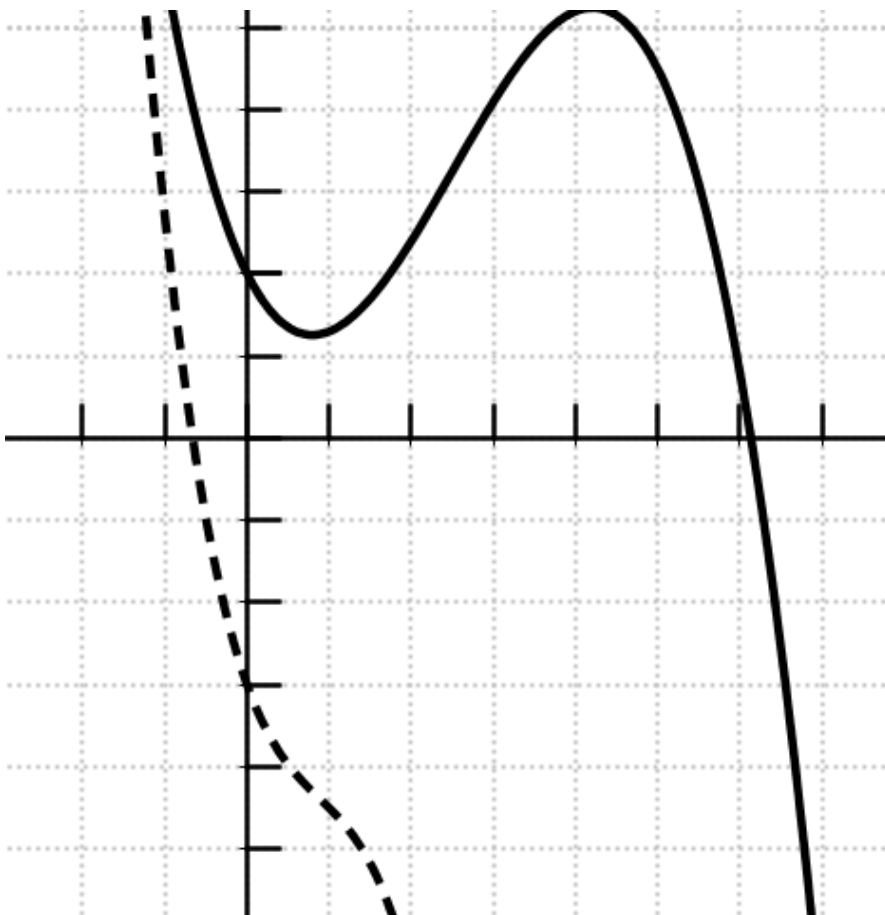


$$f_{\text{G3.7}}: a \cdot x^3 + b \cdot x^2 + c \cdot x + d$$

enthält Punkt $(0|d)$

1 bis 3 Nullstellen

$a < 0$: beginnt fallend



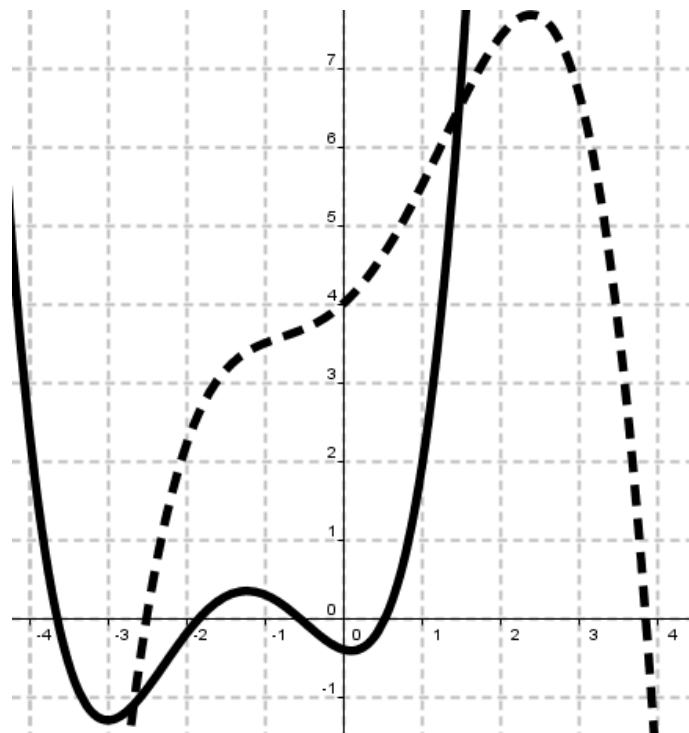
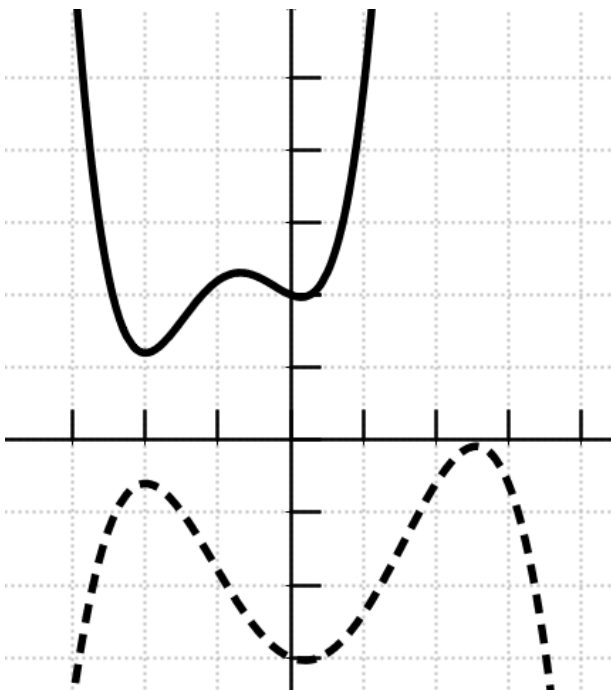
$$f_{G4.1}: f(x) = a \cdot x^4 + b \cdot x^3 + c \cdot x^2 + d \cdot x + e$$

enthält Punkt $(0|e)$,

0 bis 4 Nullstellen

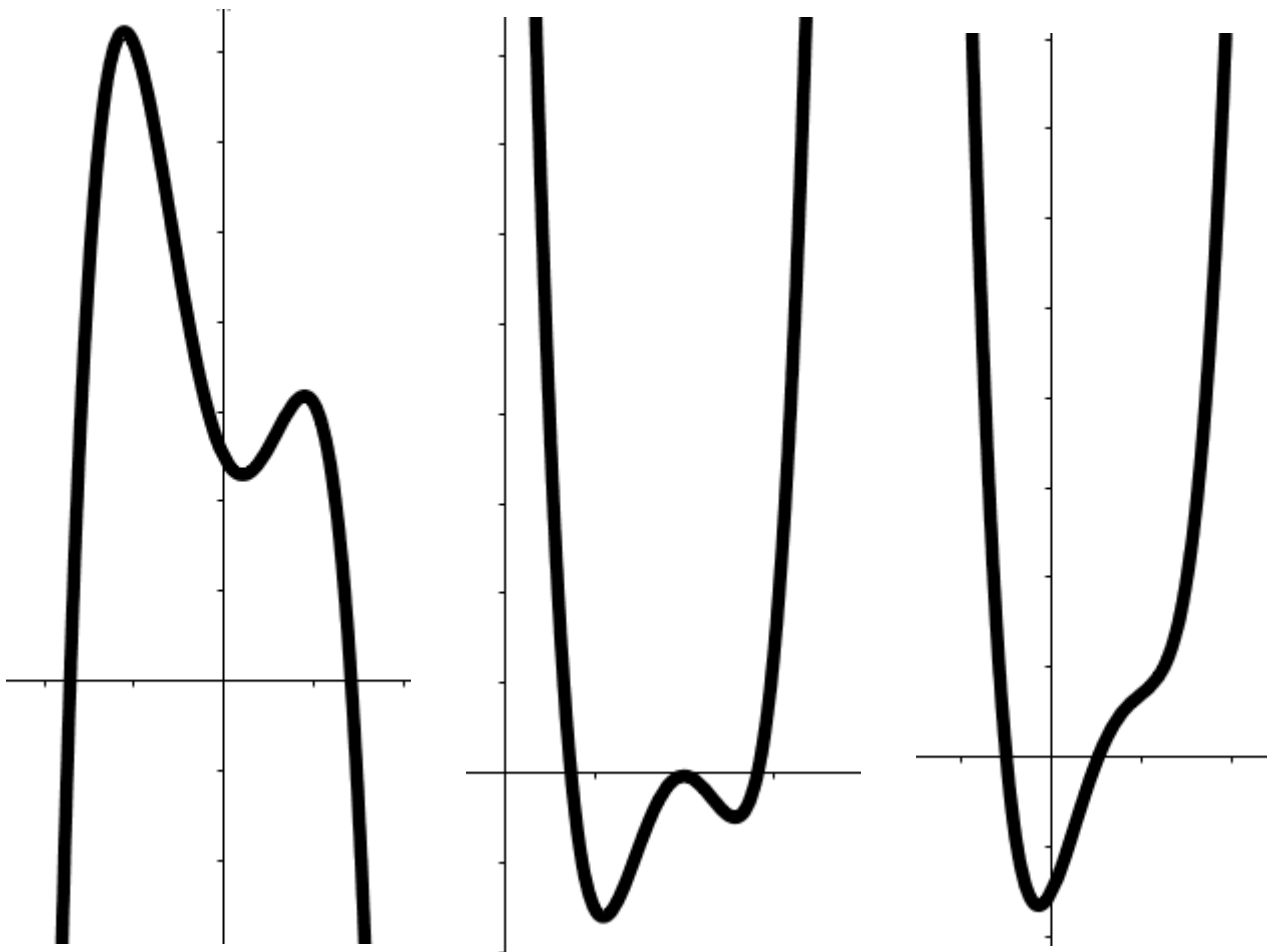
$a > 0$: beginnt fallend

$a < 0$: beginnt steigend



$$f_{\text{G4.2}}: f(x) = a \cdot x^4 + b \cdot x^3 + c \cdot x^2 + d \cdot x + e$$

Doppel-S-Kurve
verschiedenste
Ausprägungen



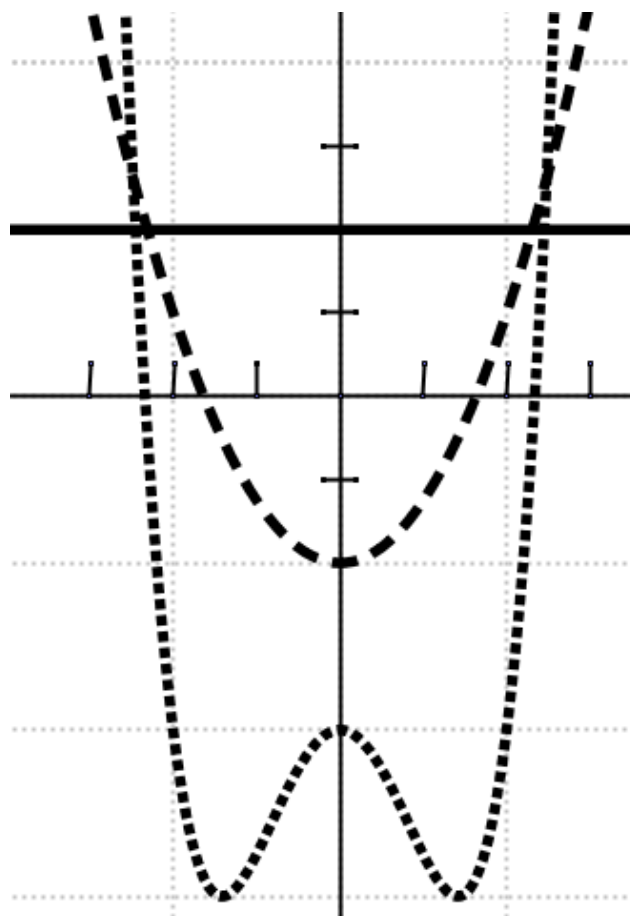
f_g : Hochzahl gerade

Symmetrisch zur
senkrechten Achse, $a \neq 0$

$$f(x) = a \cdot x^0 = a \quad \text{—————}$$

$$f(x) = a \cdot x^2 + b \quad \text{-----}$$

$$f(x) = a \cdot x^4 + b \cdot x^2 + c \quad \text{.....}$$



f_u: Hochz. ungerade

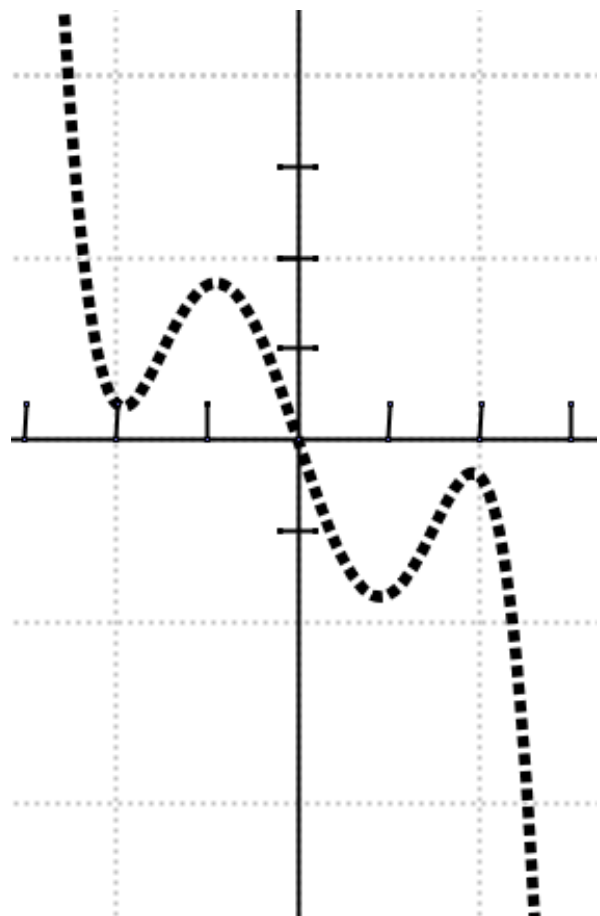
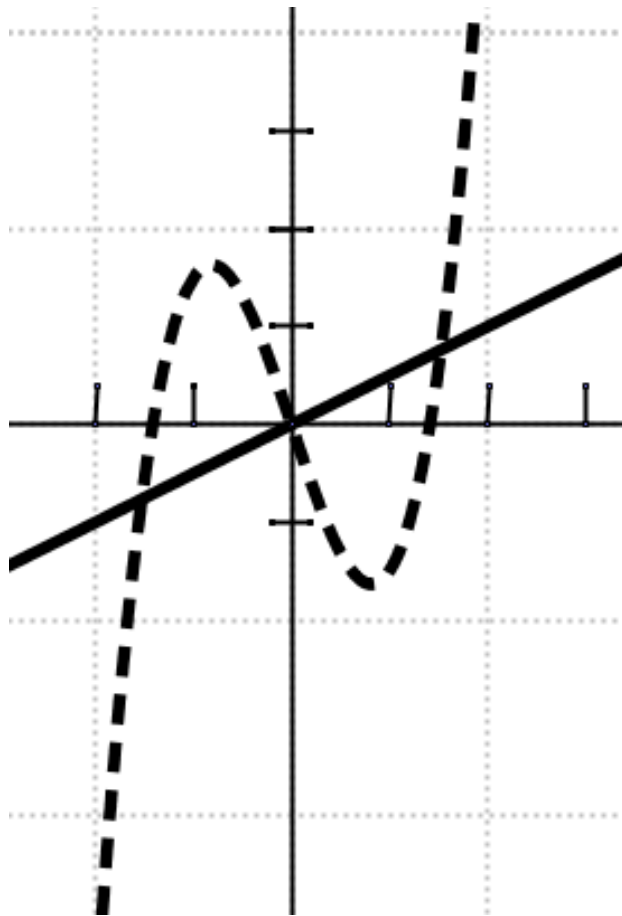
Symmetrisch zum

Ursprung, $a \neq 0$

$$f(x) = a \cdot x \quad \text{—————}$$

$$f(x) = a \cdot x^3 + b \cdot x \quad \text{-----}$$

$$f(x) = a \cdot x^5 + b \cdot x^3 + c \cdot x \quad \text{.....}$$



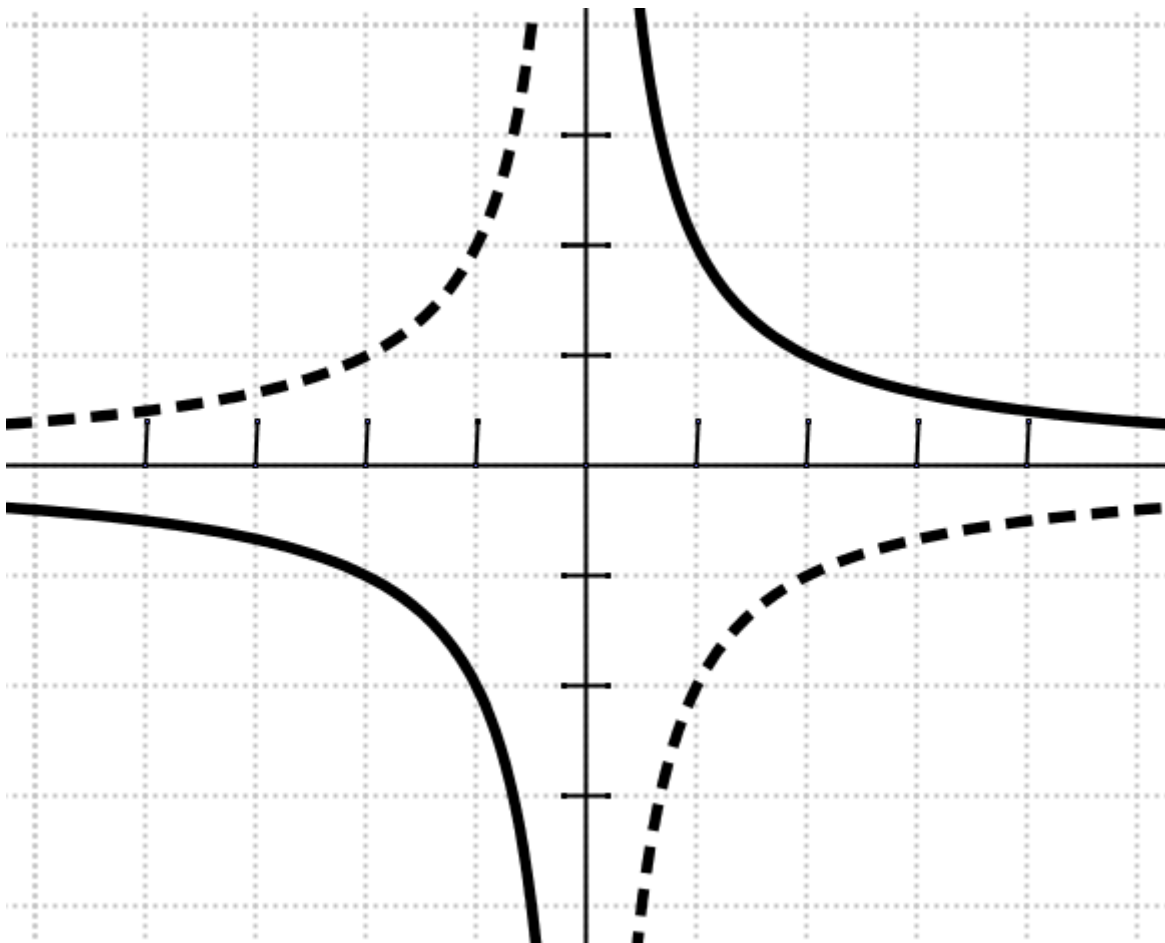
$f_{\text{gebr1.1}}: f(x) = a/x$

$a > 0$ mit $(1|a)$

————

$a < 0$ mit $(-1|a)$

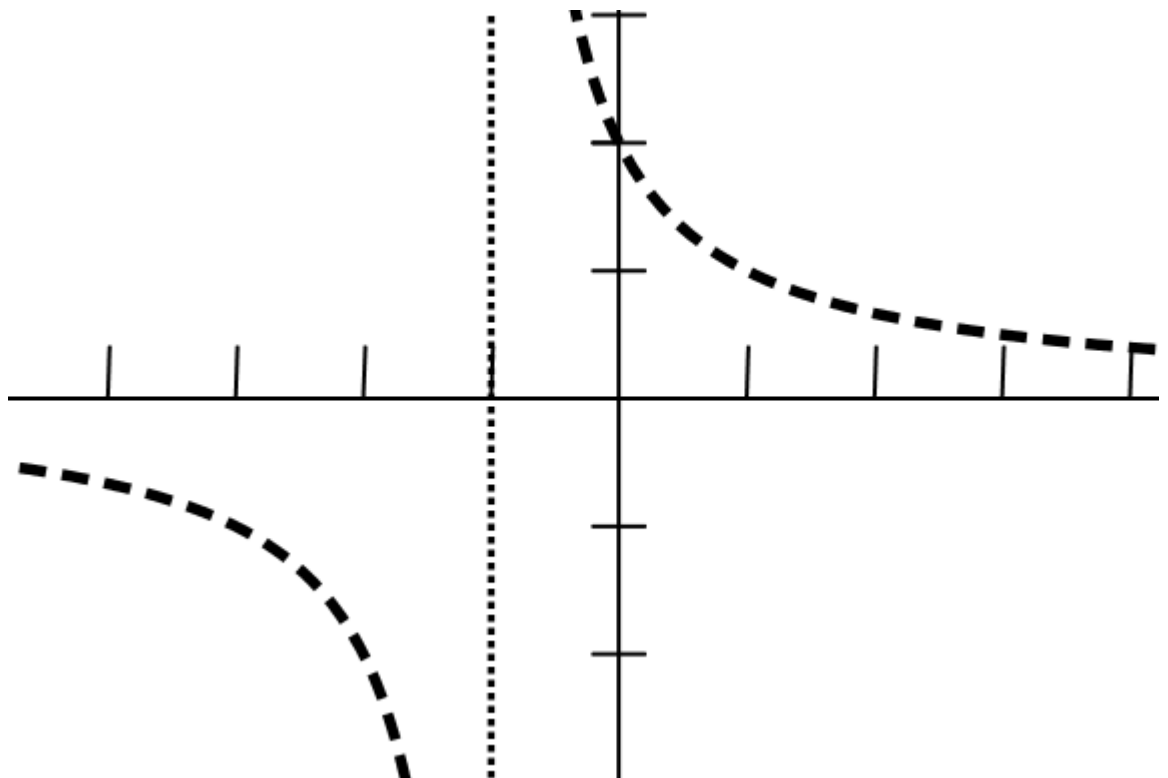
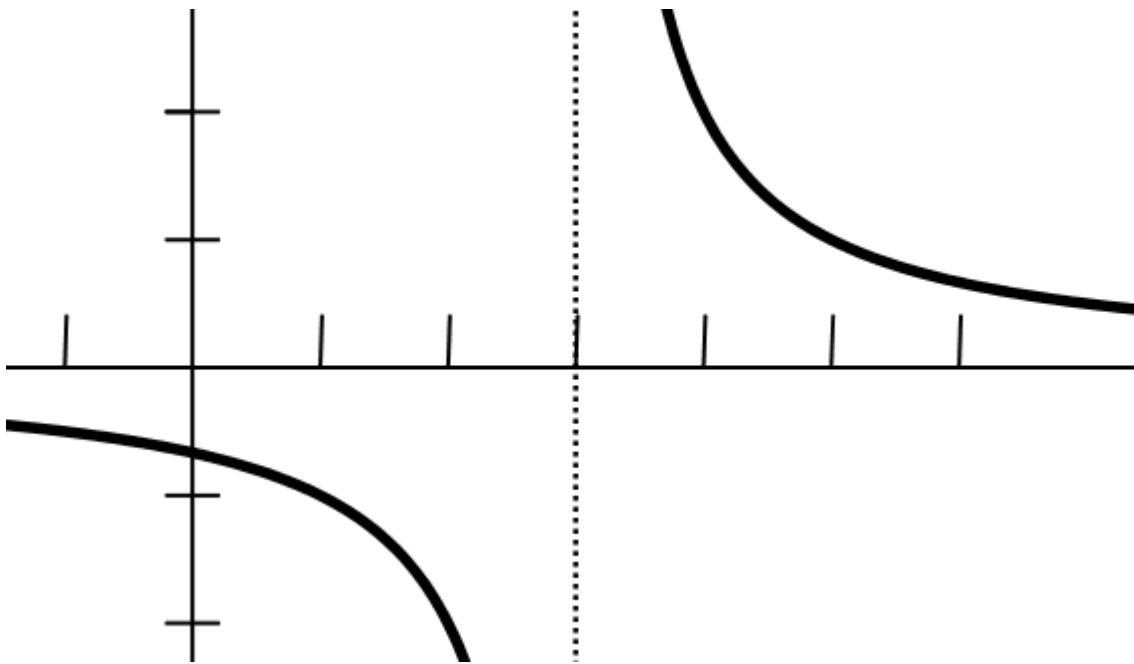
- - - -



f_gebr1.2: $f(x) = a/(x + b)$

$a > 0, b < 0$ —————

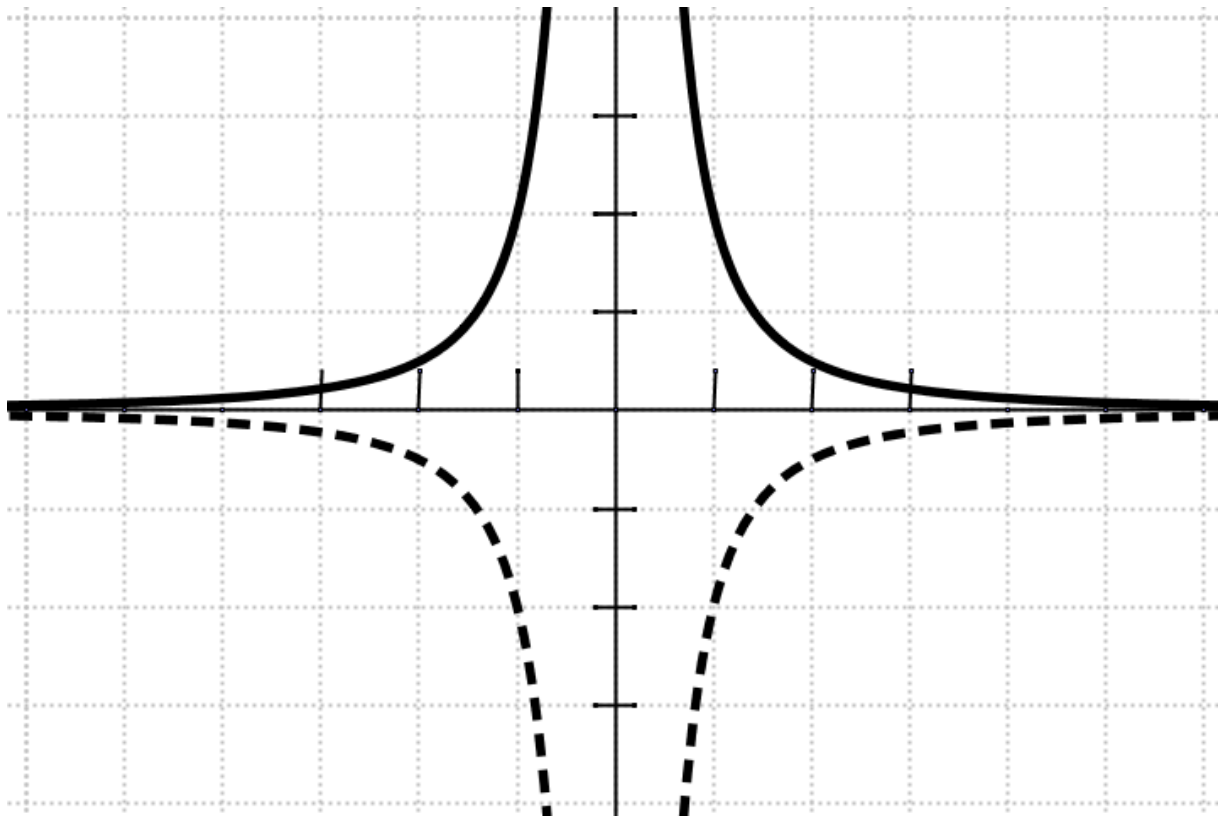
$a > 0, b > 0$ - - - - -



f_gebr2.1: $f(x) = a/x^2$

$a > 0$: ———

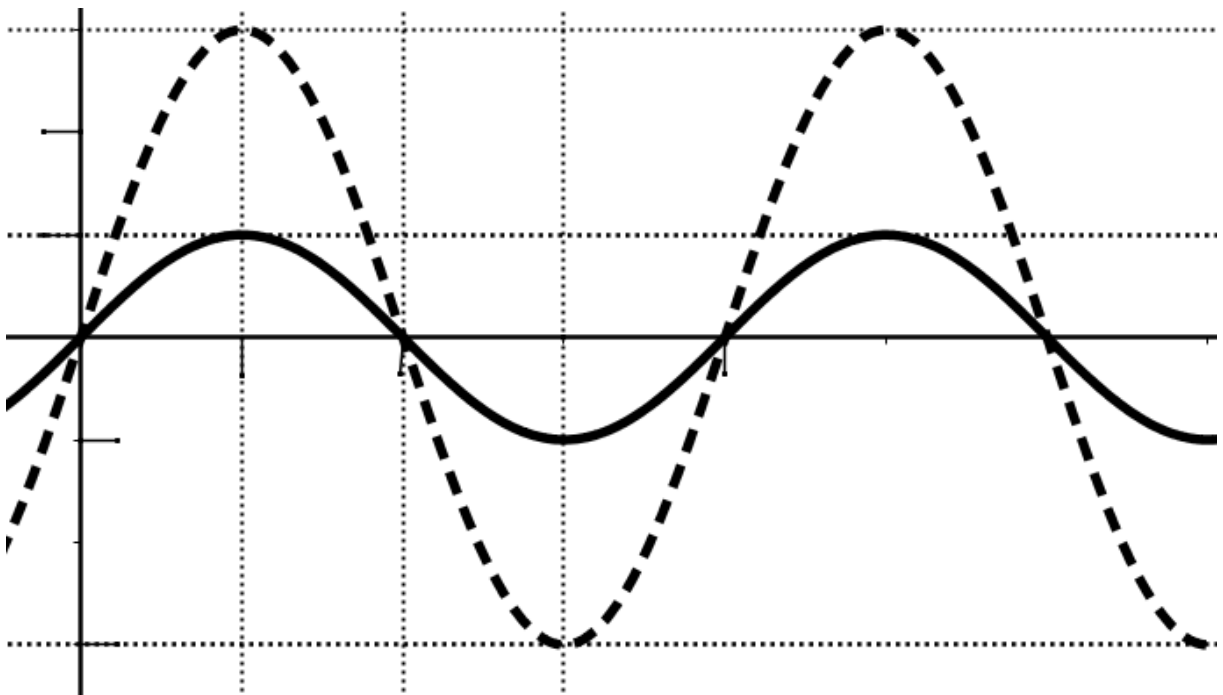
$a < 0$: - - - - -



f_sin.1: $f(x) = a \cdot \sin(x)$

$a = 1$: ———

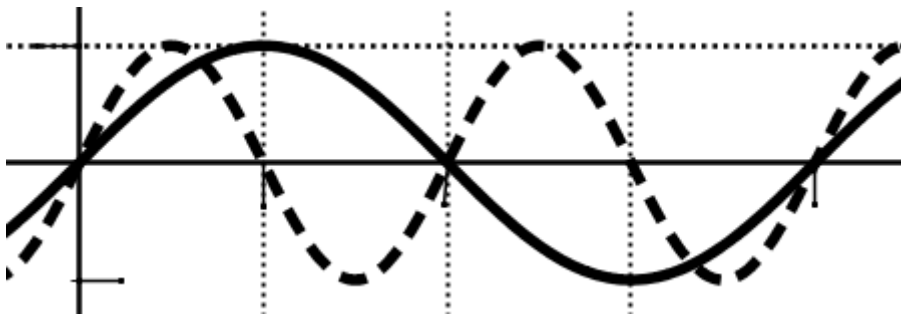
$a = 3$: - - - - -



f_sin.2: $f(x) = \sin(b \cdot x)$

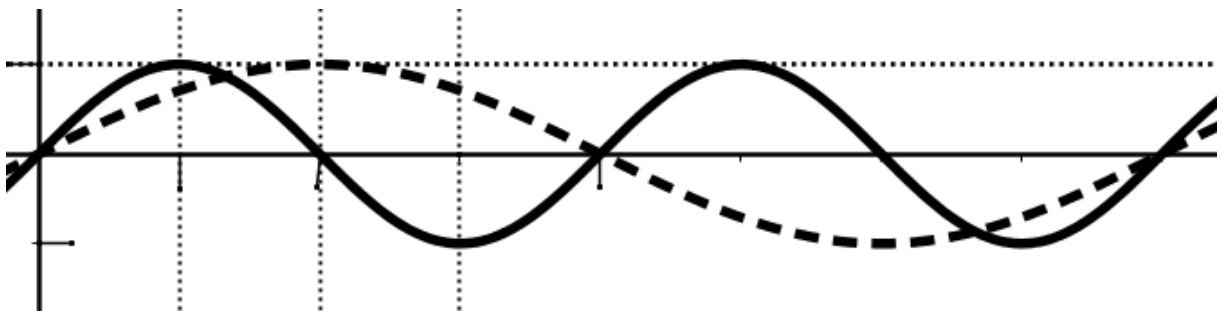
$b = 1$: _____

$b = 2$: - - - - -



$b = 1$: _____

$b = 1/2$: - - - - -



EK

$P(\cos(\alpha) | \sin(\alpha))$ •

