

Funktionen in 'R²

9. Schulstufe

Schwarzdruckkopiervorschläge mit großer Schrift
und starken Linien

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Inhalt: Grafiken zu den Themen: einem x-Wert werden mehr als ein y-Wert zugeordnet, lineare Funktion, quadratische Funktion, Polynomfunktion 3. Grades, Polynomfunktion 4. Grades, gerade Funktion, ungerade Funktion, gebrochen rationale Funktion mit x im Nenner, gebrochen rationale Funktion mit x^2 im Nenner, Sinusfunktion und Einheitskreis

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EK 31

Abkürzungen

f_lin: lineare Funktion

f_q: quadratische Funktion

f_G3: Funktion 3. Grades

f_G4: Funktion 4. Grades

f_g: gerade Funktion

f_u: ungerade Funktion

f_gebr1: gebrochen

rationale Funktion Grad 1

f_gebr2: gebrochen

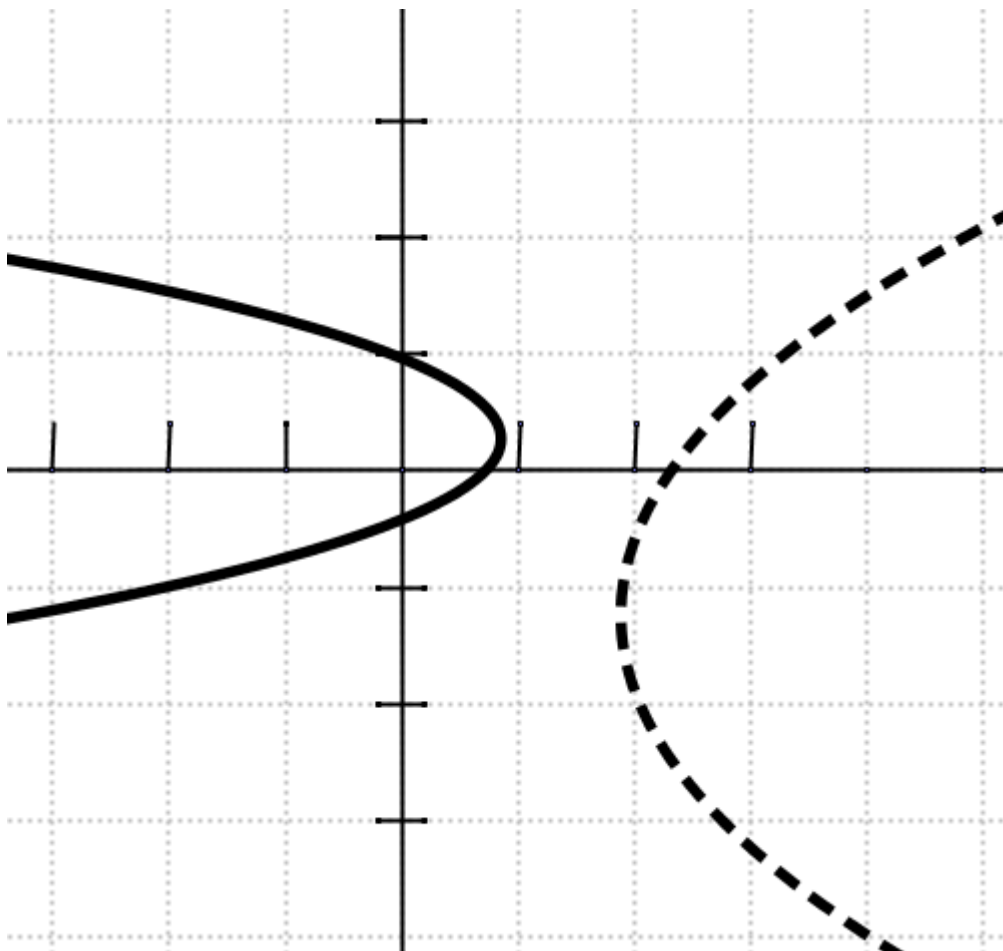
rationale Funktion Grad 2

f_sin: Winkelfunktion

EK: Einheitskreis

keine Funktionen

mehr y-Werte zu einem x



f_lin: $f(x) = k * x + d$

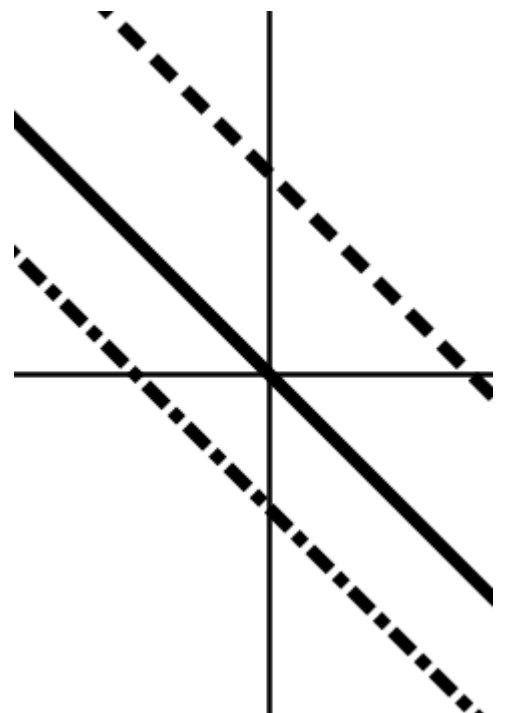
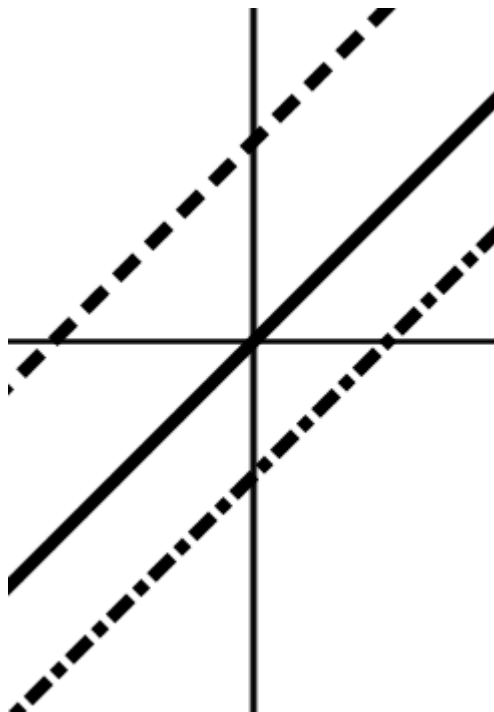
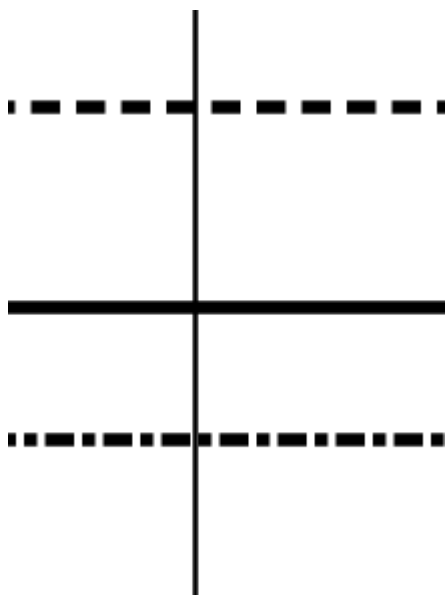
$$f(x) = k * x + d$$

$d = 0$: ———

$d > 0$: - - - - -

$d < 0$: - · - · - · -


$k = 0$ \parallel $k > 0$ \parallel $k < 0$



f_q .1: $f(x) = a * x^2$

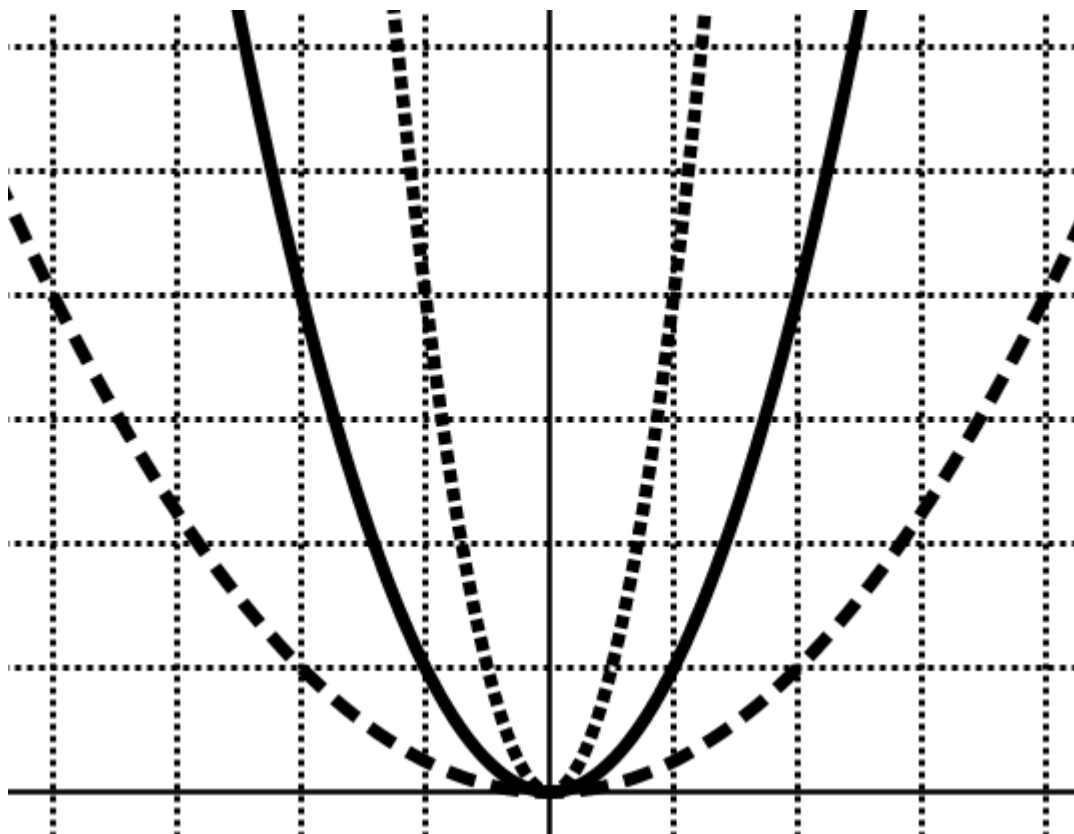
Parabel nach oben offen:

$a > 0$: 

$f(x) = x^2$; $a = +1$: 


$f(x) = 1/4 * x^2$; $a = 1/4$: 

$f(x) = 4 * x^2$; $a = 4$: 




$$f_{-q/2}: f(x) = a \cdot x^2$$

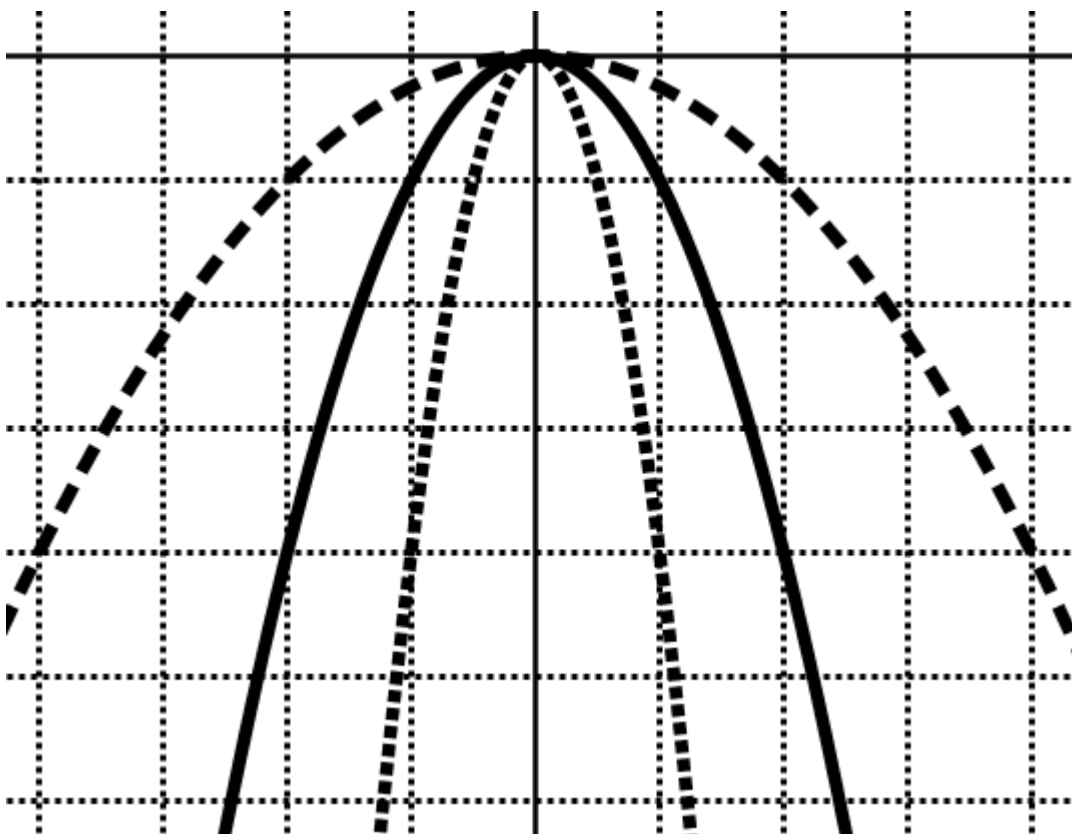
Parabel nach unten offen:

$a < 0$: 

$f(x) = -x^2$; $a = -1$: 

$f(x) = -1/4 \cdot x^2$; $a = -1/4$: 

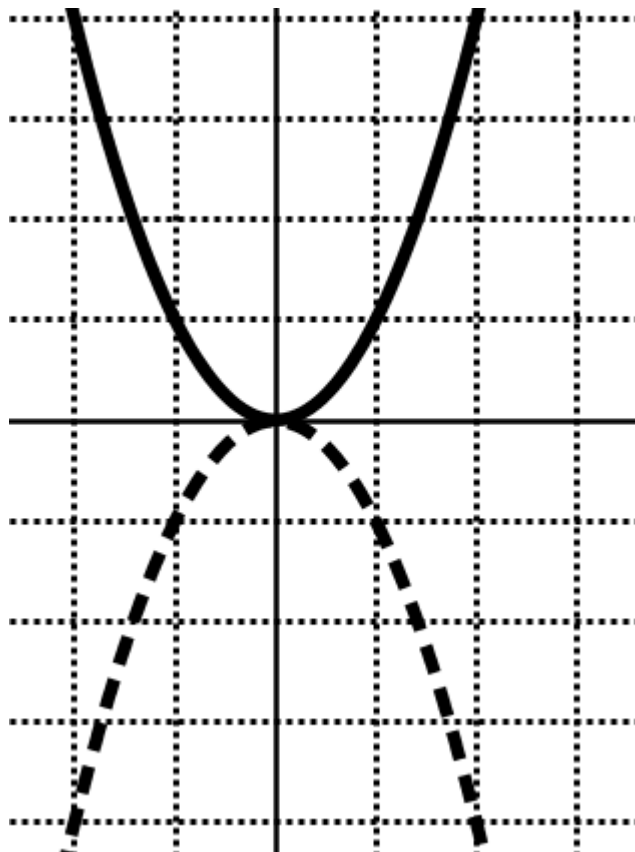
$f(x) = -4 \cdot x^2$; $a = -4$: 



f_q.3: $f(x) = a \cdot x^2$

Parabel spiegeln

$a = 1$: — || $a = -1$: - - - - -



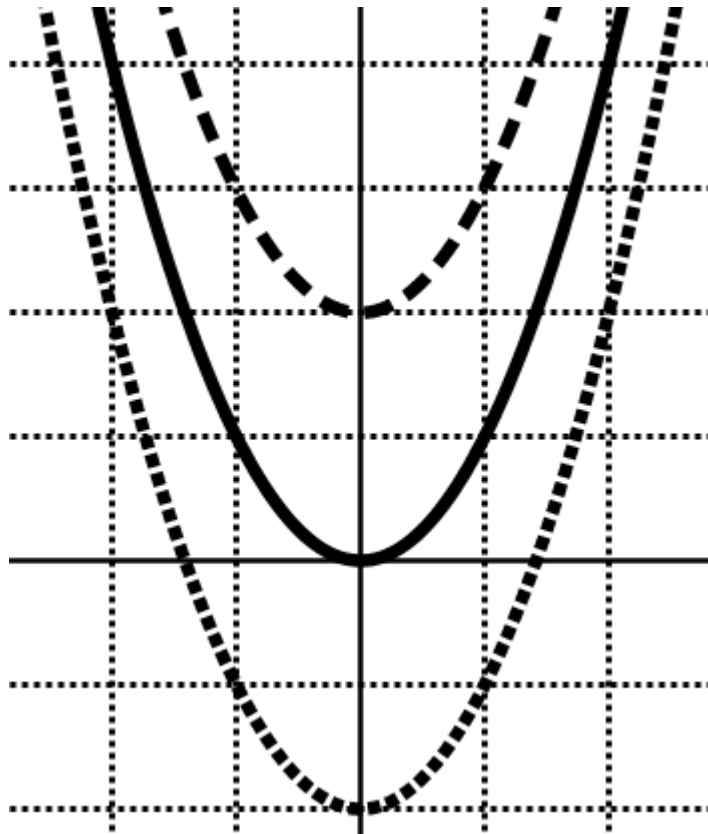
f_q.4: $f(x) = x^2 + c$

senkrecht verschieben

$c = 0$ ($f(x) = x^2$): ———

$c > 0$ (hinauf): - - - - -

$c < 0$ (hinunter):
.....



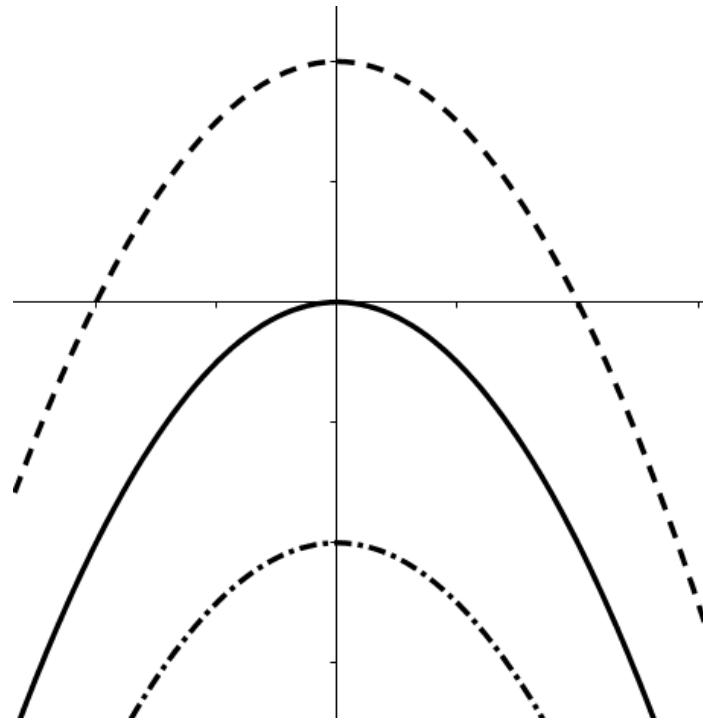
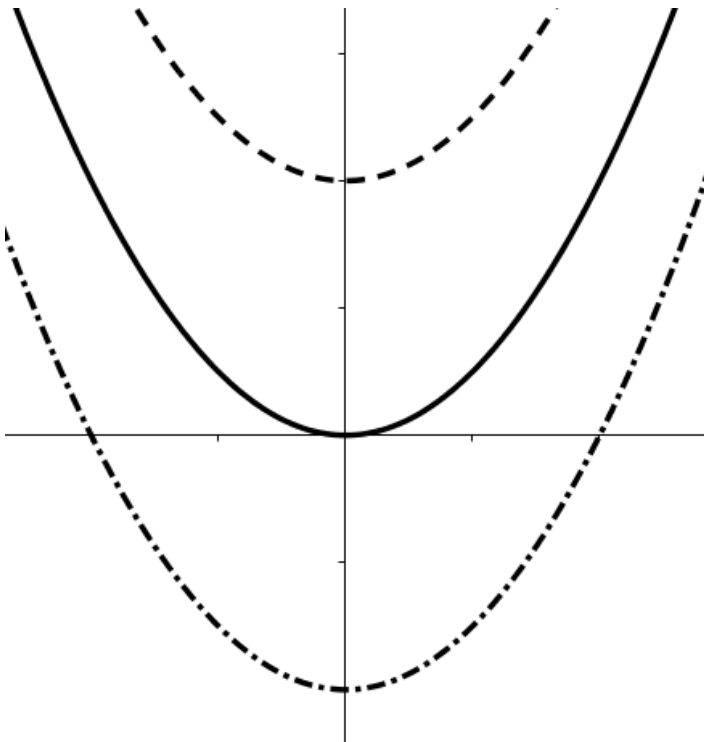
f_q.5: $f(x) = a \cdot x^2 + c$

$c = 0$: ———

$c > 0$: - - - -

$c < 0$: — . —

$a > 0$ || $a < 0$



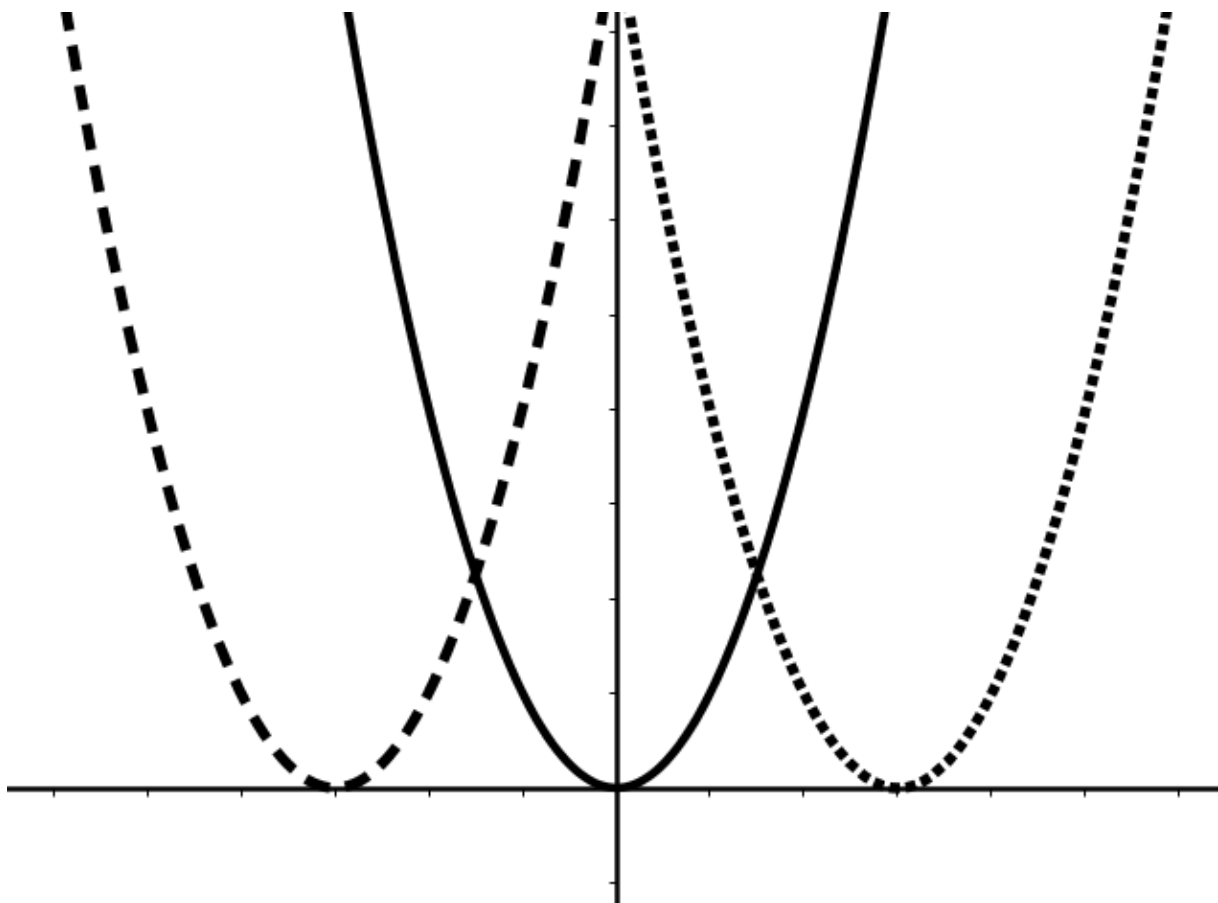
f_q.6: $f(x) = (x + b)^2$

waagrecht verschieben

$b = 0$ ($f(x) = x^2$): ———

$b > 0$ (nach links): - - - -

$b < 0$ (nach rechts):

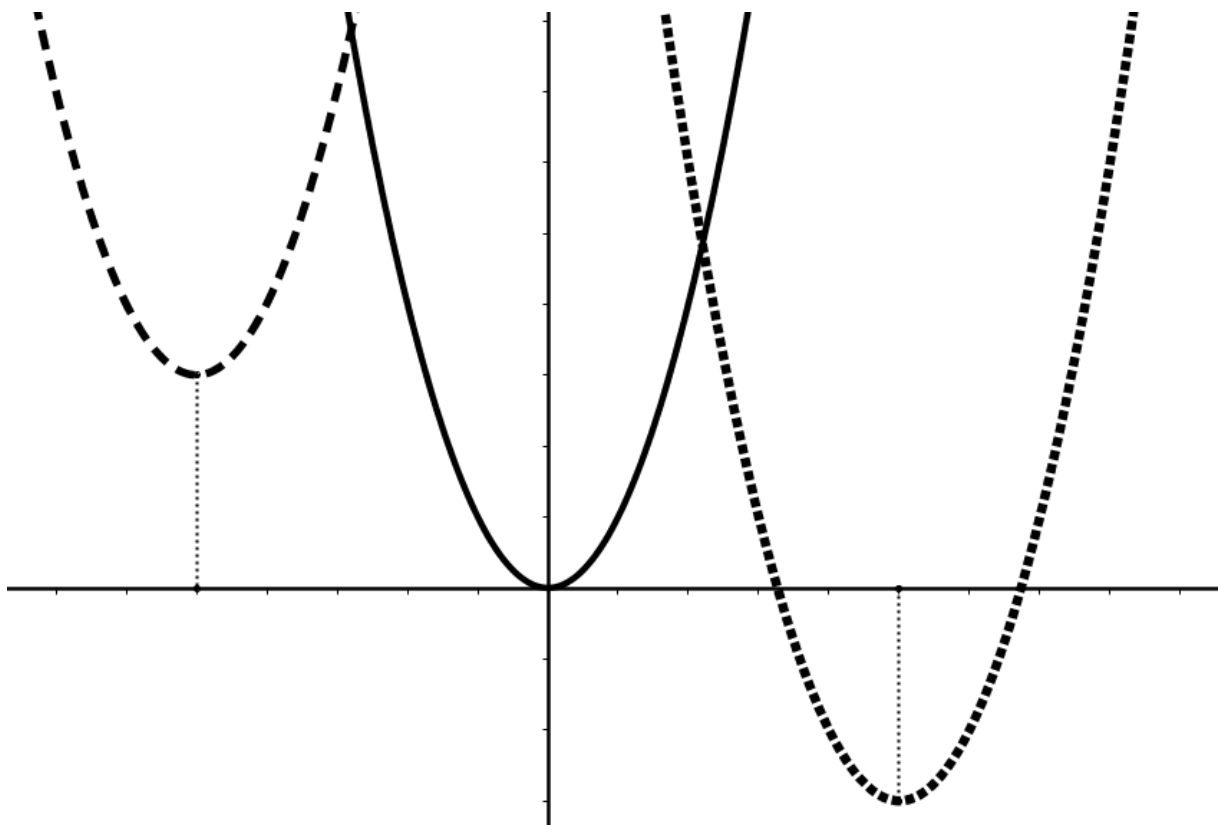


f_q.7: $f(x) = (x + b)^2 + c$

$b = 0, c = 0$ ($f(x) = x^2$): ———

$b > 0, c > 0$ (li, hinauf): - - - -

$b < 0, c < 0$ (re, hinunter):

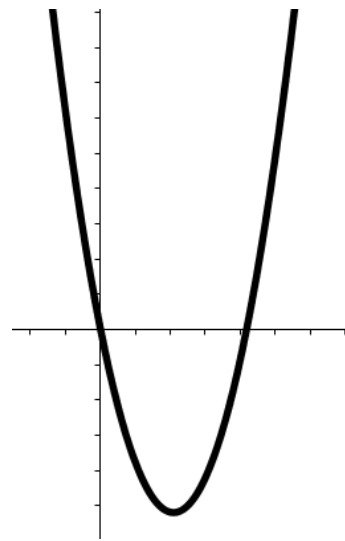
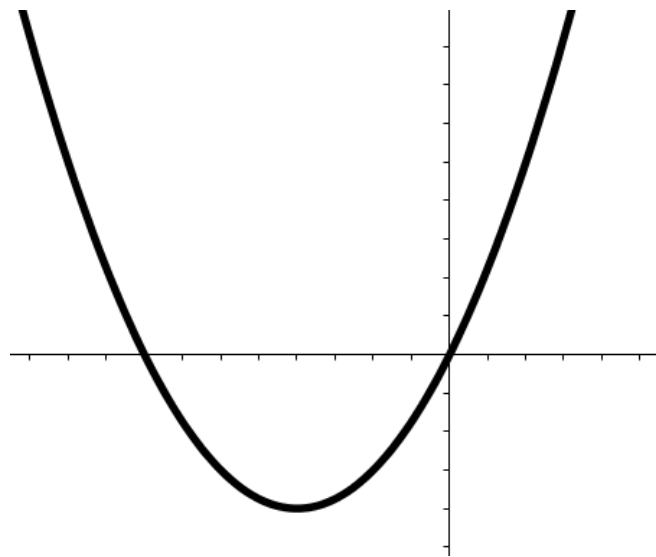


f_q.8: $f(x) = a \cdot x^2 + b \cdot x$

enthält Ursprung (0|0)

$a > 0, b > 0$

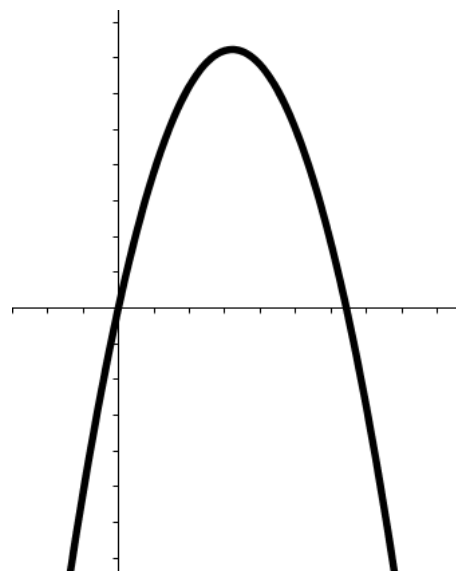
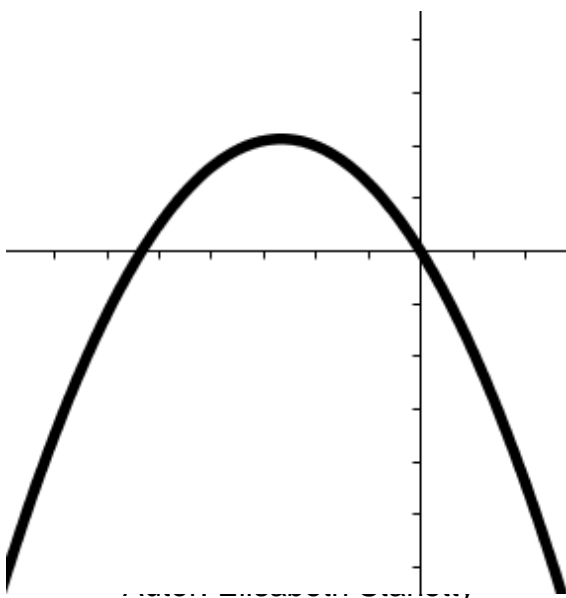
$a > 0, b < 0$



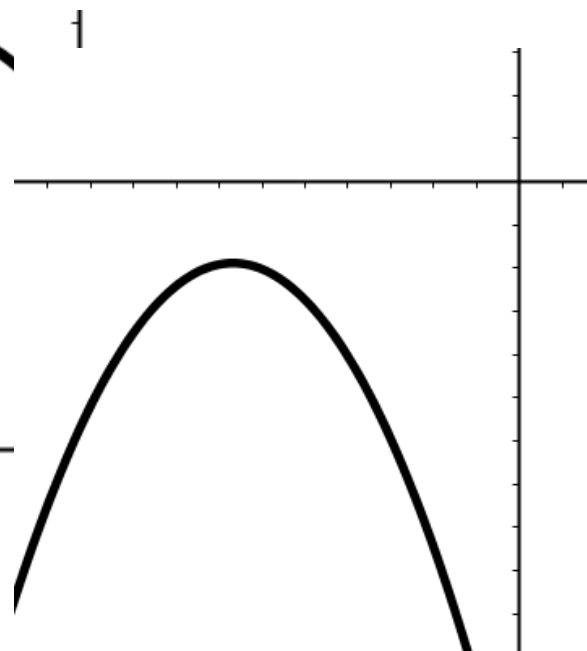
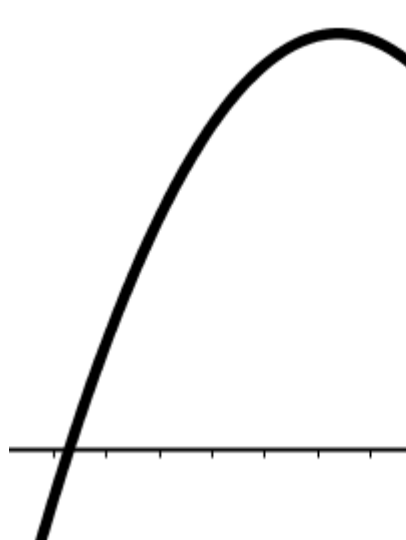
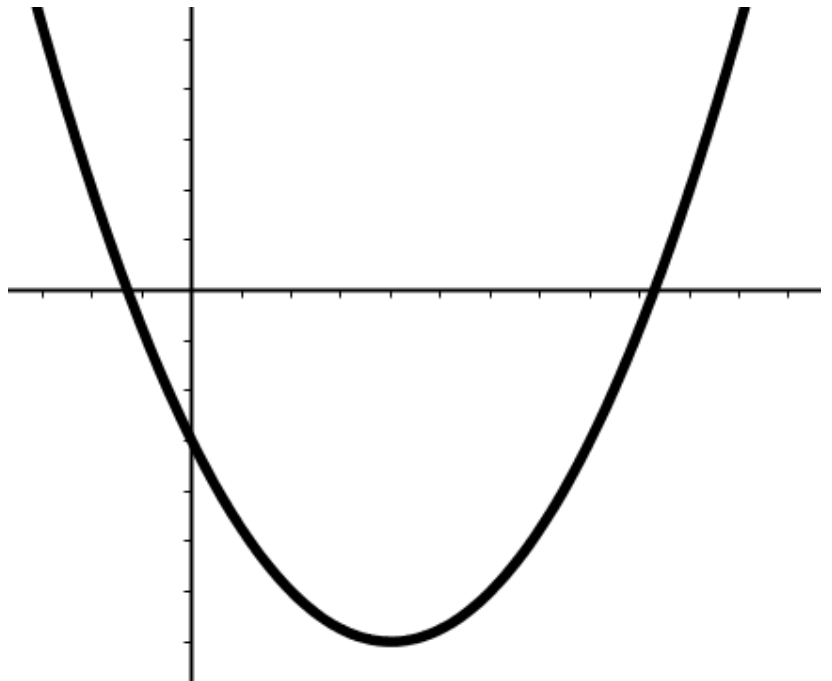
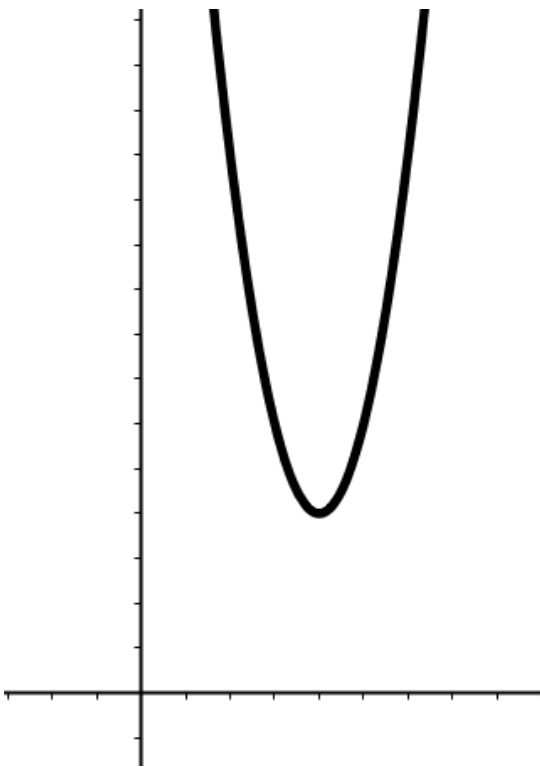
a

$a < 0, b > 0$

$a < 0, b < 0$



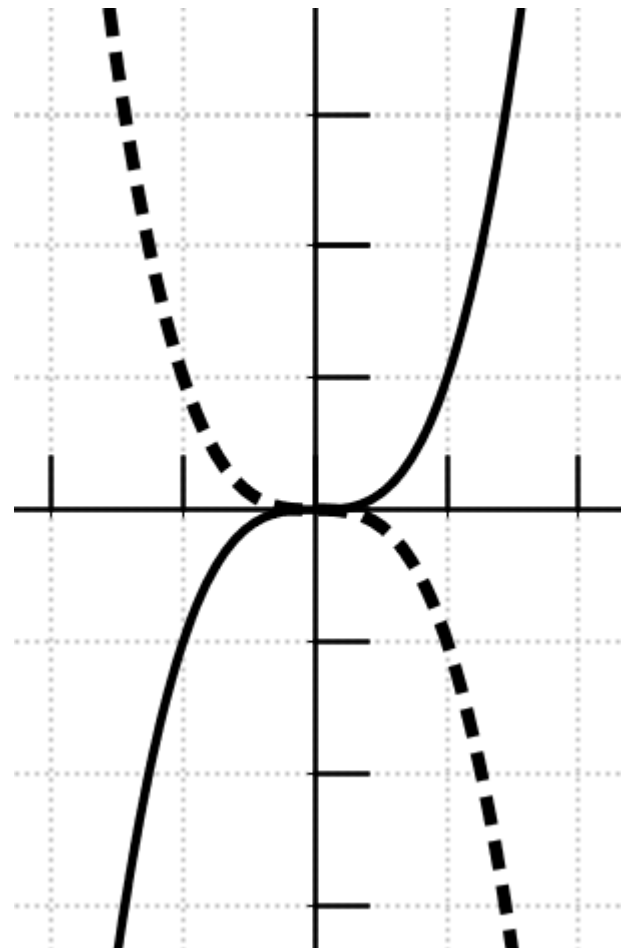
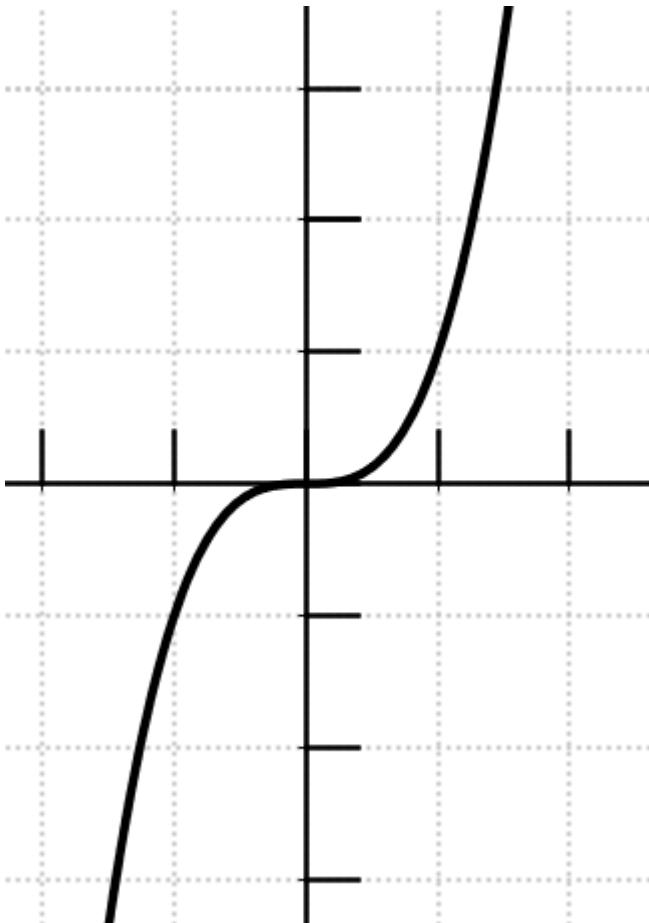
f_{q.9}: f: a * x² + b * x + c



f_G3.1: $f(x) = a * x^3$

$a = 1$ ($f(x) = x^3$): ———

$a = -1$ ($f(x) = -x^3$): - - - -



$$f_G3.2: f(x) = a * x^3 + c$$

senkrecht verschieben

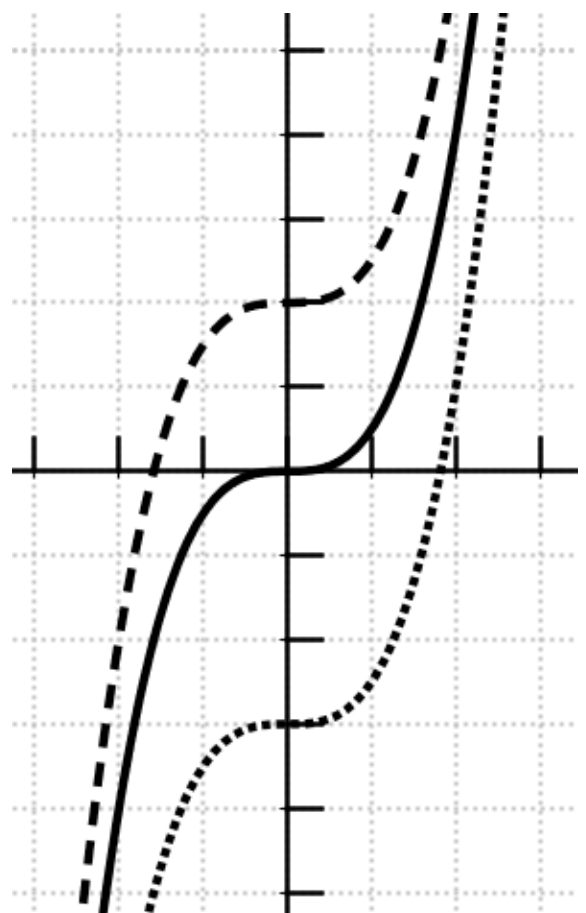
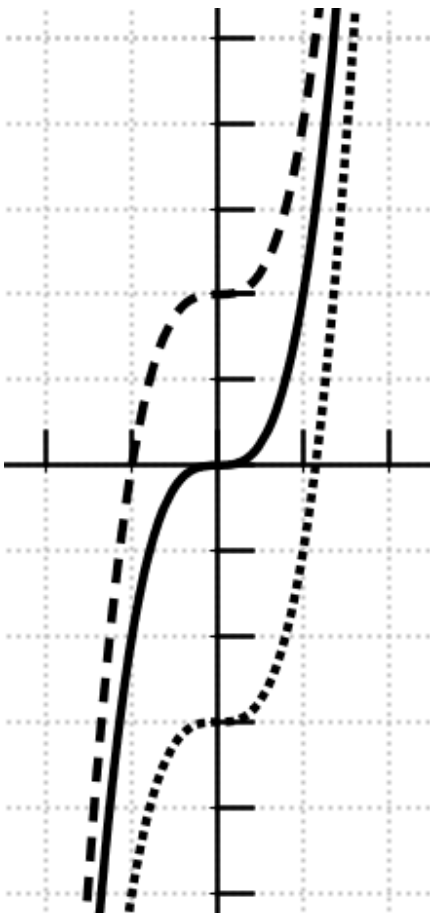
$a > 0, c = 0$: ———

$a > 0, c > 0$ (hinauf): - - - -

$a > 0, c < 0$ (hinunter):

$a=2$

$a = 0,5$



$$f_{G3.3}: f(x) = a \cdot x^3 + c$$

senkrecht verschieben

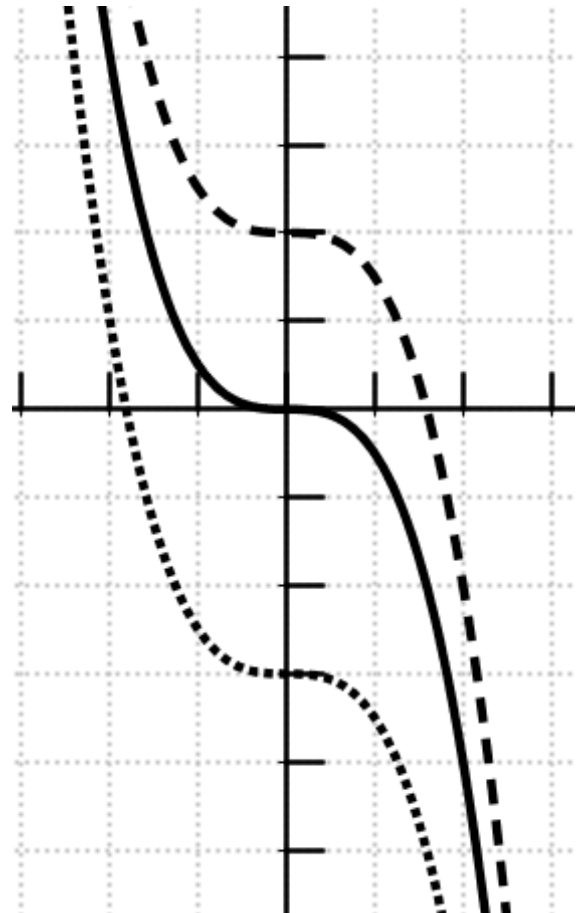
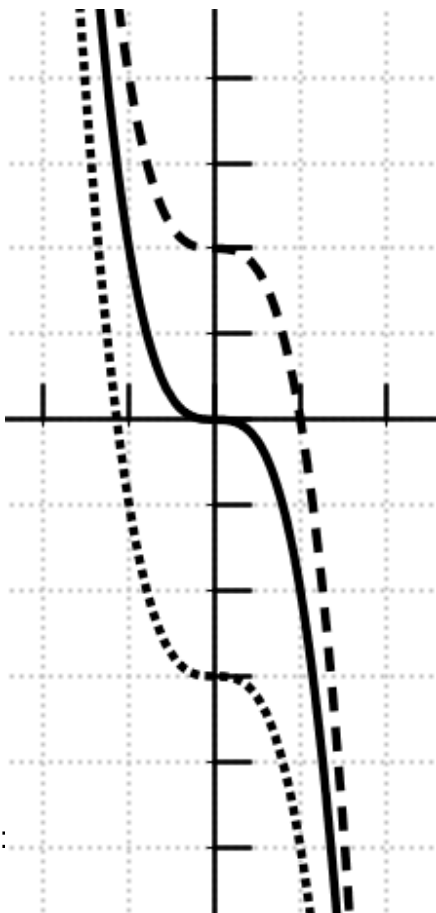
$a < 0, c = 0$: ———

$a < 0, c > 0$ (hinauf): - - - -

$a < 0, c < 0$ (hinunter):

$a = -2$

$a = -0,5$



$$f_G3.4: f(x) = (x + b)^3$$

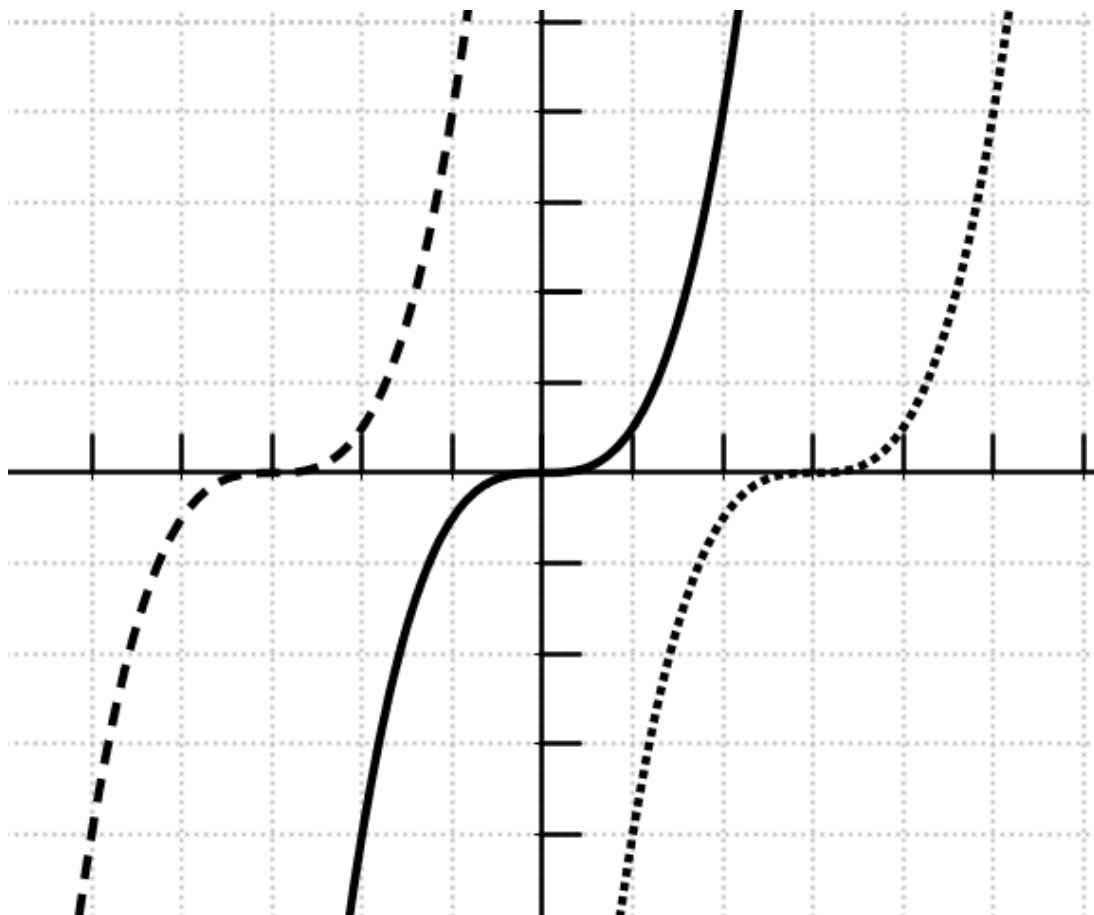
waagrecht verschieben

$a > 0, b = 0$: ———

$a > 0, b > 0$ (nach links: - - - -

$a > 0, b < 0$ (n. rechts):

$$a = 0,5$$



$$f_G3.5: f(x) = (x + b)^3$$

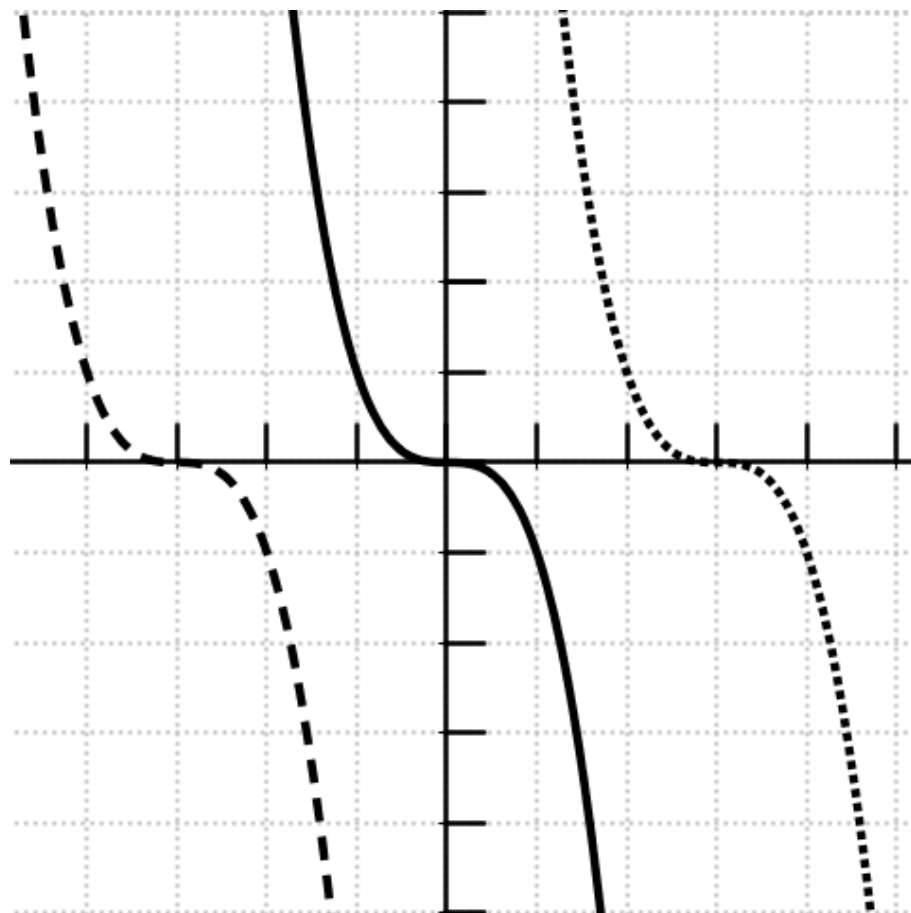
waagrecht verschieben

$a < 0, b = 0$: ———

$a < 0, b > 0$ (nach links: - - - -

$a < 0, b < 0$ (n. rechts):

$$a = -1$$

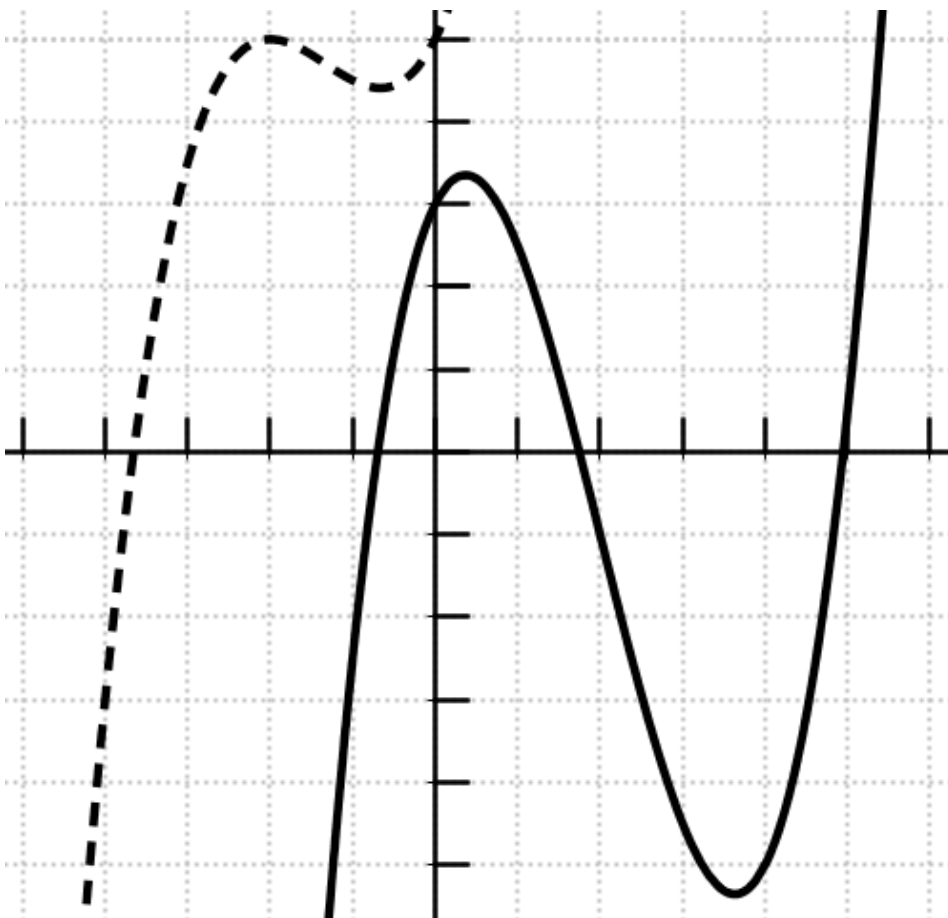


$$f_{G3.6}: a \cdot x^3 + b \cdot x^2 + c \cdot x + d$$

enthält Punkt $(0|d)$

1 bis 3 Nullstellen

$a > 0$: beginnt steigend

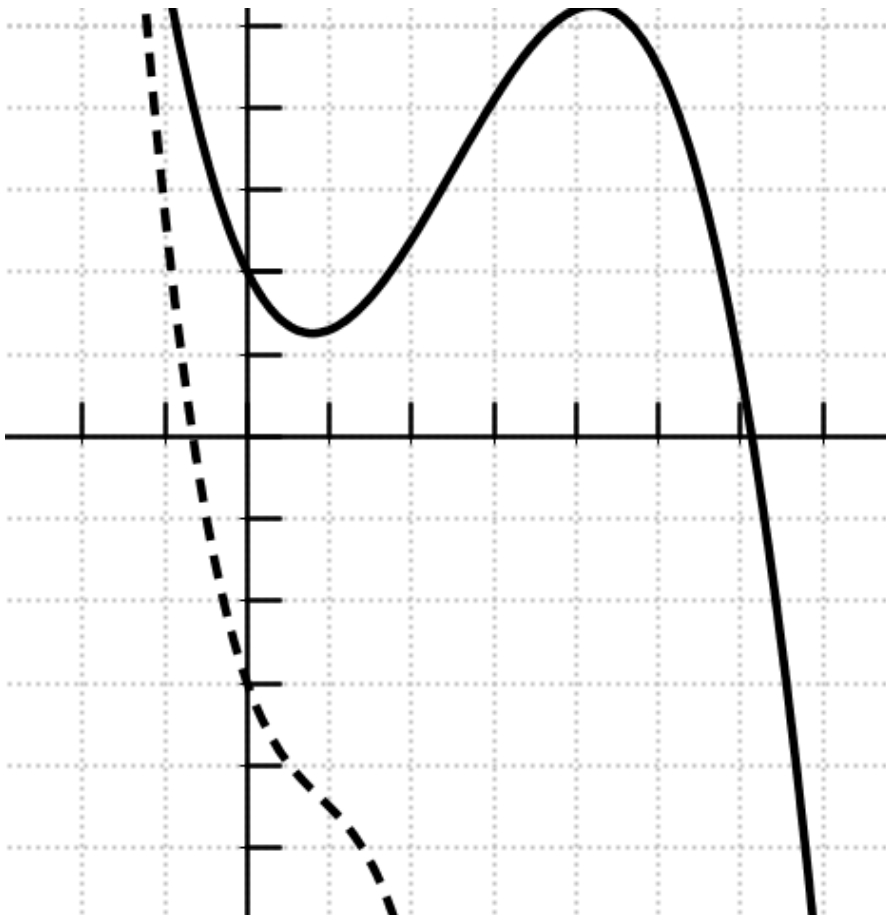


$$f_{G3.7}: a \cdot x^3 + b \cdot x^2 + c \cdot x + d$$

enthält Punkt $(0|d)$

1 bis 3 Nullstellen

$a < 0$: beginnt fallend



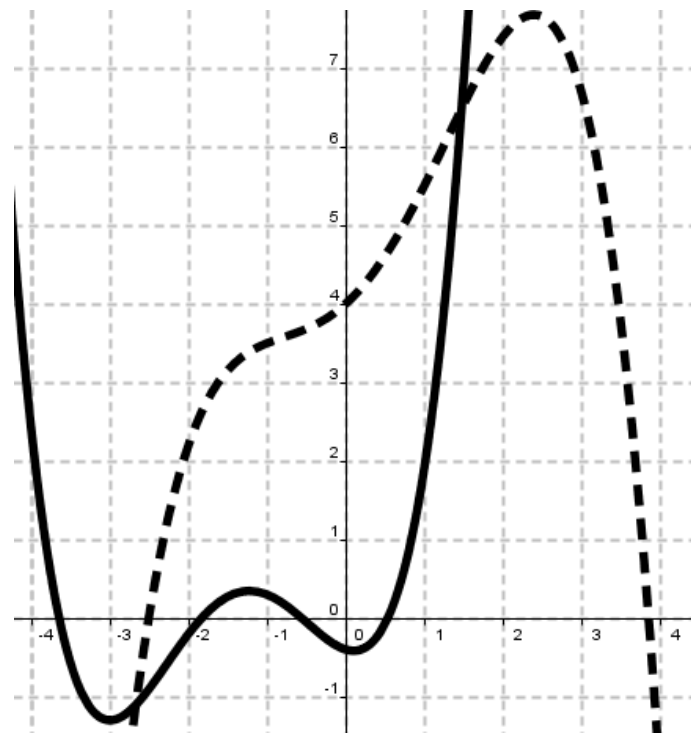
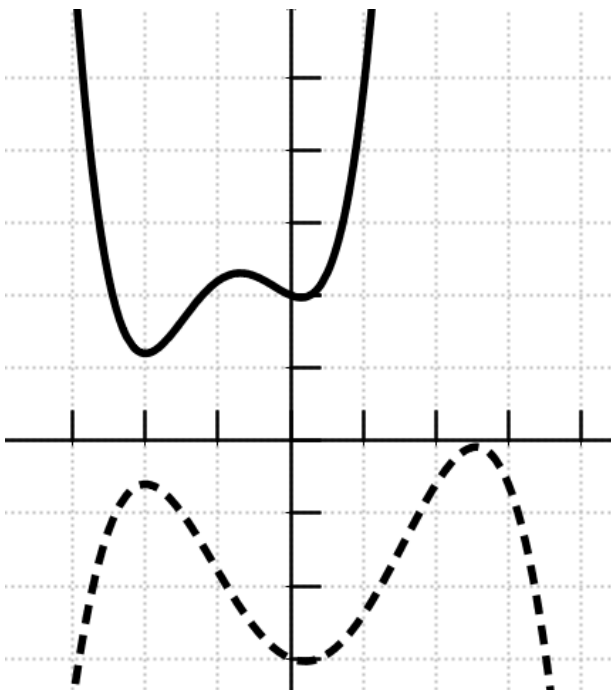
$$f_G4.1: f(x) = a \cdot x^4 + b \cdot x^3 + c \cdot x^2 + d \cdot x + e$$

enthält Punkt $(0|e)$,

0 bis 4 Nullstellen

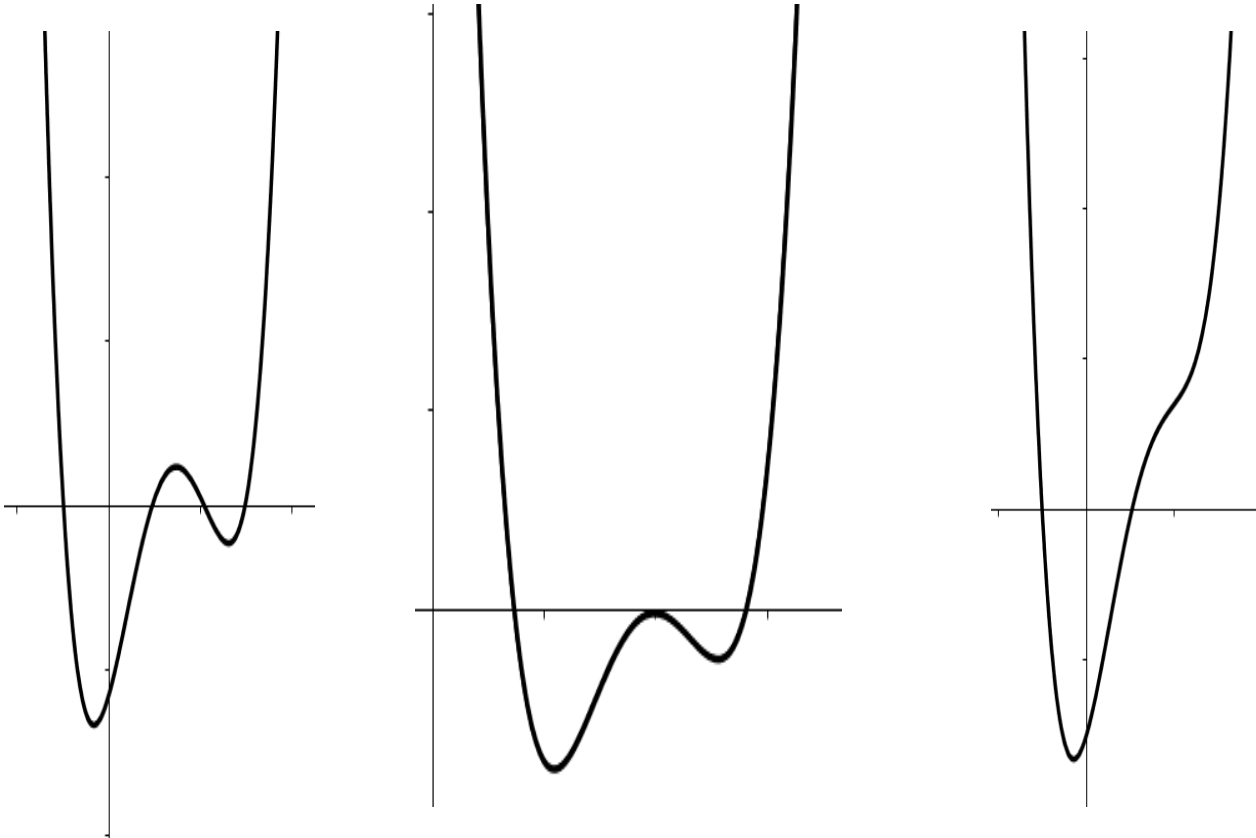
$a > 0$: beginnt fallend

$a < 0$: beginnt steigend



$$f_G4.2: f(x) = a * x^4 + b * x^3 + c * x^2 + d * x + e$$

Doppel-S-Kurve
verschiedenste
Ausprägungen



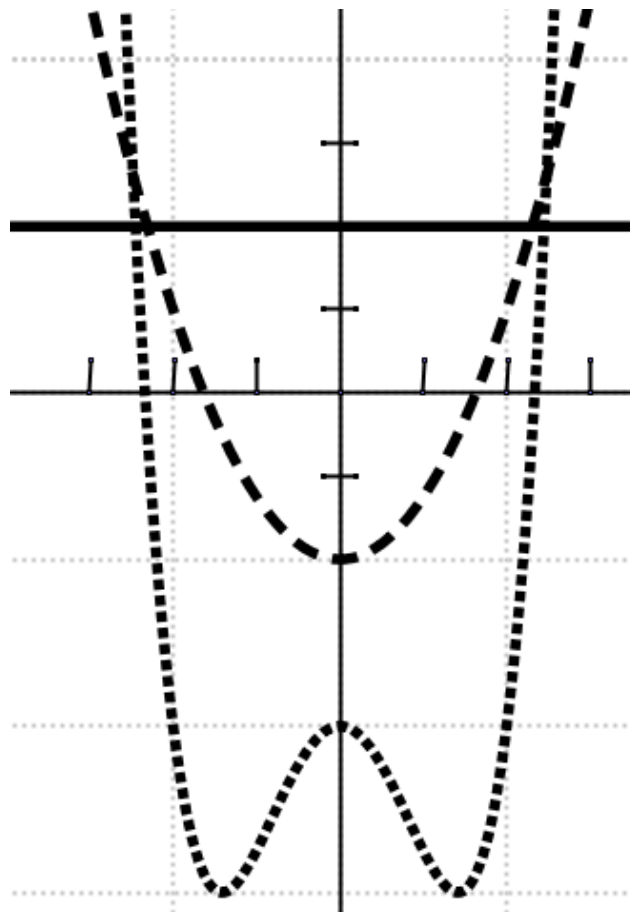
f_g: Hochzahl gerade

Symmetrisch zur
senkrechten Achse, $a \neq 0$

$$f(x) = a \cdot x^0 = a \quad \text{—————}$$

$$f(x) = a \cdot x^2 + b \quad \text{-----}$$

$$f(x) = a \cdot x^4 + b \cdot x^2 + c \quad \text{.....}$$



f_u: Hochz. ungerade

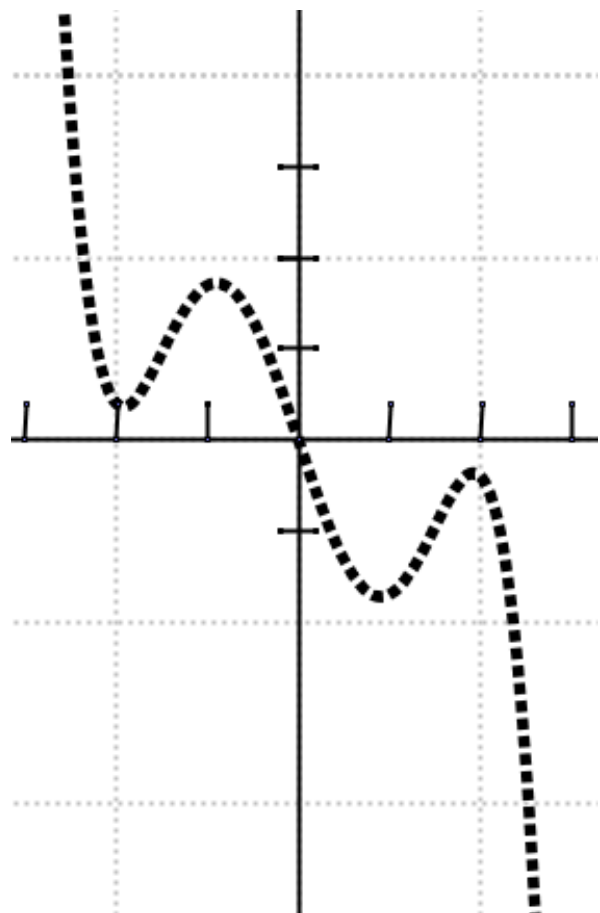
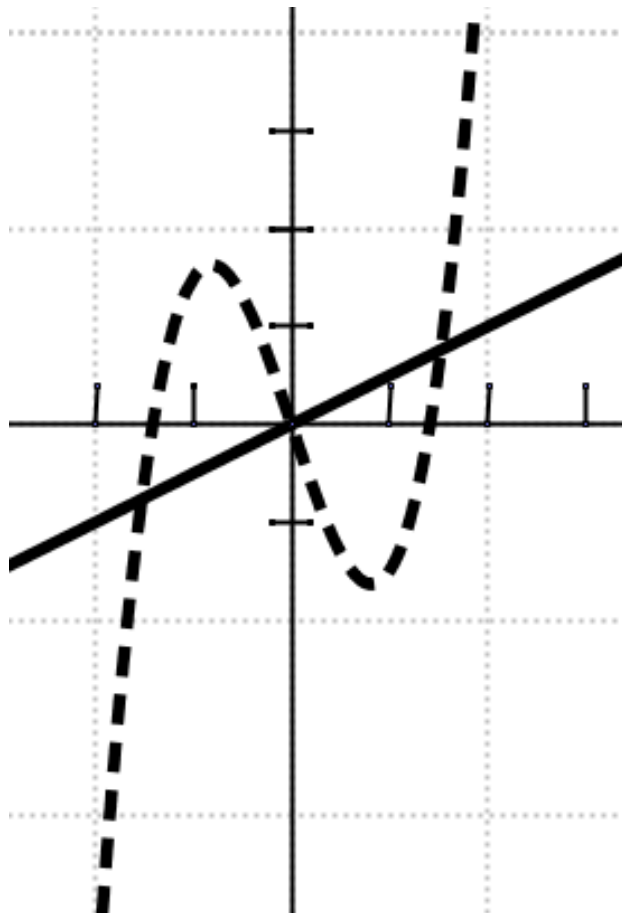
Symmetrisch zum

Ursprung, $a \neq 0$

$$f(x) = a \cdot x \quad \text{—————}$$

$$f(x) = a \cdot x^3 + b \cdot x \quad \text{-----}$$

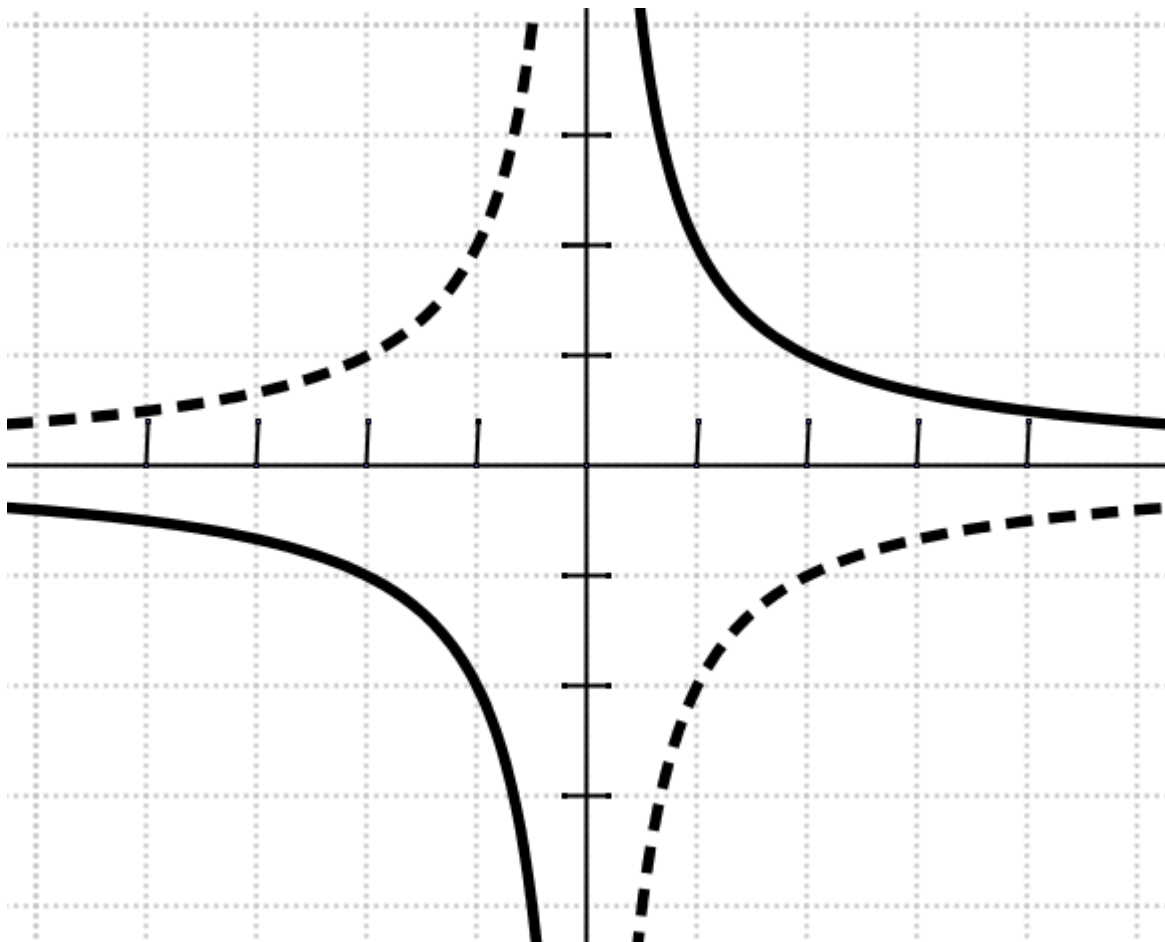
$$f(x) = a \cdot x^5 + b \cdot x^3 + c \cdot x \quad \text{.....}$$



f_gebr1.1: $f(x) = a/x$

$a > 0$ mit $(1|a)$ —————

$a < 0$ mit $(-1|a)$ - - - - -



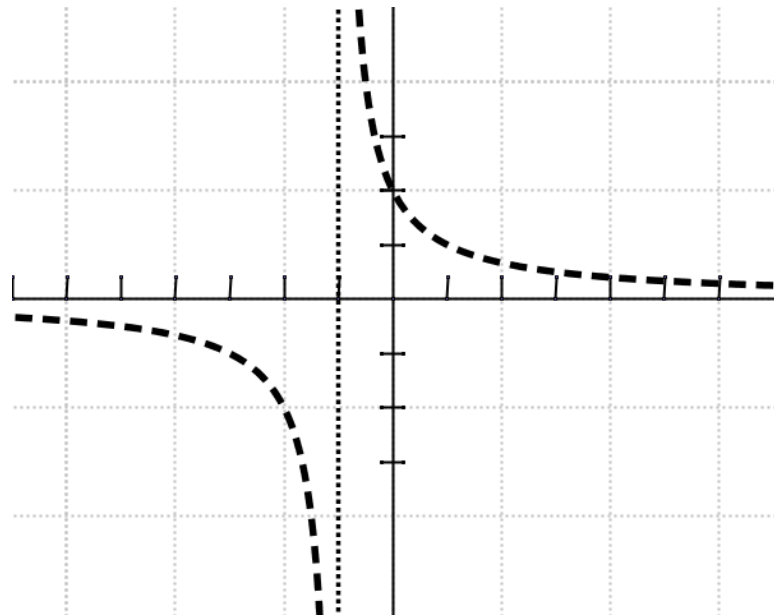
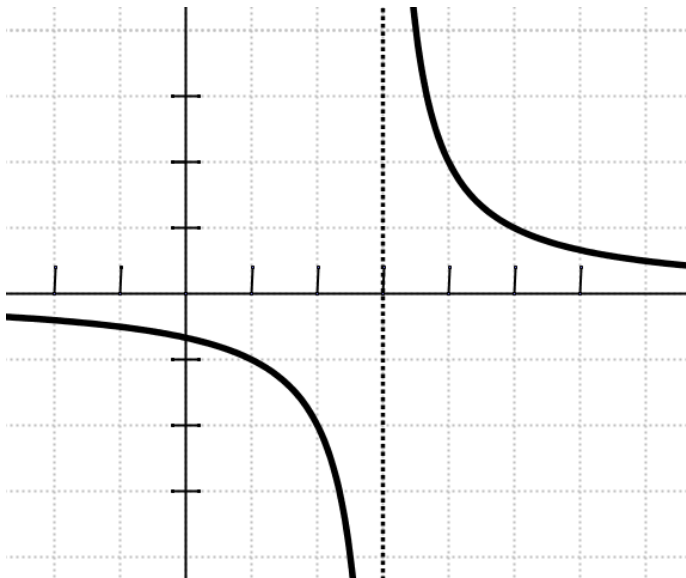
f_gebr1.2: $f(x) = a/(x + b)$

$a > 0, b < 0$

————

$a > 0, b > 0$

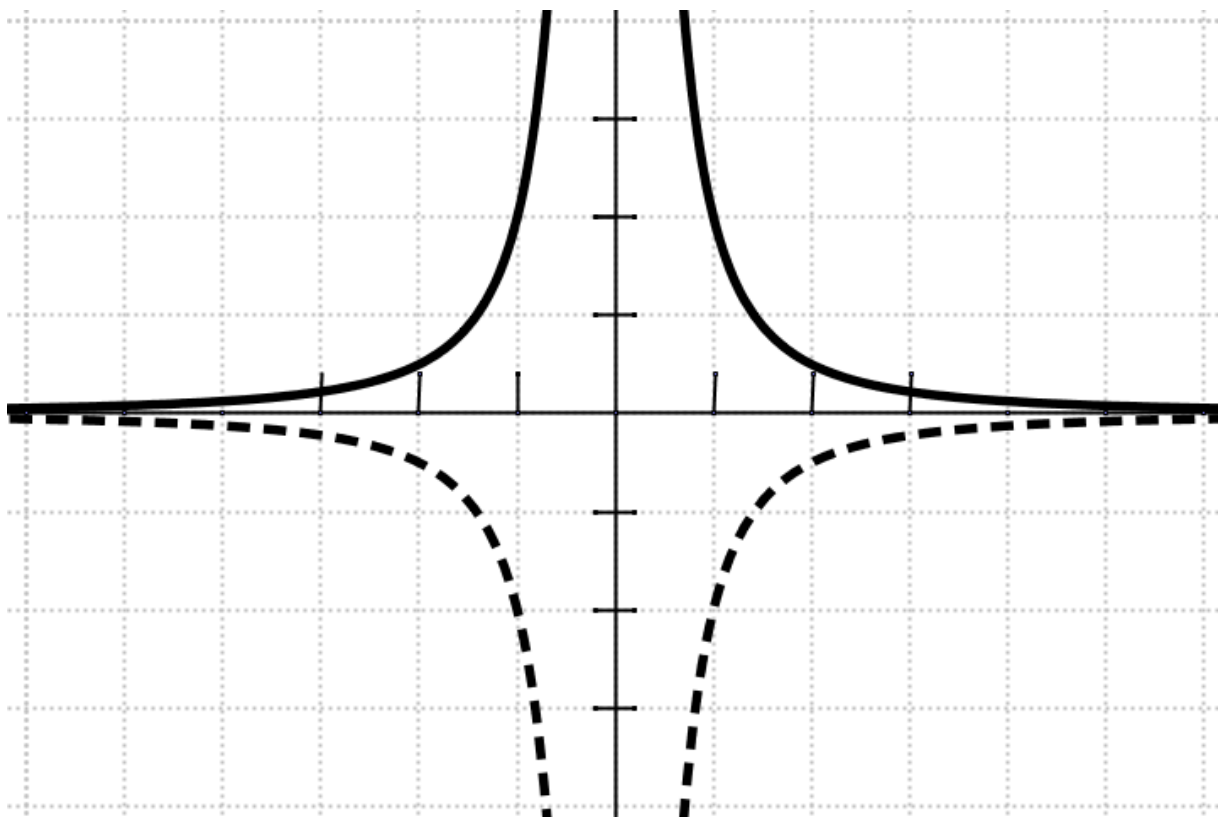
- - - -



$f_{\text{gebr2.1}}: f(x) = a/x^2$

$a > 0$: 

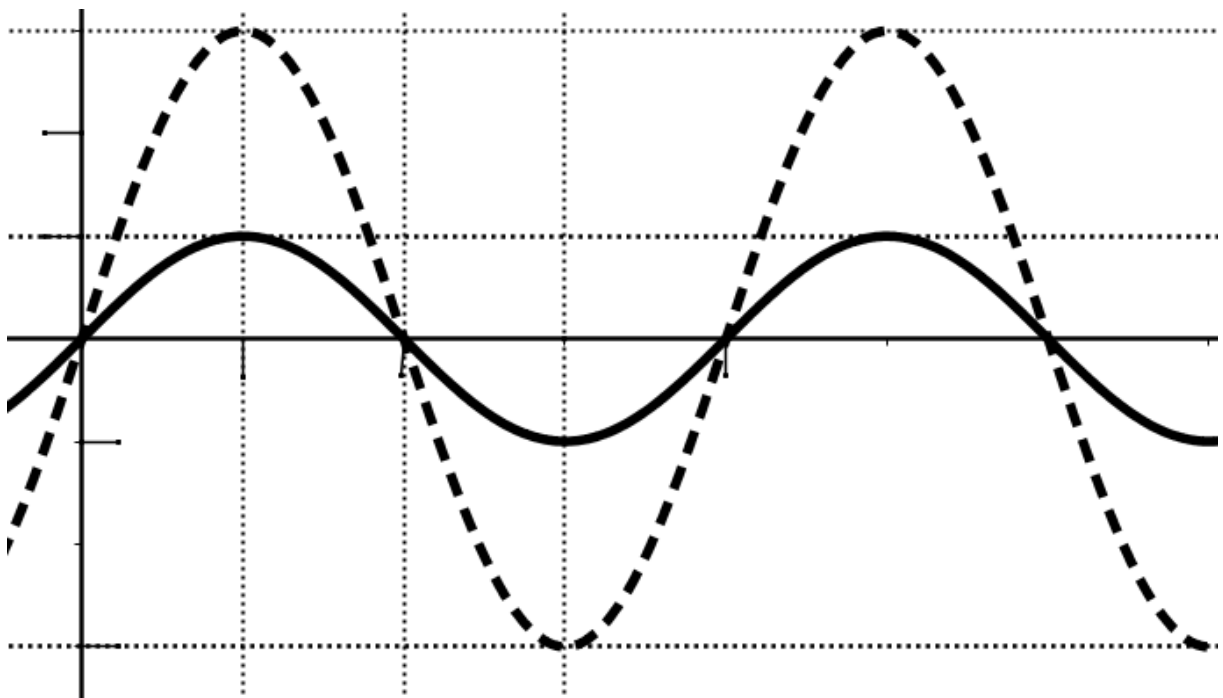
$a < 0$: 



f_sin.1: $f(x) = a \cdot \sin(x)$

a = 1: 

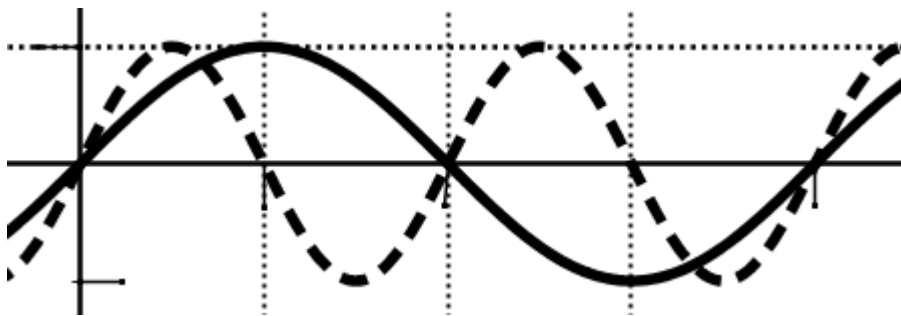
a = 3: 



f_sin.2: $f(x) = \sin(b \cdot x)$

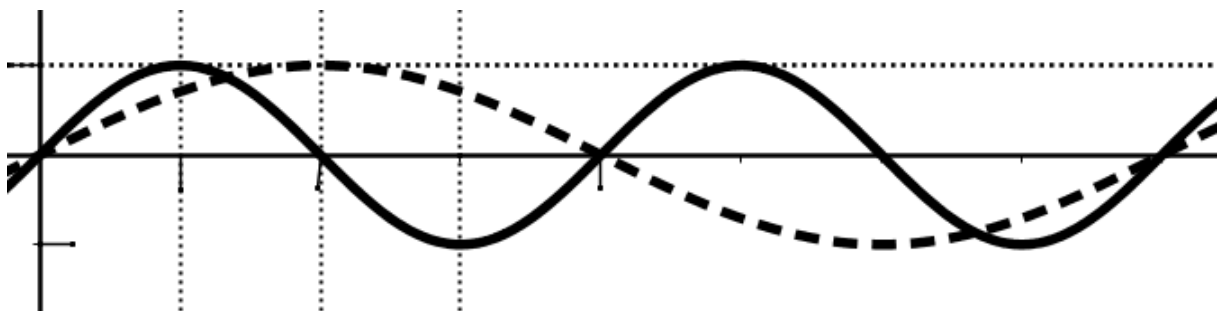
$b = 1$: 

$b = 2$: 



$b = 1$: 

$b = 1/2$: 



EK

$P(\cos(\alpha) | \sin(\alpha))$ •

